

Evidence for spatial variation of α

- Webb, King, Murphy, Flambaum, Carswell, Bainbridge, arxiv:1008.3907,

$$\alpha(x) = \alpha(0) + \alpha'(0)x + \dots$$

$x = r \cos(\phi)$, $r = ct$ – distance (instead of time)

Reconciles all measurements of the variation

- Berengut, Flambaum, arxiv:1008.3957

Manifestations on atomic clocks, Oklo, meteorites and cosmological phenomena

- Berengut, Flambaum, King, Curran, Webb,

Further evidence

Variation of Fundamental Constants

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Motivation

- **Extra space dimensions** (Kaluza-Klein, Superstring and M-theories). Extra space dimensions is a common feature of theories unifying **gravity** with other interactions. Any change in size of these dimensions would manifest itself in the 3D world as variation of fundamental constants.
- **Scalar fields** . Fundamental constants depend on scalar fields which vary in space and time (variable vacuum dielectric constant ϵ_0). May be related to “dark energy” and accelerated expansion of the Universe..
- **“Fine tuning”** of fundamental constants is needed for humans to exist. Example: low-energy resonance in production of carbon from helium in stars ($\text{He}+\text{He}+\text{He}=\text{C}$). Slightly different coupling constants — no resonance — no life.

Variation of coupling constants in space provide natural explanation of the “fine tuning”: we appeared in area of the Universe where values of fundamental constants are suitable for our existence.

Search for variation of fundamental constants

- Big Bang Nucleosynthesis
- Quasar Absorption Spectra ¹
- Oklo natural nuclear reactor
- Atomic clocks ¹
- Enhanced effects in atoms ¹, molecules¹ and nuclei
- Dependence on gravity

evidence?

evidences?

¹ *Based on atomic and molecular calculations*

Dimensionless Constants

Since variation of dimensional constants cannot be distinguished from variation of units, it only makes sense to consider variation of dimensionless constants.

- **Fine structure constant** $\alpha = e^2 / 2\epsilon_0 \hbar c = 1/137.036$
- Electron or quark mass/QCD strong interaction scale, $m_{e,q} / \Lambda_{QCD}$
 $\alpha_{strong}(r) = \text{const} / \ln(r \Lambda_{QCD} / \hbar c)$

Variation of strong interaction

Grand unification

$$\frac{\Delta \left(m / \Lambda_{QCD} \right)}{m / \Lambda_{QCD}} = R \frac{\Delta \alpha}{\alpha}$$

1. Proton mass $M_p = 3\Lambda_{QCD}$, measure m_e / M_p

2. Nuclear magnetic moments

$$\mu = g e \hbar / 4M_p c, \quad g = g \left(m_q / \Lambda_{QCD} \right)$$

3. Nuclear energy levels and resonances

Variation of strong interaction

Grand unification (Calmet, Fritzsche; Langecker, Segre, Strasser; Wetterich, Dent)

$$\frac{\Delta(m / \Lambda_{QCD})}{m / \Lambda_{QCD}} \approx 35 \frac{\Delta\alpha}{\alpha}$$

1. Proton mass $M_p \approx 3\Lambda_{QCD}$, measure m_e / M_p

2. Nuclear magnetic moments

$$\mu = g e \hbar / 4M_p c, \quad g = g(m_q / \Lambda_{QCD})$$

3. Nuclear energy levels and resonances

Relation between variations of different coupling constants

Grand unification models Calmet, Fritzsch;
Langecker, Segre, Strasser; Wetterich, Dent

$$\alpha_i^{-1}(\nu) = \alpha_{GUT}^{-1} + b_i \ln(\nu / \nu_0)$$

Variation of GUT const α_{GUT}

$$d\alpha_1^{-1} = d\alpha_2^{-1} = d\alpha_3^{-1} = d\alpha_{GUT}^{-1}$$

$$d\alpha_3 / \alpha_3^2 = d\alpha_1 / \alpha_1^2$$

$$\alpha_3^{-1}(m) = \alpha_{\text{strong}}^{-1}(m) = b_3 \ln(m / \Lambda_{\text{QCD}})$$

$$\alpha^{-1}(m) = 5/3 \alpha_1^{-1}(m) + \alpha_2^{-1}(m)$$

$$\frac{\Delta(m / \Lambda_{\text{QCD}})}{m / \Lambda_{\text{QCD}}} = \frac{1}{b_3 \alpha_3} \frac{\Delta \alpha_3}{\alpha_3} = \frac{\text{const}}{\alpha} \frac{\Delta \alpha}{\alpha} \approx 35 \frac{\Delta \alpha}{\alpha}$$

1. Proton mass $M_p \approx 4\Lambda_{\text{QCD}}$, measure m_e / M_p

2. Nuclear magnetic moments

$$\mu = g e \hbar / 4M_p c, \quad g = g(m_q / \Lambda_{\text{QCD}})$$

3. Nuclear energy levels and resonances

Dependence on quark mass

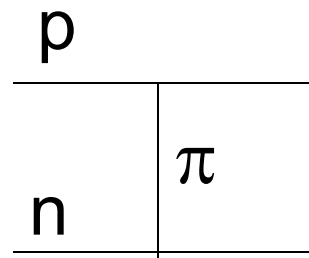
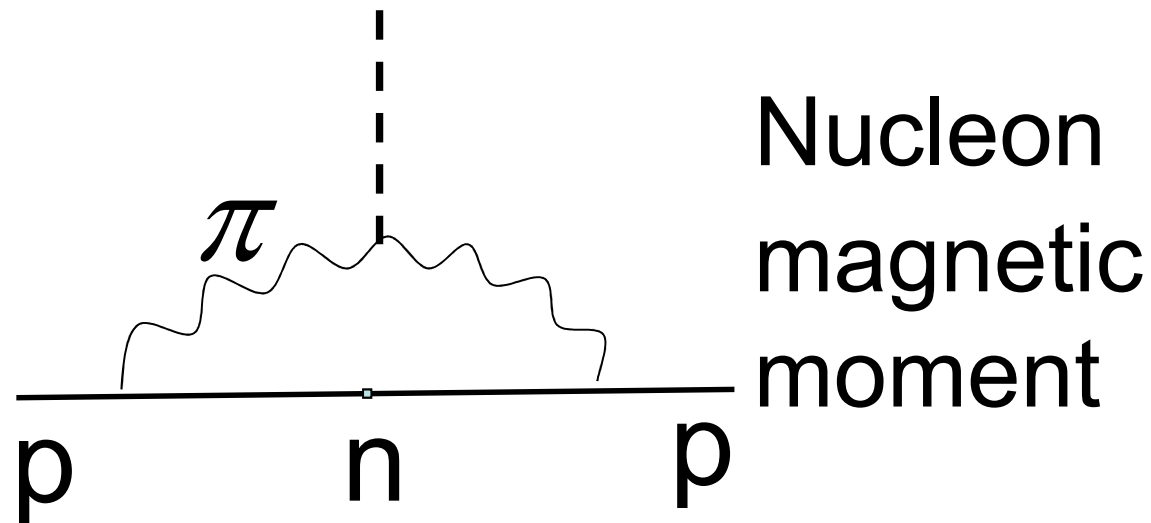
- Dimensionless parameter is m_q/Λ_{QCD} . It is convenient to assume $\Lambda_{\text{QCD}} = \text{const}$, i.e. measure m_q in units of Λ_{QCD}
- m_π is proportional to $(m_q \Lambda_{\text{QCD}})^{1/2}$
 $\Delta m_\pi / m_\pi = 0.5 \Delta m_q / m_q$
- Other meson and nucleon masses remains finite for $m_q = 0$. $\Delta m / m = K \Delta m_q / m_q$

Argonne: K are calculated for $p, n, \rho, \omega, \sigma$.

$$m_q = \frac{m_u + m_d}{2} \approx 4 \text{ MeV}, \quad \Lambda_{\text{QCD}} = 220 \text{ MeV} \rightarrow K = 0.02 - 0.06$$

Strange quark mass $m_s = 120 \text{ MeV}$

Nuclear magnetic moments
depends on π -meson mass m_π



Spin-spin interaction
between valence and
core nucleons

Nucleon magnetic moment

$$\mu = \mu_0 (1 + am_\pi + \dots) = \mu_0 (1 + b\sqrt{m_q} + \dots)$$

Nucleon and meson masses

$$M = M_0 + am_q$$

QCD calculations: lattice, chiral perturbation theory, cloudy bag model, Dyson-Schwinger and Faddeev equations, semiempirical.

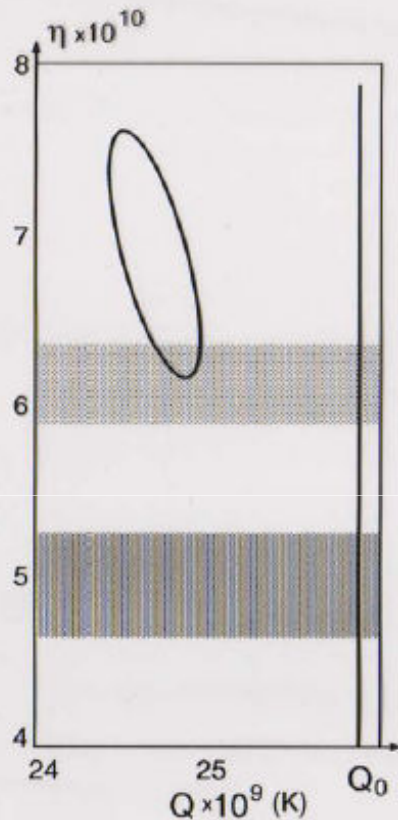
Nuclear calculations: meson exchange theory of strong interaction. Nucleon mass in kinetic energy $p^2/2M$

Big Bang nucleosynthesis: dependence on quark mass

- Flambaum, Shuryak 2002
- Flambaum, Shuryak 2003
- Dmitriev, Flambaum 2003
- Dmitriev, Flambaum, Webb 2004
- Coc, Nunes, Olive, Uzan, Vangioni 2007
- Dent, Stern, Wetterich 2007
- Flambaum, Wirlinga 2007
- Berengut, Dmitriev, Flambaum 2009

Big Bang Nucleosynthesis

(Dmitriev, Flambaum, Webb)



Productions of D, ^4He , ^7Li are exponentially sensitive to deuteron binding energy E_d

$$\sim e^{-\frac{E_d}{T_f}}$$

- η from cosmic microwave background fluctuations (η - barion to photon ratio).

- η from BBN for present value of Q ($Q = |E_d|$)

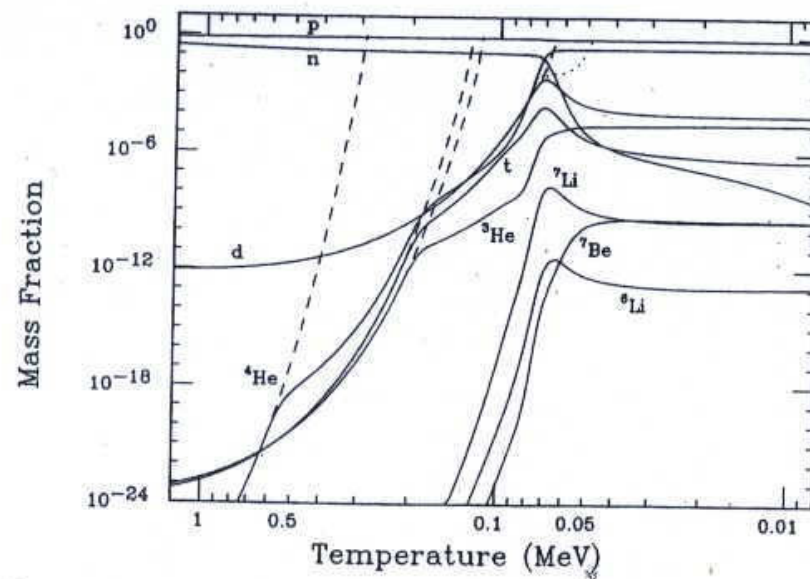


FIG. 2.—Evolution of light-element abundances with temperature, for a baryon-to-photon ratio $\eta_{10} = 3.16$. The dashed curves give the NSE curves of ${}^4\text{He}$, t , ${}^3\text{He}$, and d , respectively. The dotted curve is explained in the text.

Deuterium bottleneck

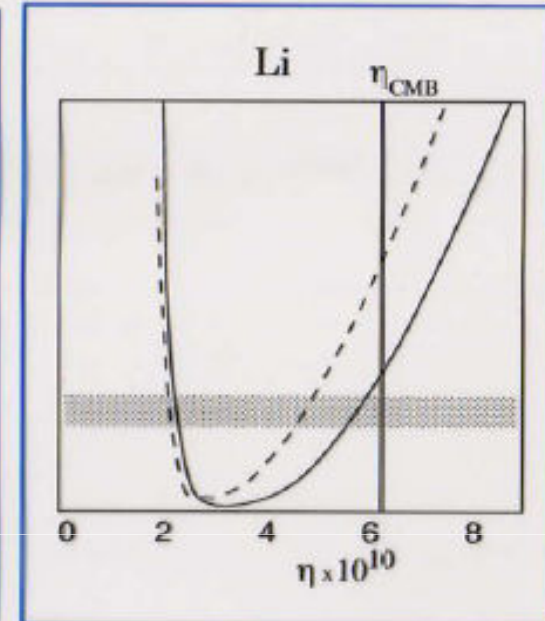
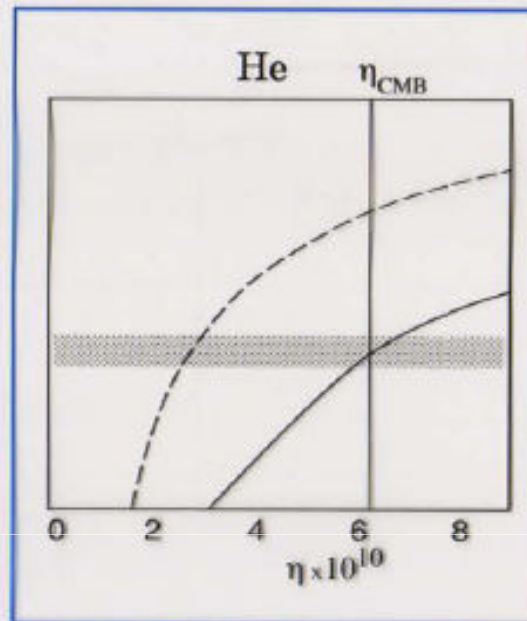
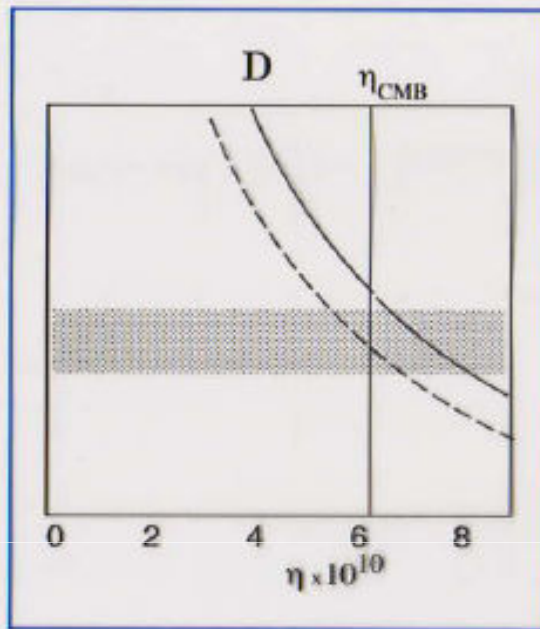
At temperature $T < 0.3 \text{ MeV}$ all abundances follow deutron abundance

(no other nuclei produced if there are no deuterons)

Reaction $\gamma d \rightarrow n p$, exponentially small number of energetic photons, $e^{-(E_d/T)}$

Exponential sensitivity to deutron binding energy E_d , $E_d = 2 \text{ MeV}$,

Freezeout temperature $T_f = 30 \text{ KeV}$



Comparison with observations gives

$$\frac{\delta E_d}{E_d} = -0.019 \pm 0.005$$

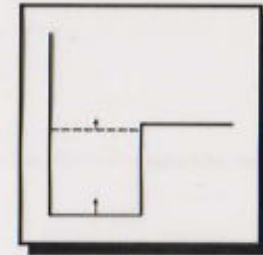
This also leads to agreement

$$\eta(BBN) \approx \eta(CMB)$$

Flambaum, Shuryak: Deuteron Binding Energy is very sensitive to variation of *strange* quark mass (4 factors of enhancement):

1. Deuteron is a shallow bound level.

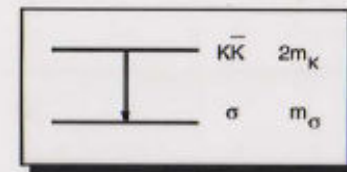
Virtual level in $n + p \rightarrow d + \gamma$ is even more sensitive to the variation of the potential.



2. Strong compensation between σ -meson and ω -meson exchange in potential (Walecka model): $4\pi r V = -g_s^2 e^{-m_\sigma r} + g_v^2 e^{-m_\omega r}$

3. $\sigma = \frac{1}{\sqrt{3}}(u\bar{u} + d\bar{d} + s\bar{s}), \quad m_\sigma \approx 3m_s + 2\Lambda_{QCD}$

4. Repulsion of σ from $K\bar{K}$ threshold



Total $\frac{\delta E_d}{E_d} \approx -17 \frac{\delta m_s}{m_s}$ and $\frac{\delta(m_s/\Lambda_{QCD})}{m_s/\Lambda_{QCD}} = (+1.1 \pm 0.3) \times 10^{-3}$

New BBN result

- Dent, Stern, Wetterich 2007; Berengut, Dmitriev, Flambaum 2009: dependence of BBN on energies of $^2,^3\text{H}$, $^3,^4\text{He}$, $^6,^7\text{Li}$, $^7,^8\text{Be}$
- Flambaum, Wiringa 2007 : dependence of binding energies of $^2,^3\text{H}$, $^3,^4\text{He}$, $^6,^7\text{Li}$, $^7,^8\text{Be}$ on nucleon and meson masses,
- Flambaum, Holl, Jaikumar, Roberts, Write, Maris 2006: dependence of nucleon and meson masses on light quark mass m_q .

Big Bang Nucleosynthesis: Dependence on m_q/Λ_{QCD}

- ^2H $1+7.7x=1.07(15)$ $x=0.009(19)$
- ^4He $1-0.95x=1.005(36)$ $x=-0.005(38)$
- ^7Li $1-50x=0.33(11)$ $x=0.013(02)$

Final result

$$x = \Delta X_q / X_q = 0.013 (02), \quad X_q = m_q / \Lambda_{\text{QCD}}$$

Big Bang Nucleosynthesis:

Dependence on $m_q / \Lambda_{\text{QCD}}$

- ^2H $1+7.7x=1.07(15)$ $x=0.009(19)$
- ^4He $1-0.95x=1.005(36)$ $x=-0.005(38)$
- ^7Li $1-50x=0.33(11)$ $x=0.013(02)$

result

$$x = \Delta X_q / X_q = 0.013 (02), \quad X_q = m_q / \Lambda_{\text{QCD}}$$

Dominated by ^7Li abundance (3 times difference), consistent with $^2\text{H}, ^4\text{He}$

Nonlinear effects: $x = \Delta X_q / X_q = 0.016 (05)$

Atomic transition frequencies

Use atomic calculations to find $\omega(\alpha)$.

For α close to α_0 $\omega = \omega_0 + q(\alpha^2/\alpha_0^2 - 1)$

q is found by varying α in computer codes:

$$q = d\omega/dx = [\omega(0.1) - \omega(-0.1)]/0.2, \quad x = \alpha^2/\alpha_0^2 - 1$$

Many-Multiplet Method
Dzuba, Flambaum, Webb 1998
quasar spectroscopy and atomic clocks

Variation of fine structure constant α

Many-Multiplet Method

Relativistic correction to electron energy E_n :

$$\Delta_n = \frac{E_n}{\nu} (Z\alpha)^2 \left[\frac{1}{j + 1/2} - C(Z, j, l) \right] \quad C \approx 0.6$$

1. Increases with nuclear charge Z .
2. Changes sign for higher angular momentum j .

Methods of Atomic Calculations

N_{ve}	Relativistic Hartree-Fock +	Accuracy
1	All-orders sum of dominating diagrams	0.1-1%
2-6	Configuration Interaction + Many-Body Perturbation Theory	1-10%
2-15	Configuration Interaction	10-20%

These methods cover all periodic system of elements

They were used for many important problems:

- Test of Standard Model using Parity Violation in Cs,Tl,Pb,Bi
- Predicting spectrum of **Fr (accuracy 0.1%)**, etc.

Results of calculations (in cm⁻¹)

Anchor lines

Atom	ω_0	q
Mg I	35051.217	86
Mg II	35760.848	211
Mg II	35669.298	120
Si II	55309.3365	520
Si II	65500.4492	50
Al II	59851.924	270
Al III	53916.540	464
Al III	53682.880	216
Ni II	58493.071	-20

Also, many transitions in Mn II, Ti II, Si IV, C II, C IV, N V, O I, Ca I, Ca II, Ge II, O II, Pb II, Co II, ...

Different signs and magnitudes of q provides opportunity to study systematic errors!

Negative shifters

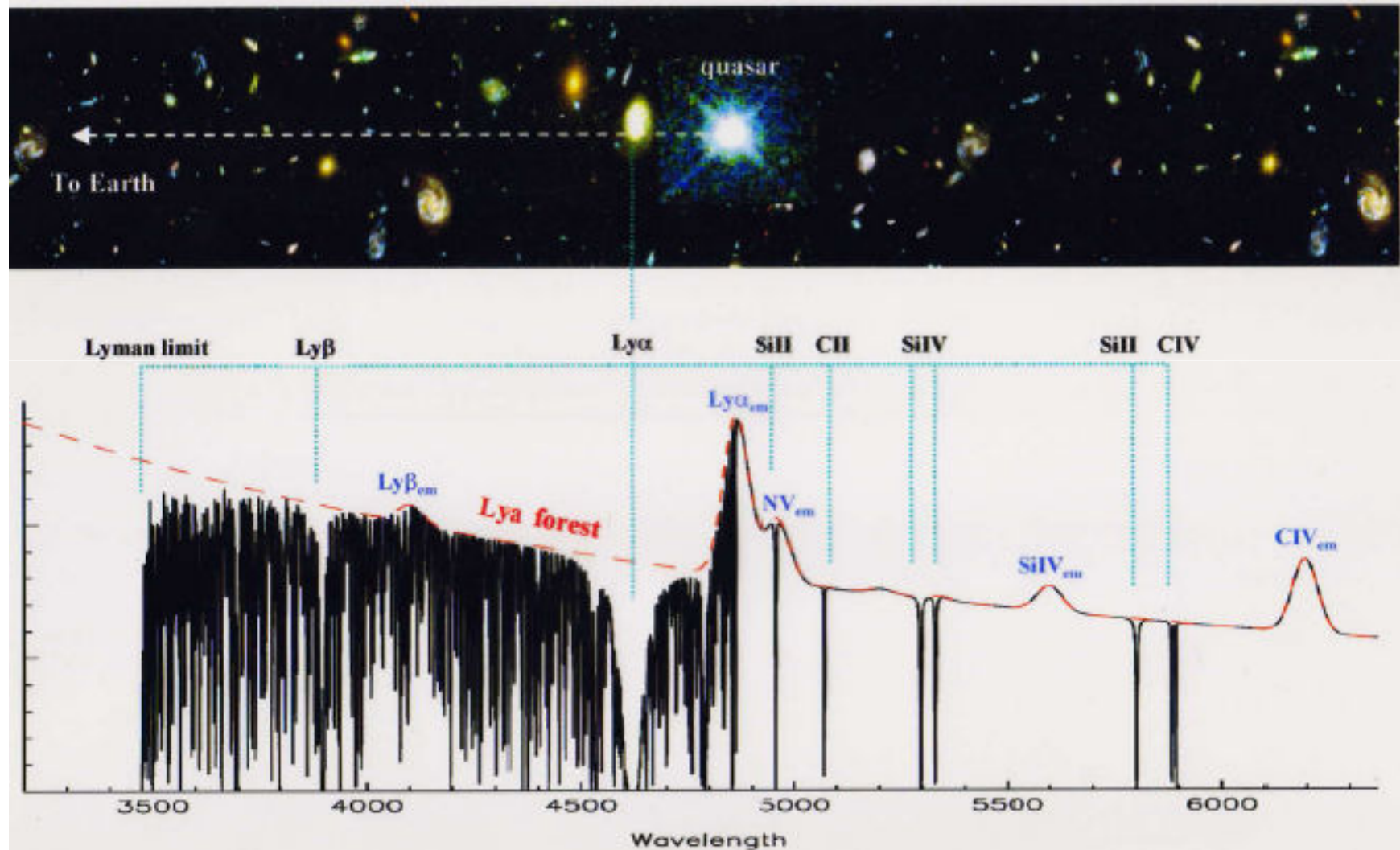
Atom	ω_0	q
Ni II	57420.013	-1400
Ni II	57080.373	-700
Cr II	48632.055	-1110
Cr II	48491.053	-1280
Cr II	48398.862	-1360
Fe II	62171.625	-1300

Positive shifters

Atom	ω_0	q
Fe II	62065.528	1100
Fe II	42658.2404	1210
Fe II	42114.8329	1590
Fe II	41968.0642	1460
Fe II	38660.0494	1490
Fe II	38458.9871	1330
Zn II	49355.002	2490
Zn II	48841.077	1584

4.2 Astrophysical constraints:

Quasars - probing the universe back to much earlier times



Alkali Doublet Method

(Bahcall, Sargent; Varshalovich, Potekhin, Ivanchik, et al)

Fine structure interval

$$\Delta_{FS} = E(p_{3/2}) - E(p_{1/2}) = A(Z\alpha)^2$$

If Δ_z is observed at red shift z and Δ_0 is FS measured on Earth then

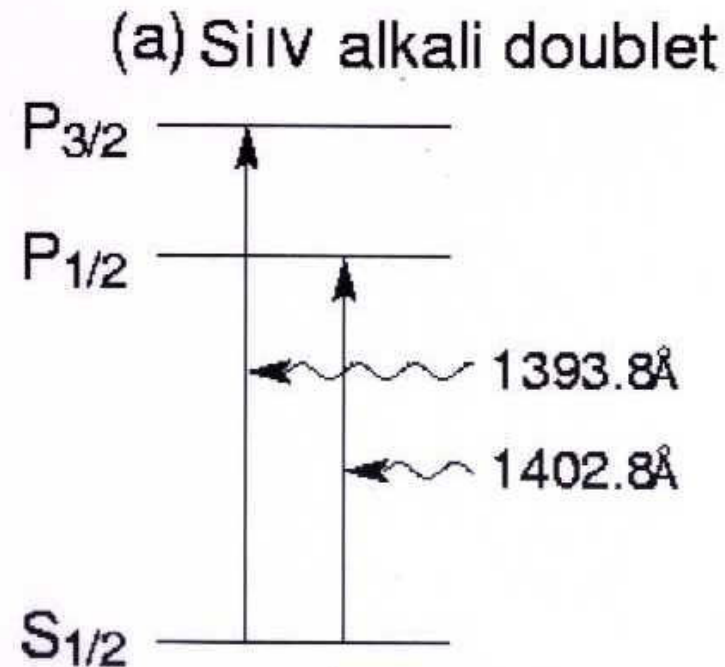
$$\frac{\Delta \alpha}{\alpha} = \frac{1}{2} \left(\frac{\Delta_z}{\Delta_0} - 1 \right)$$

Ivanchik et al, 1999: $\Delta\alpha/\alpha = -3.3(6.5)(8) \times 10^{-5}$.

Murphy et al, 2001: $\Delta\alpha/\alpha = -0.5(1.3) \times 10^{-5}$.

The alkali doublet (AD) method

- The AD method is simple ... but inefficient.
- The common S ground state in ADs has maximal relativistic corrections!



Request for laboratory measurements: shopping list arxiv: physics/0408017

- More accurate measurements of **UV transition frequencies**
- Measurements of **isotope shifts**
Cosmological evolution of isotope abundances in the Universe:
 - a). Systematics for the variation of α
 - b). Test of theories of nuclear reactions in stars and supernovae
- **Oscillator strengths** to fit column densities

A new method

- Relativistic corrections are large when the electron is near the nucleus:

$$\frac{mv^2}{2} - \frac{Ze^2}{r} = E, \text{ so } \frac{v^2}{c^2} \propto \frac{1}{r}$$

- S-electron ($l=0$) has maximal probability to be at small distances

→ maximal relativistic corrections.

However, S- electron has no spin-orbit splitting, $\therefore \vec{L} \cdot \vec{S} = 0$!

- New method - compare spectra of different atoms → more than 10 X increase in sensitivity.

$$\frac{\text{relativistic correction}}{\text{energy of electron}} \approx (Z\alpha)^2 \left[\frac{1}{j+1/2} - C \right] \frac{1}{v}$$

Z - nuclear charge

$j = l + s$ - total electron angular momentum (s - electron $j = 1/2$)

$C \approx 0.6$ - contribution of the many - body effect

v - effective principal quantum number

Variation of fine structure constant α

Many-Multiplet Method

Relativistic correction to electron energy E_n :

$$\Delta_n = \frac{E_n}{\nu} (Z\alpha)^2 \left[\frac{1}{j + 1/2} - C(Z, j, l) \right] \quad C \approx 0.6$$

1. Increases with nuclear charge Z .
2. Changes sign for higher angular momentum j .

Probing the variability of α with QSO absorption lines

Procedure:

1. Compare heavy ($Z \sim 30$) and light ($Z < 10$) atoms, OR
2. Compare $s \rightarrow p$ and $d \rightarrow p$ transitions in heavy atoms.

Shifts can be of opposite sign.

Basic formula:

$$E_z = E_{z=0} + q \left[\left(\frac{\alpha_z}{\alpha_0} \right)^2 - 1 \right]$$

$E_{z=0}$ is the laboratory frequency. 2nd term is non-zero only if α has changed. q is derived from atomic calculations. (Method: frequencies of different lines are computed for different values of α).

Relativistic shift of the central line in the multiplet

$$q = Q + K(L.S)$$

K is the spin-orbit splitting parameter. $Q \sim 10K$

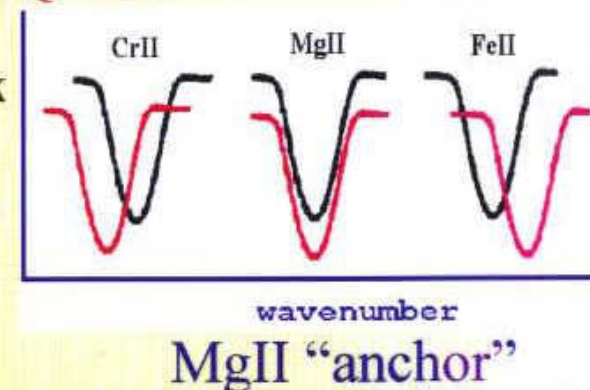
Numerical examples: (units = cm^{-1})

$Z=26$ ($s \rightarrow p$) FeII 2383A: $\omega_0 = 38458.987(2) + 1449x$

$Z=12$ ($s \rightarrow p$) MgII 2796A: $\omega_0 = 35669.298(2) + 120x$

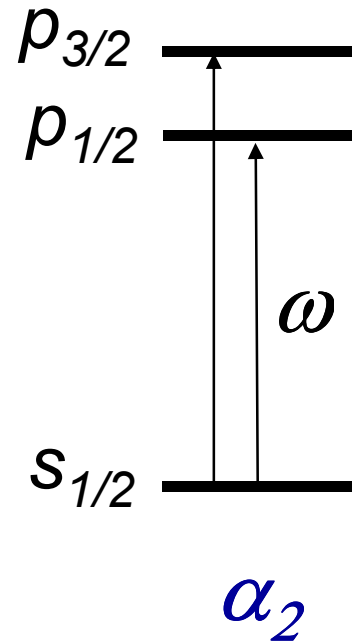
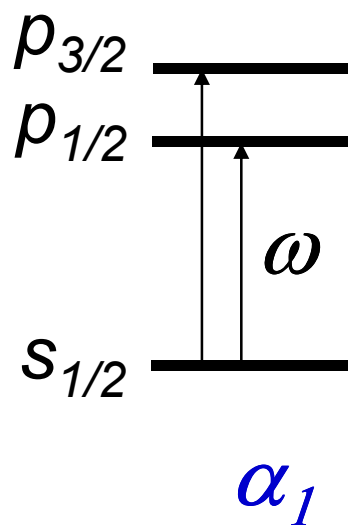
$Z=24$ ($d \rightarrow p$) CrII 2066A: $\omega_0 = 48398.666(2) - 1267x$

$$x = (\alpha_z/\alpha_0)^2 - 1$$



Many Multiplet Method

(Dzuba, Flambaum, Webb)

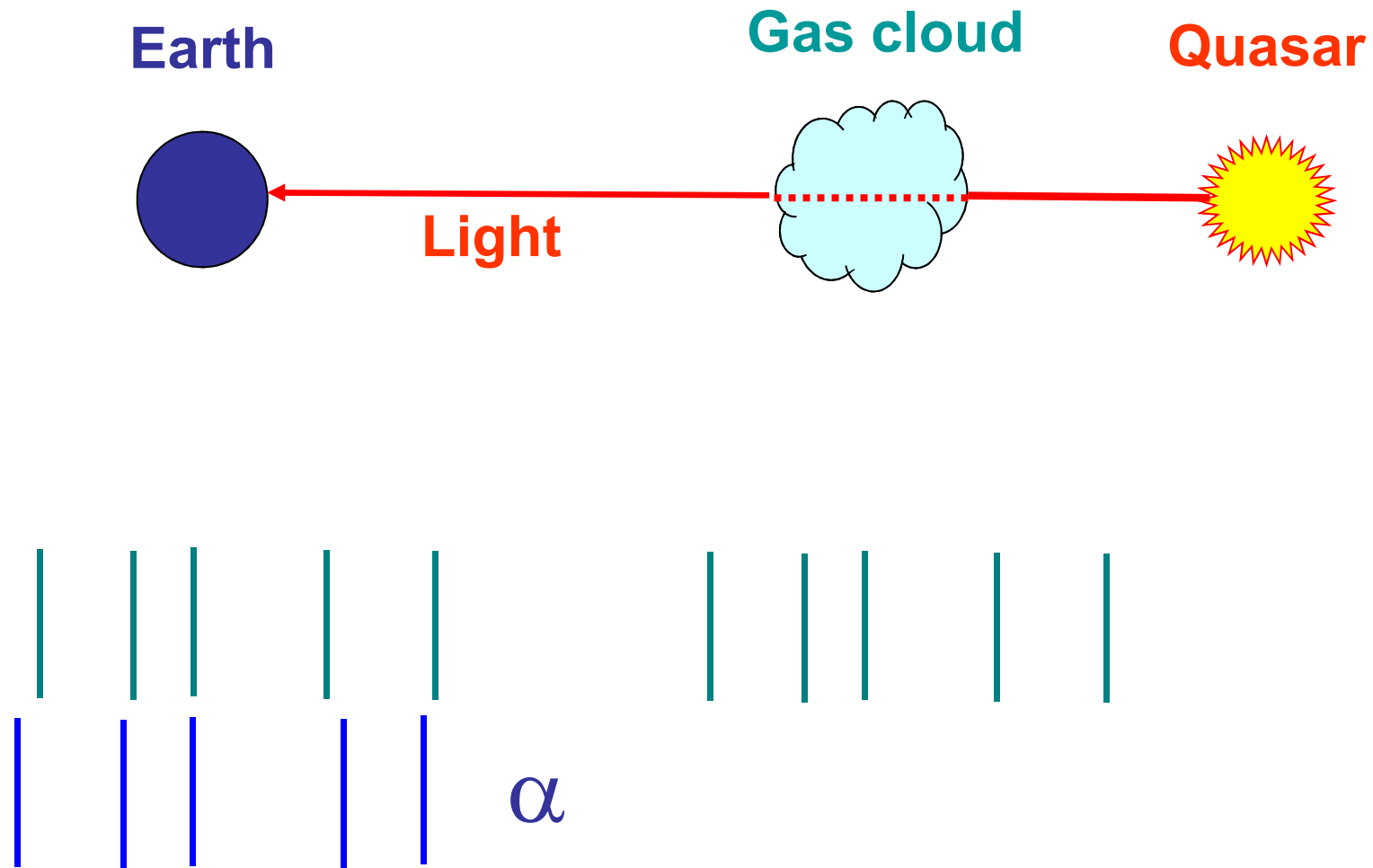


$$\delta\omega \gg \delta\Delta_{FS}!$$

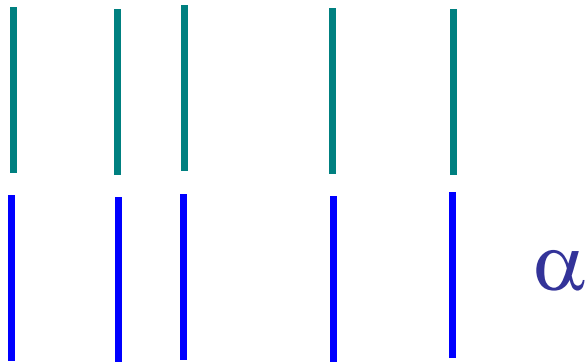
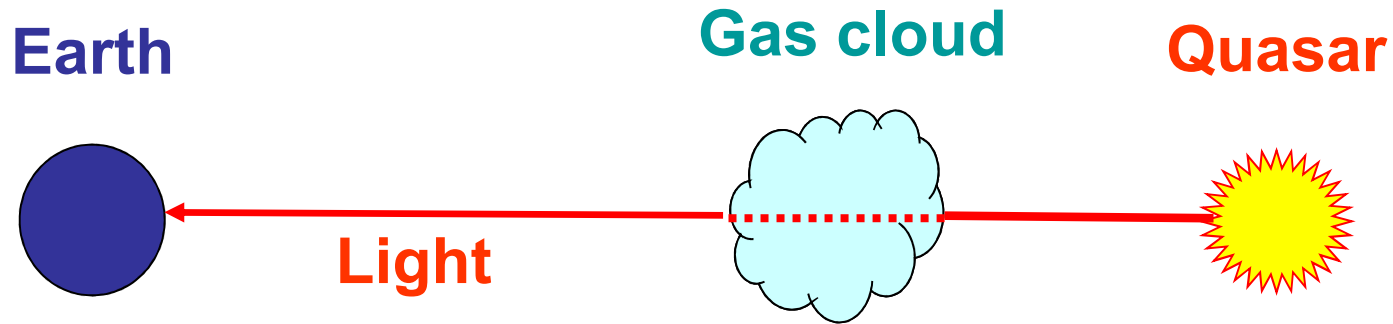
Advantages:

- Order of magnitude gain in sensitivity
- Statistical: all lines are suitable for analysis
- Observe all universe (up to $z=4.2$)
- Many opportunities to study systematic errors

Quasar absorption spectra



Quasar absorption spectra



One needs to know
 $E(\alpha^2)$ for each line to
do the fitting

Use atomic calculations to find $\omega(\alpha)$.

For α close to α_0 $\omega = \omega_0 + q(\alpha^2/\alpha_0^2 - 1)$

q is found by varying α in computer codes:

$$q = d\omega/dx = [\omega(0.1) - \omega(-0.1)]/0.2, \quad x = \alpha^2/\alpha_0^2 - 1$$

$\alpha = e^2/2 \varepsilon_0 \hbar c = 0$ corresponds to non-relativistic limit (infinite c).

Methods were used for many important problems:

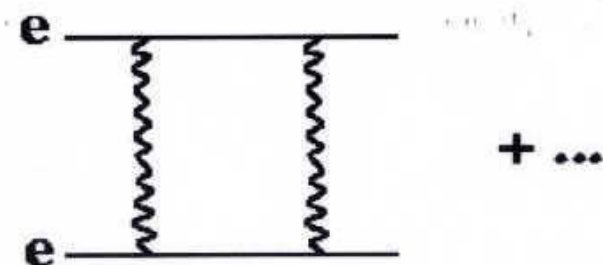
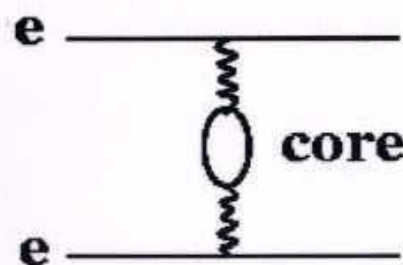
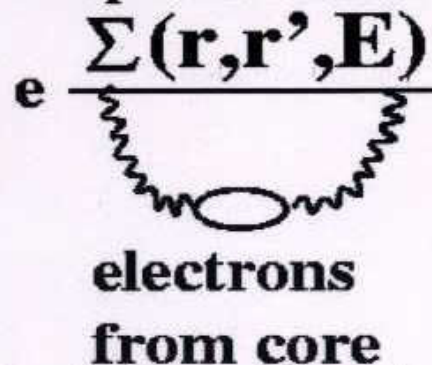
- Test of Standard Model using Parity Violation in Cs,Tl,Pb,Bi
- Predicting spectrum of **Fr (accuracy 0.1%)**, etc.

Probing the variability of α with QSO absorption lines

To find dependence of atomic transition frequencies on α we have performed calculations of atomic transition frequencies for different values of α .

1. Zero Approximation – Relativistic Hartree-Fock method: energies, wave functions, Green's functions

2. Many-body perturbation theory to calculate effective Hamiltonian for valence electrons including self-energy operator and screening; perturbation $\longrightarrow V = H - H_{\text{HF}}$

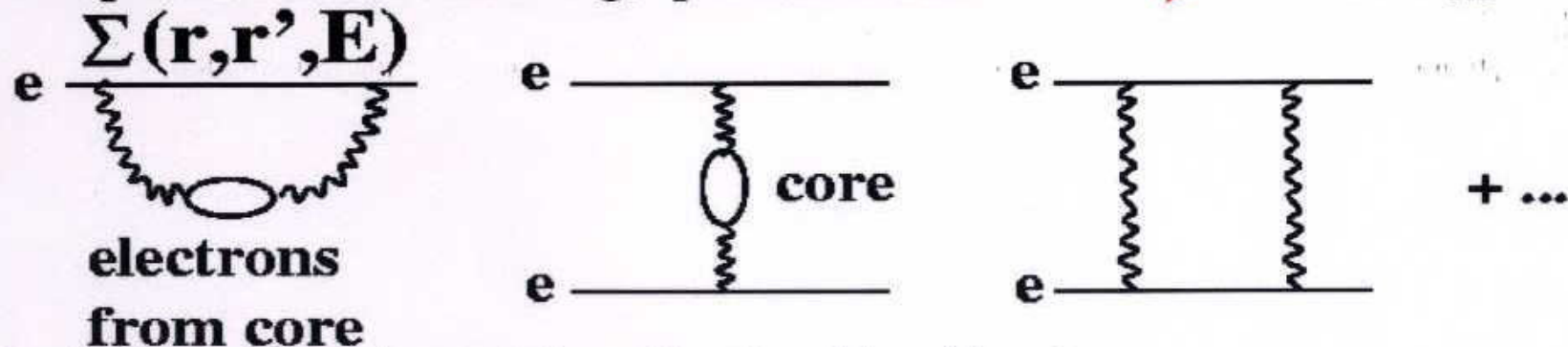


3. Diagonalization of the effective Hamiltonian

Probing the variability of α with QSO absorption lines

To find dependence of atomic transition frequencies on α we have performed calculations of atomic transition frequencies for different values of α .

1. Zero Approximation – Relativistic Hartree-Fock method: energies, wave functions, Green's functions
2. Many-body perturbation theory to calculate effective Hamiltonian for valence electrons including self-energy operator and screening; perturbation $\longrightarrow V = H - H_{\text{HF}}$



3. Diagonalization of the effective Hamiltonian

Test: Energy levels in Mg II to 0.2% accuracy

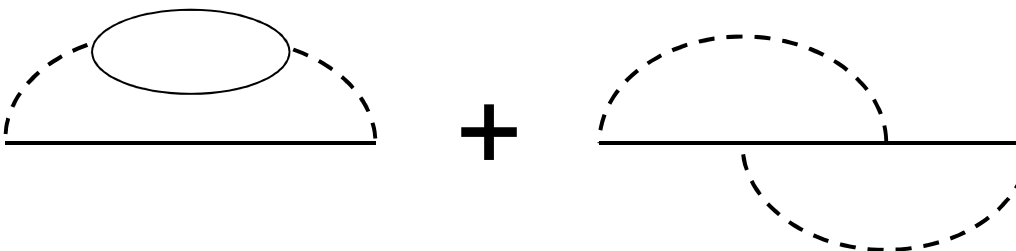
Correlation potential method

[Dzuba, Flambaum, Sushkov (1989)]

- Zeroth-order: relativistic Hartree-Fock. Perturbation theory in difference between exact and Hartree-Fock Hamiltonians.
- Correlation corrections accounted for by inclusion of a “correlation potential” Σ :

$$V_{HF} \rightarrow V_{HF} + \Sigma$$

In the lowest order Σ is given by:

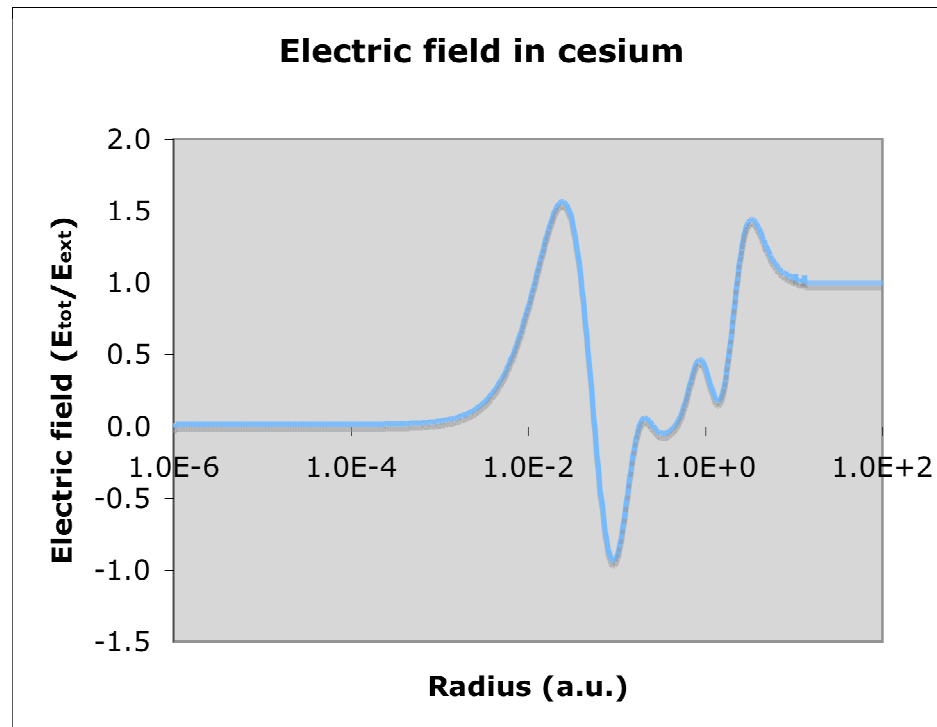
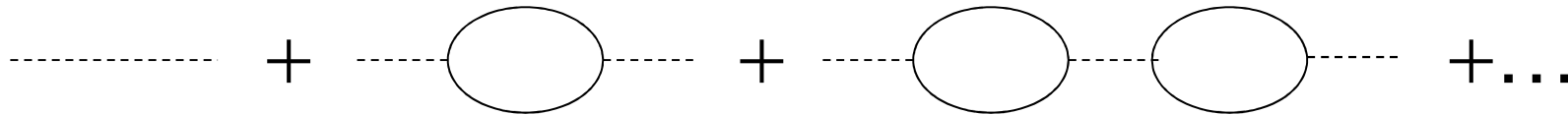
$$\Sigma = \text{diagram 1} + \text{diagram 2}$$


- External fields included using Time-Dependent Hartree-Fock (RPAE core polarization)+correlations

The correlation potential

Use the Feynman diagram technique to include three classes of diagrams to all orders:

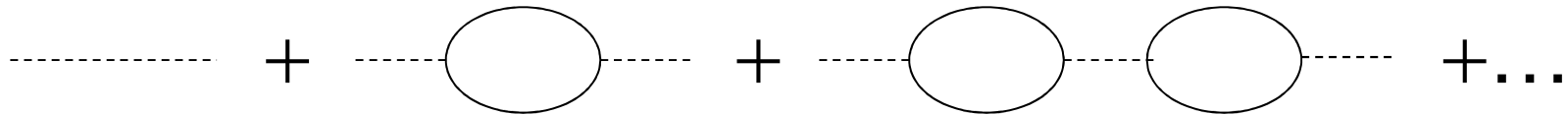
1. electron-electron screening



The correlation potential

Use the Feynman diagram technique to include three classes of diagrams to all orders:

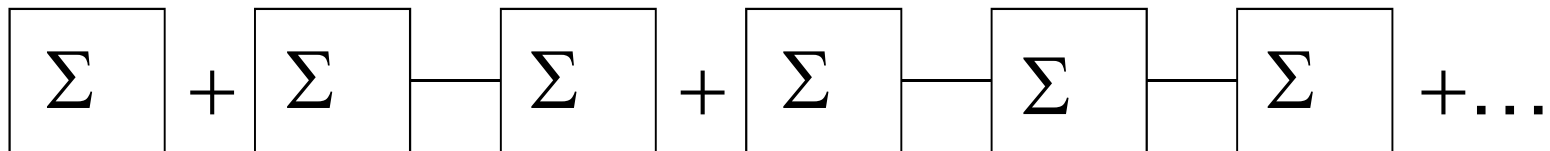
1. electron-electron screening



2. hole-particle interaction



3. nonlinear-in- Σ corrections



Atoms with several valence electrons: CI+MBPT

[Dzuba, Flambaum, Kozlov (1996)]

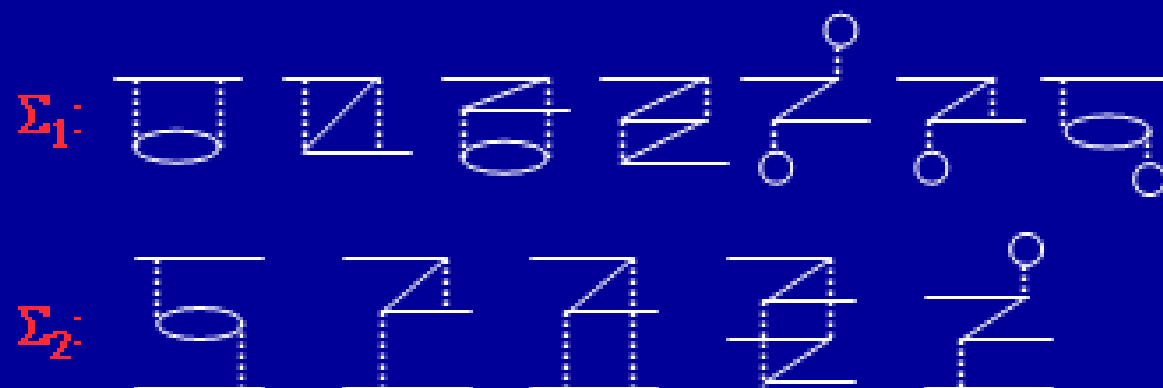
CI Hamiltonian: $\sum_i h_i + \sum_{i,j} e^2/r_{ij}$

$$h = c\alpha p + (\beta - 1)mc^2 - Ze^2/r + V_{\text{core}}$$

CI+MBPT Hamiltonian:

$$h \rightarrow h + \Sigma_1; \quad e^2/r_{ij} \rightarrow e^2/r_{ij} + \Sigma_2$$

MBPT is used to
calculate core-valence
correlation operator $\Sigma(r, r', E)$



Atoms of interest

Z	Atom / Ion	Transitions	N_{ve}^1
6	C I, C II, C III	<i>p-s</i>	4, 3, 2
8	O I	<i>p-s</i>	4
11	Na I	<i>s-p</i>	1
12	Mg I, Mg II	<i>s-p</i>	2, 1
13	Al II, Al III	<i>s-p</i>	2, 1
14	Si II, Si IV	<i>p-s</i>	3, 1
16	S II	<i>s-p</i>	4
20	Ca II	<i>s-p</i>	1
22	Ti II	<i>s-p, d-p</i>	3
24	Cr II	<i>d-p</i>	5
25	Mn II	<i>s-p, d-p</i>	1
26	Fe II	<i>s-p, d-p</i>	7
28	Ni II	<i>d-p</i>	9
30	Zn II	<i>s-p</i>	1

$^1N_{ve}$ – number of valence electrons

Methods of Atomic Calculations

N_{ve}	Relativistic Hartree-Fock +	Accuracy
1	All-orders sum of dominating diagrams	0.1-1%
2-6	Configuration Interaction + Many-Body Perturbation Theory	1-10%
2-15	Configuration Interaction	10-20%

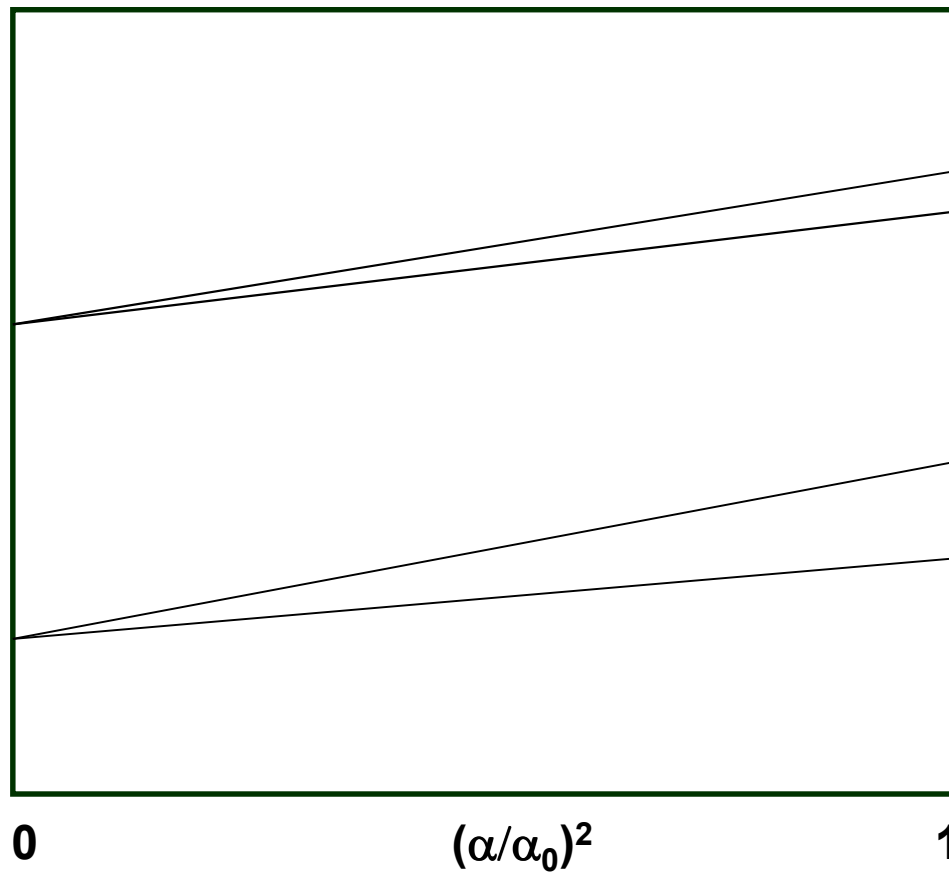
These methods cover all periodic system of elements

They were used for many important problems:

- Test of Standard Model using Parity Violation in Cs,Tl,Pb,Bi
- Predicting spectrum of **Fr (accuracy 0.1%)**, etc.

Relativistic shifts-doublets

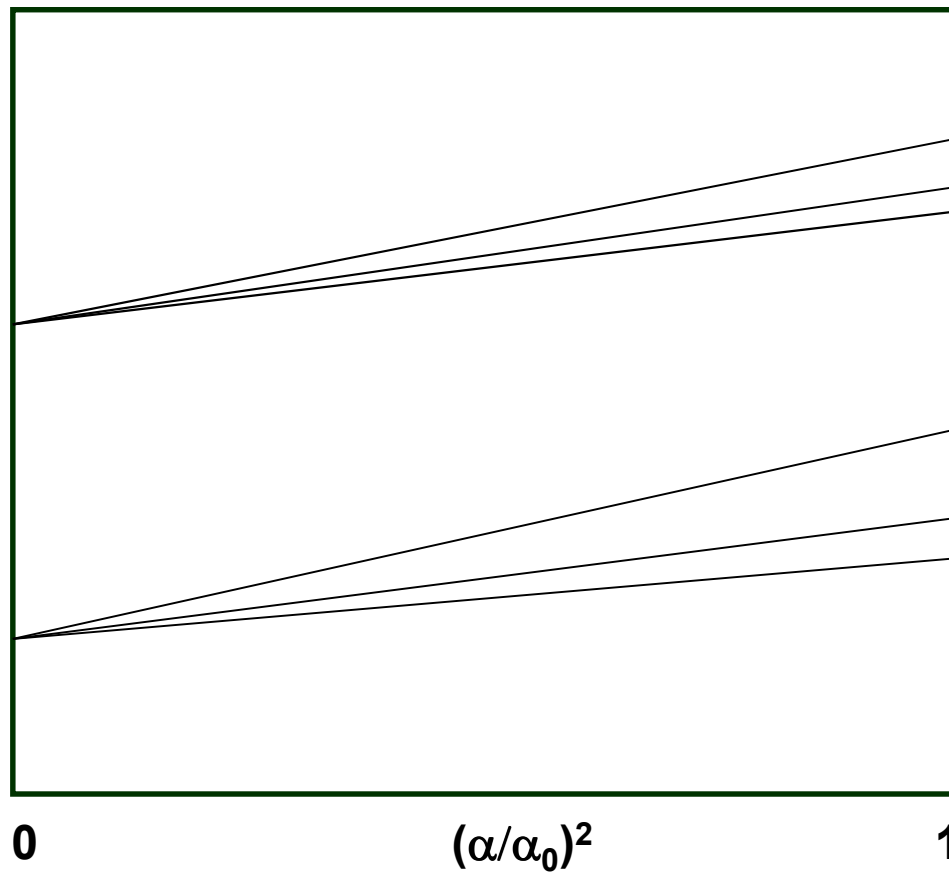
Energies of “normal” fine structure
doublets as functions of α^2



$$\Delta E = A(Z\alpha)^2$$

Relativistic shifts-triplets

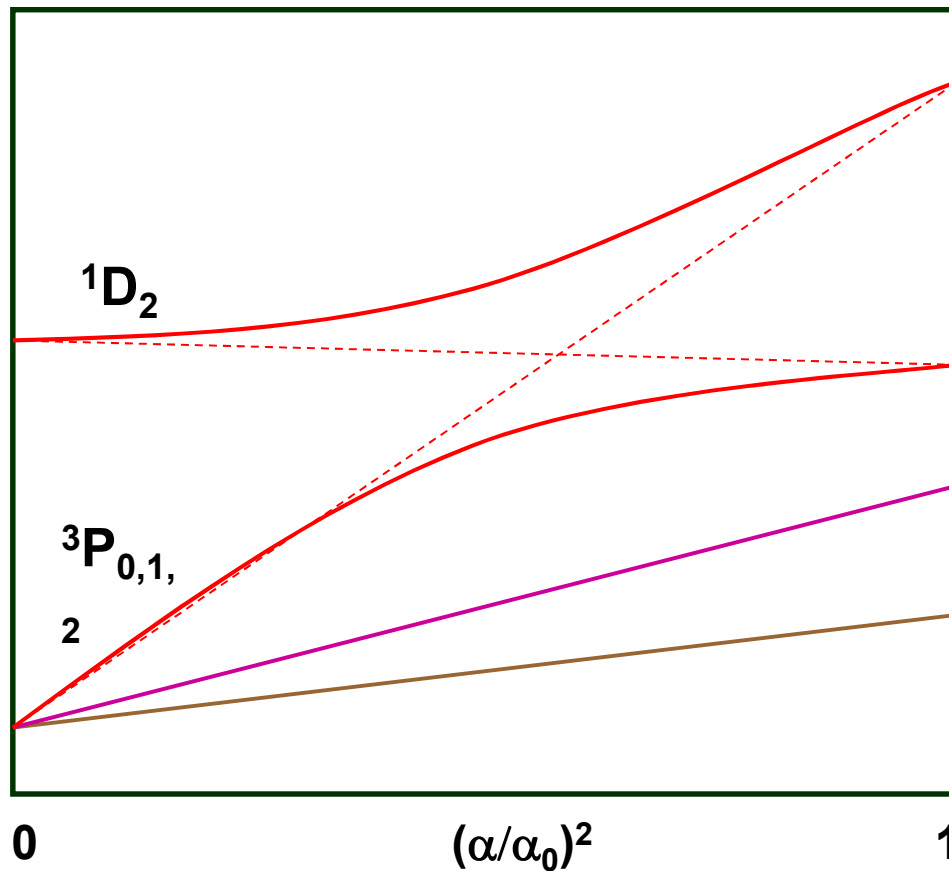
Energies of “normal” fine structure
triplets as functions of α^2



$$\Delta E = A(Z\alpha)^2$$

Fine structure anomalies and level crossing

Energies of strongly interacting states
as functions of α^2



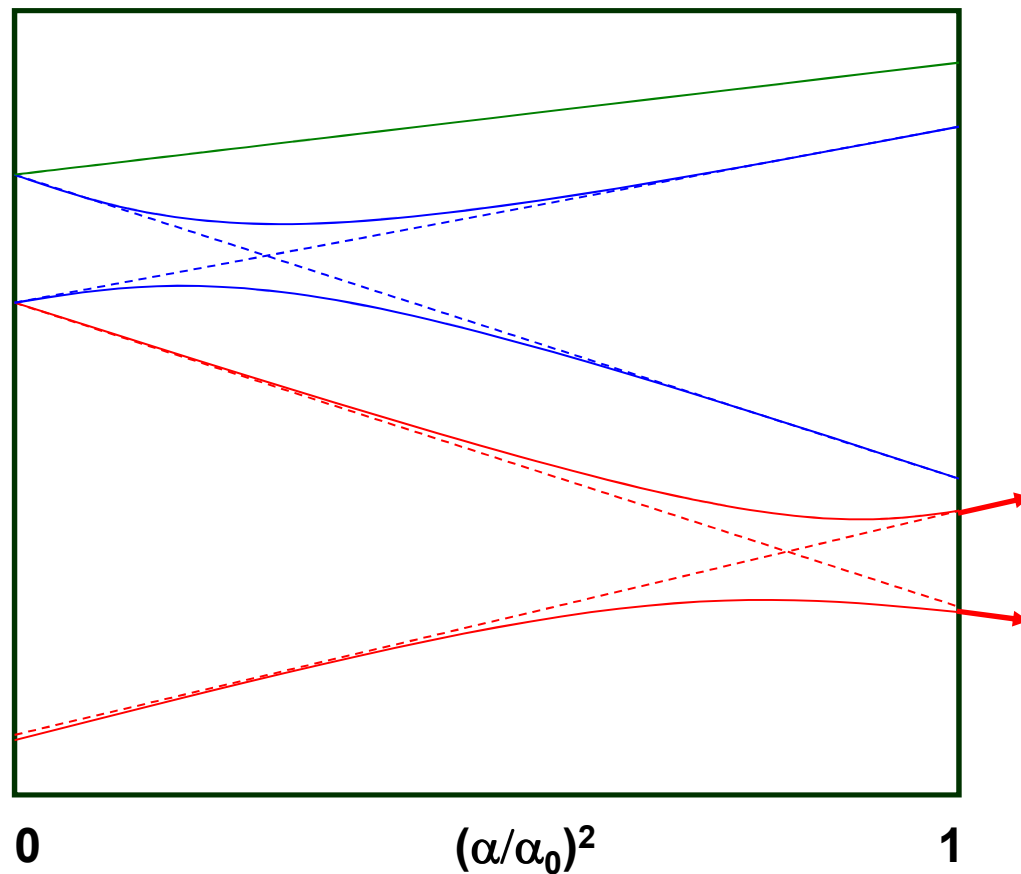
~~$\Delta E = A(Z\alpha)^2$~~

Implications to study of α variation

- Not every energy interval behaves like $\Delta E = A + B(Z\alpha)^2$.
- Strong enhancement is possible (good!).
- Level crossing may lead to instability of calculations (bad!).

Problem: level pseudo crossing

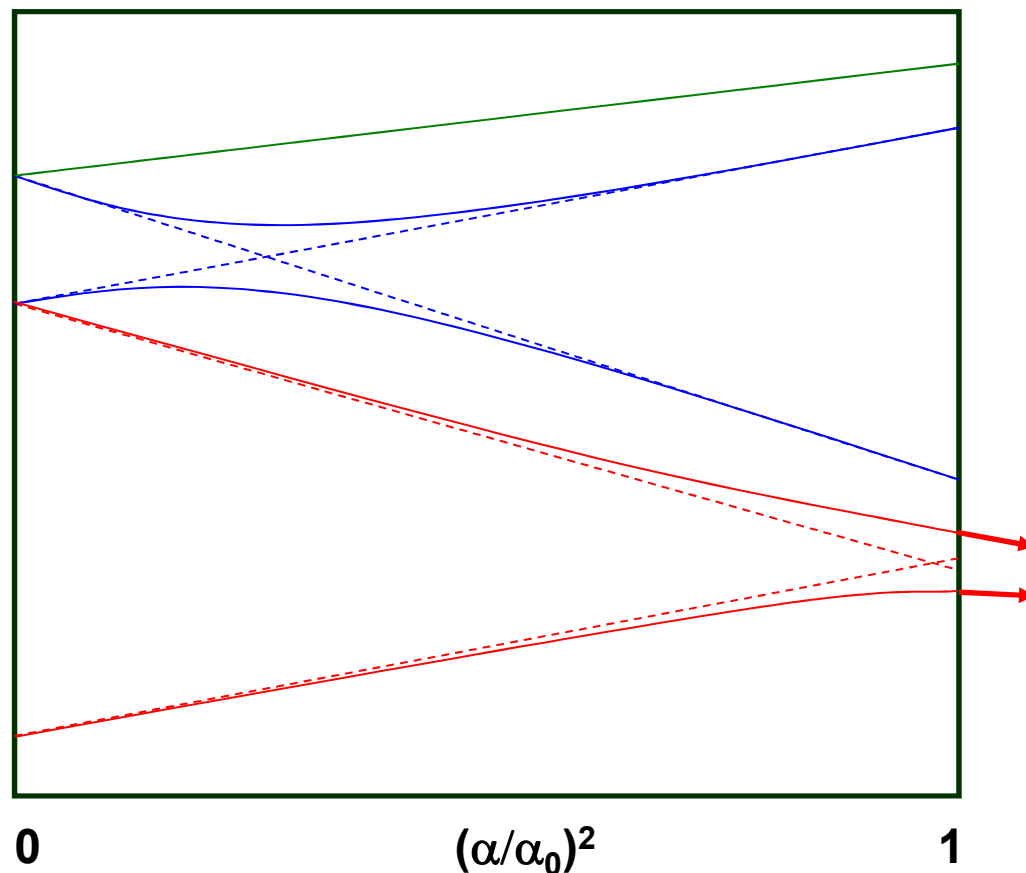
Energy levels of Ni II as functions of α^2



Values of $q = dE/d\alpha^2$
are sensitive to
the position of
level crossing

Problem: level pseudo crossing

Energy levels of Ni II as functions of α^2



Values of $q = dE/d\alpha^2$
are sensitive to
the position of
level crossing

Solution:
matching
experimental g -
factors

hyperfine= $\alpha^2 g_p m_e / M_p$ atomic units

Rotation= m_e/M_p atomic units

Variation in the fine structure constant?: Recent results and the future

Radio constraints:

- Hydrogen hyperfine transition at $\lambda_H = 21\text{cm}$.
- Molecular rotational transitions CO, HCO⁺, HCN, HNC, CN, CS ...
- $\omega_H/\omega_M \propto \alpha^2 g_p$ where g_p is the proton magnetic g -factor.

$$g_p = g_p \left(\frac{m_p}{\Lambda_{QCD}} \right)$$

Procedure:

1. Compare heavy ($Z \sim 30$) and light ($Z < 10$) atoms, OR
2. Compare $s \rightarrow p$ and $d \rightarrow p$ transitions in heavy atoms.

Shifts can be of opposite sign.

Basic formula:

$$E_z = E_{z=0} + q \left[\left(\frac{\alpha_z}{\alpha_0} \right)^2 - 1 \right]$$

$E_{z=0}$ is the laboratory frequency. 2nd term is non-zero only if α has changed. q is derived from atomic calculations. (Method: frequencies of different lines are computed for different values of α).

Relativistic shift of the central line in the multiplet

$$q = Q + K(L.S)$$

K is the spin-orbit splitting parameter. $Q \sim 10K$

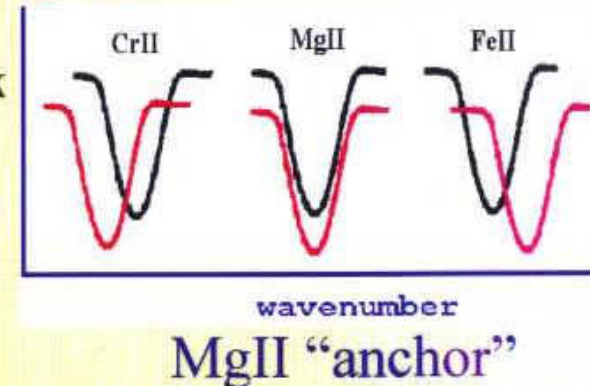
Numerical examples: (units = cm^{-1})

$$Z=26 (s \rightarrow p) \quad \text{FeII } 2383\text{\AA}: \omega_0 = 38458.987(2) + 1449x$$

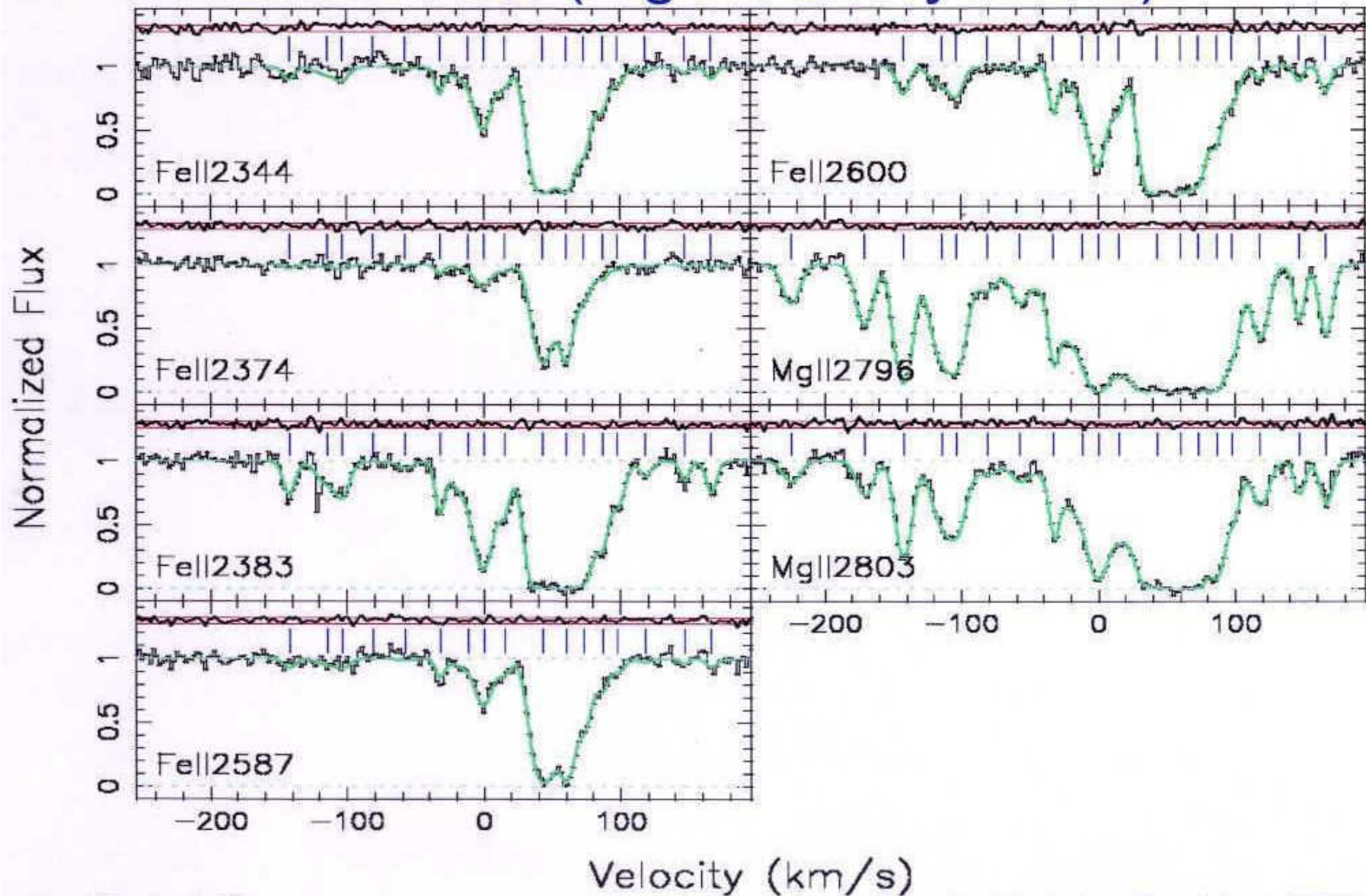
$$Z=12 (s \rightarrow p) \quad \text{MgII } 2796\text{\AA}: \omega_0 = 35669.298(2) + 120x$$

$$Z=24 (d \rightarrow p) \quad \text{CrII } 2066\text{\AA}: \omega_0 = 48398.666(2) - 1267x$$

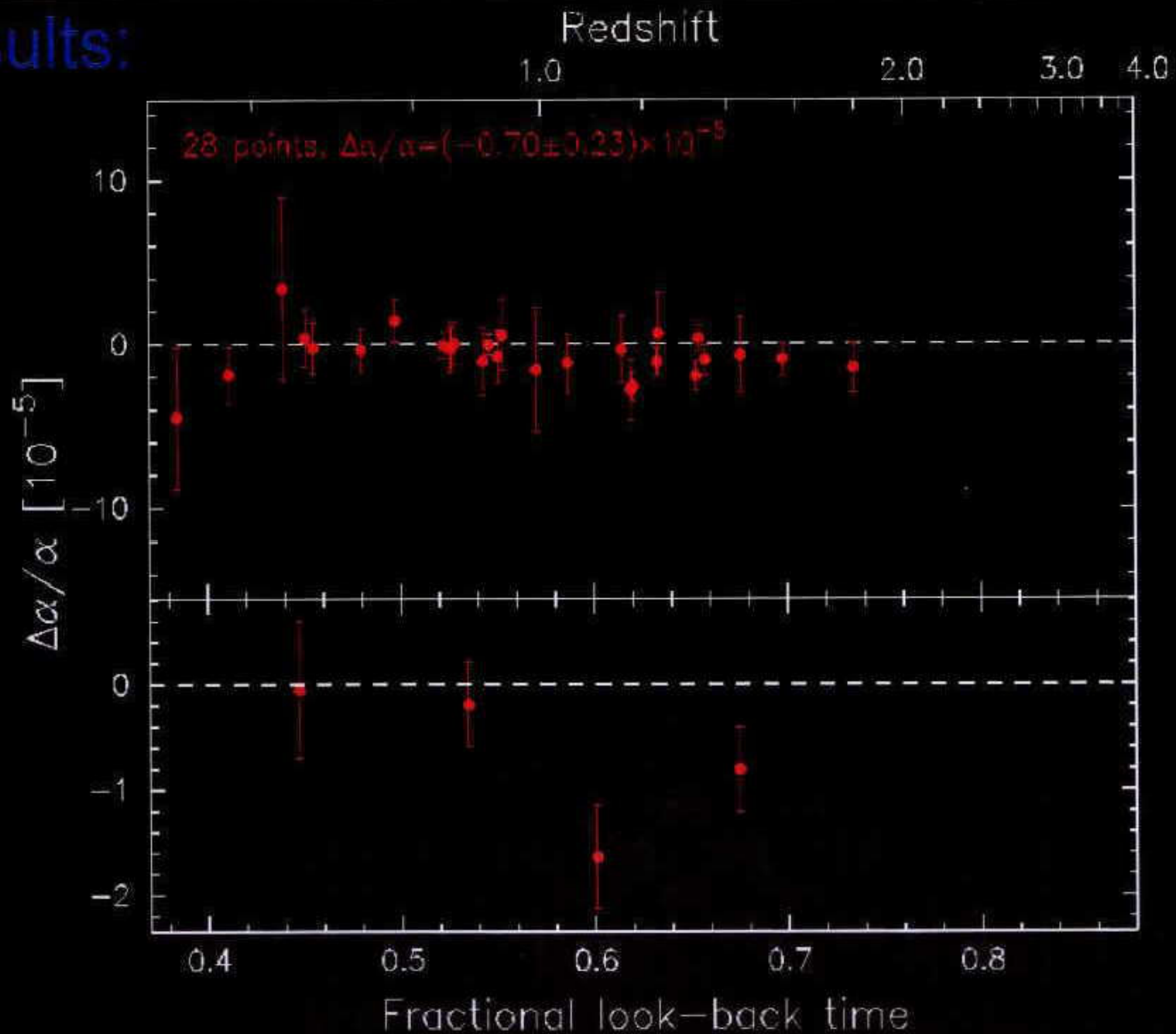
$$x = (\alpha_z/\alpha_0)^2 - 1$$



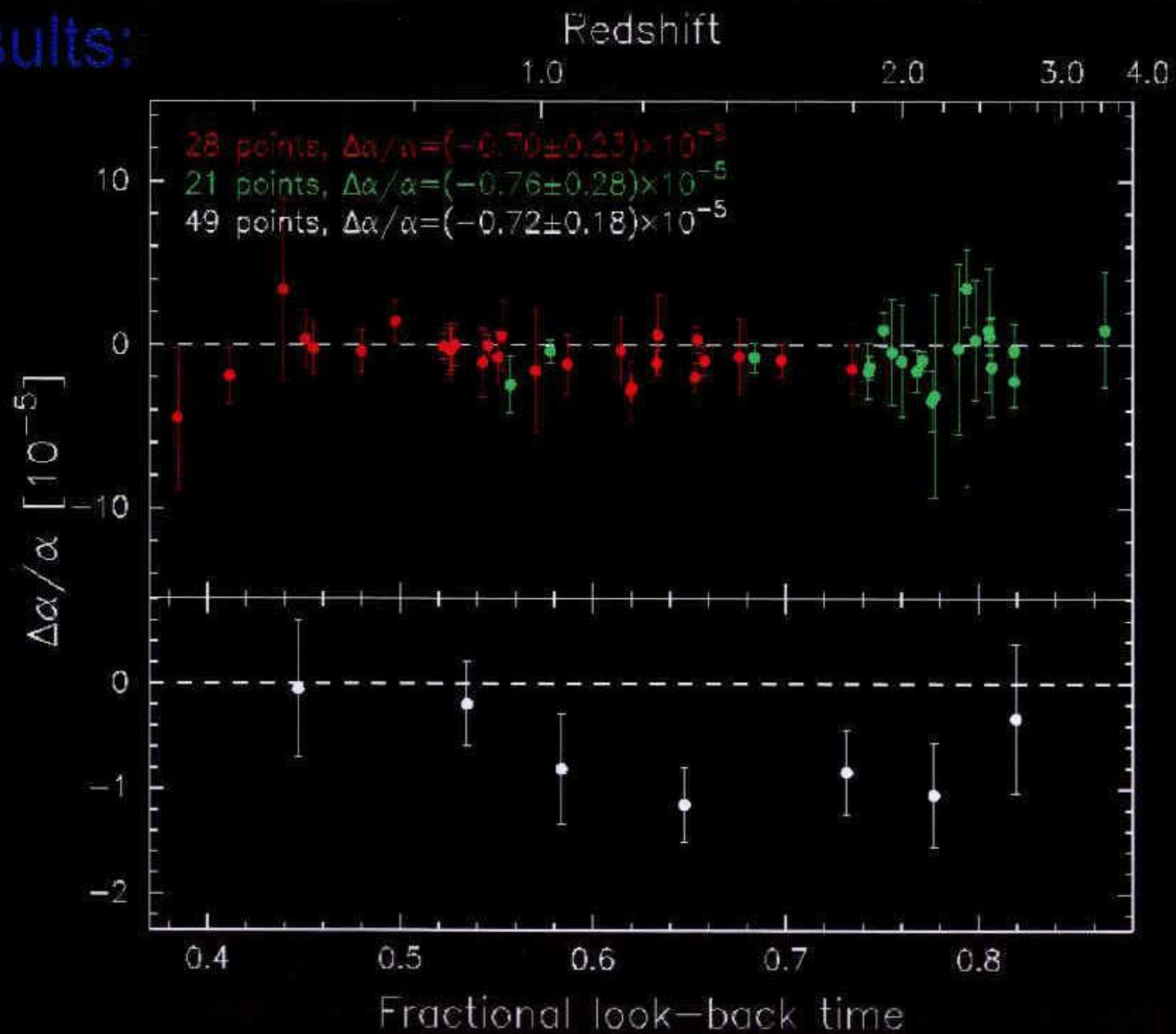
Low-redshift data (Mg II/Fe II systems):

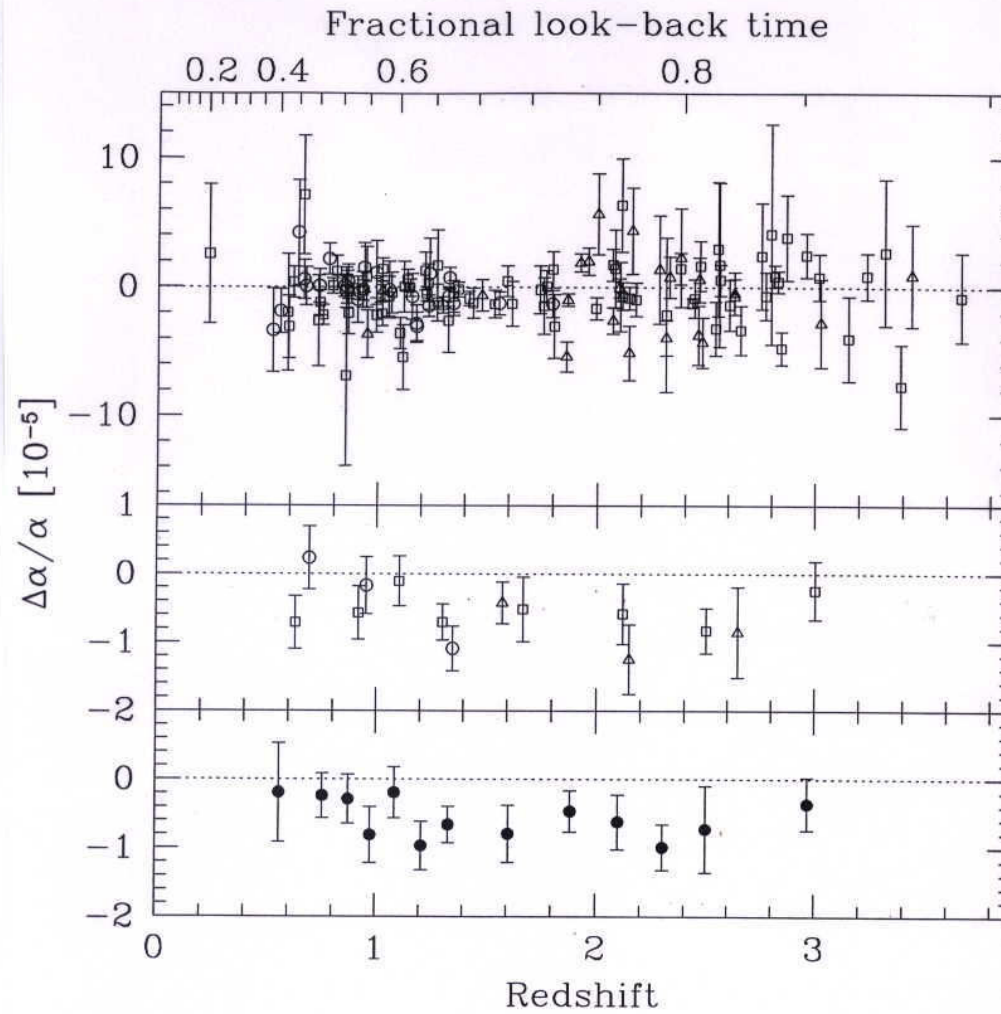


Results:



Results:

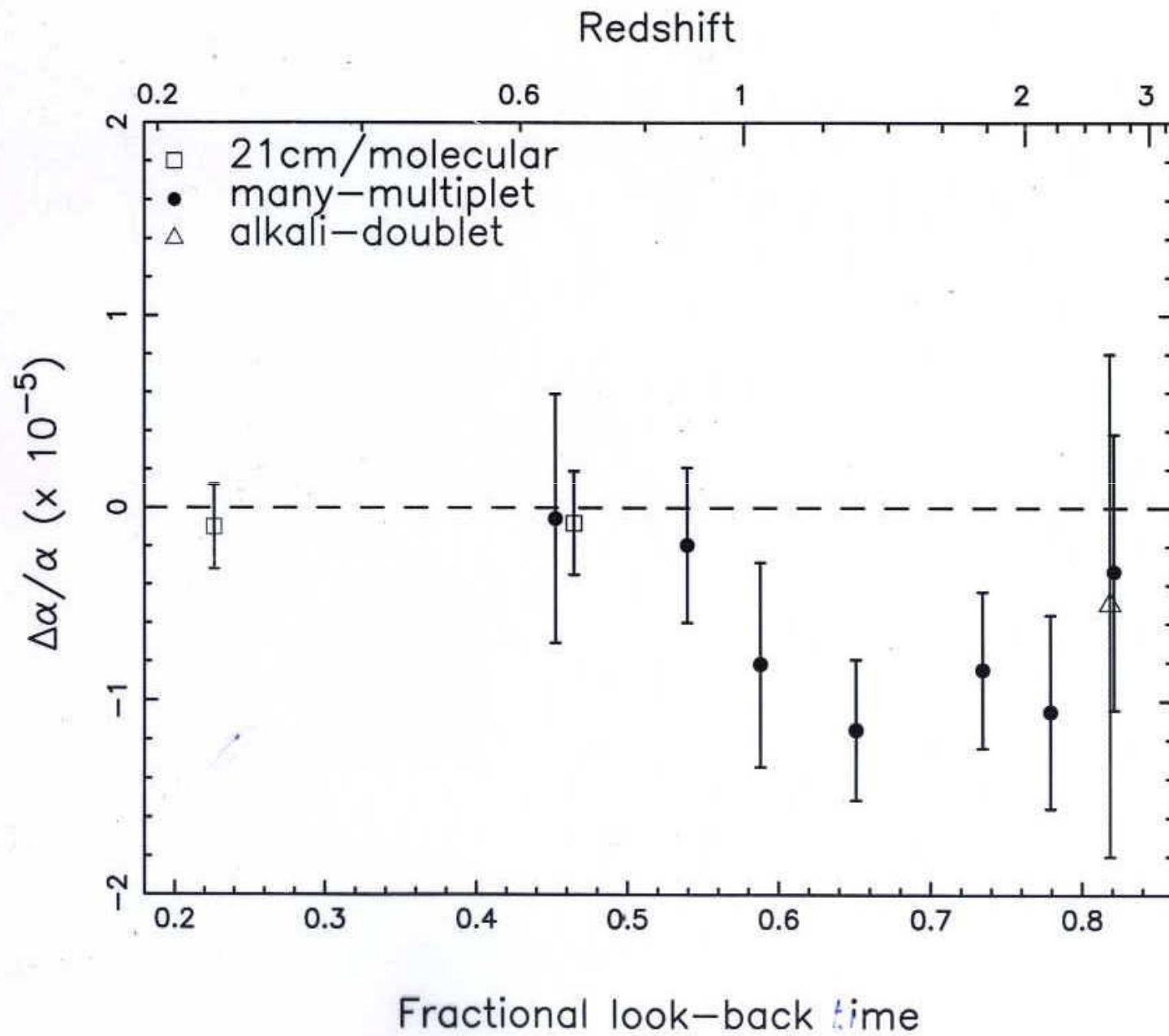




$$\frac{\Delta\alpha}{\alpha} = (-0.574 \pm 0.102) \cdot 10^{-5}$$

5.62 σ from $\Delta\alpha=0$

fudicial result $(-0.543 \pm 0.116) \cdot 10^{-5}$ 4.7 σ



- Murphy et al, 2003: **Keck telescope**, 143 systems, 23 lines, $0.2 < z < 4.2$

$$\Delta\alpha/\alpha = -0.54(0.12) \times 10^{-5}$$

- Quast et al, 2004: **VL telescope**, 1 system, Fe II, 6 lines, 5 positive q -s, one negative q , $z=1.15$

$$\Delta\alpha/\alpha = -0.4(1.9)(2.7) \times 10^{-6}$$

Molaro et al 2007 $-0.12(1.8) \times 10^{-6}$, $z=1.84$ $5.7(2.7) \times 10^{-6}$

- Srianand et al, 2004: **VL telescope**, 23 systems, 12 lines, Fe II, Mg I, Si II, Al II, $0.4 < z < 2.3$

$$\Delta\alpha/\alpha = -0.06(0.06) \times 10^{-5}$$

Murphy et al 2007 $\Delta\alpha/\alpha = -0.64(0.36) \times 10^{-5}$
Further revision may be necessary.

Potential systematic effects:

- **Laboratory wavelength errors:** New, mutually consistent laboratory spectra from Imperial College, Lund University and NIST
- **Data quality variations:** Can only produce systematic shifts if combined with laboratory wavelength errors
- **Heliocentric velocity variation:** Smearing in velocity space is degenerate with fitted redshift parameters
- **Isotopic ratio shifts:** Very small effect possible if evolution of isotopic ratios allowed
- **Hyperfine structure shifts:** same as for isotopic shifts
- **Magnetic fields:** Large scale fields could introduce correlations in $\Delta\alpha/\alpha$ for neighbouring QSO site lines (if QSO light is polarised) - extremely unlikely and huge fields required
- **Wavelength miscalibration:** mis-identification of ThAr lines or poor polynomial fits could lead to systematic miscalibration of wavelength scale
- **Temperature changes during observations:** Refractive index changes between ThAr and QSO exposures – random error
- **Line blending:** Are there ionic species in the clouds with transitions close to those we used to find $\Delta\alpha/\alpha$?
- **Atmospheric refraction effects:** Different angles through optics for blue and red light – can only produce positive $\Delta\alpha/\alpha$ at low redshift
- **Instrumental profile variations:** Intrinsic IP variations along spectral direction of CCD?

Possible systematic effect:
isotopic ratio evolution.



Different isotope abundances
→ shift of line.

We calculated isotopic shifts for
 Hg II , $\text{Si II (p} \rightarrow \text{s)}$, Si IV , Zn II . However,
calculations are too complicated
for open d-shell atoms Cr II , Fe II , Ni II ,
(also $\text{Si II s}^2\text{p} \rightarrow \text{sp}^2$) - in progress.

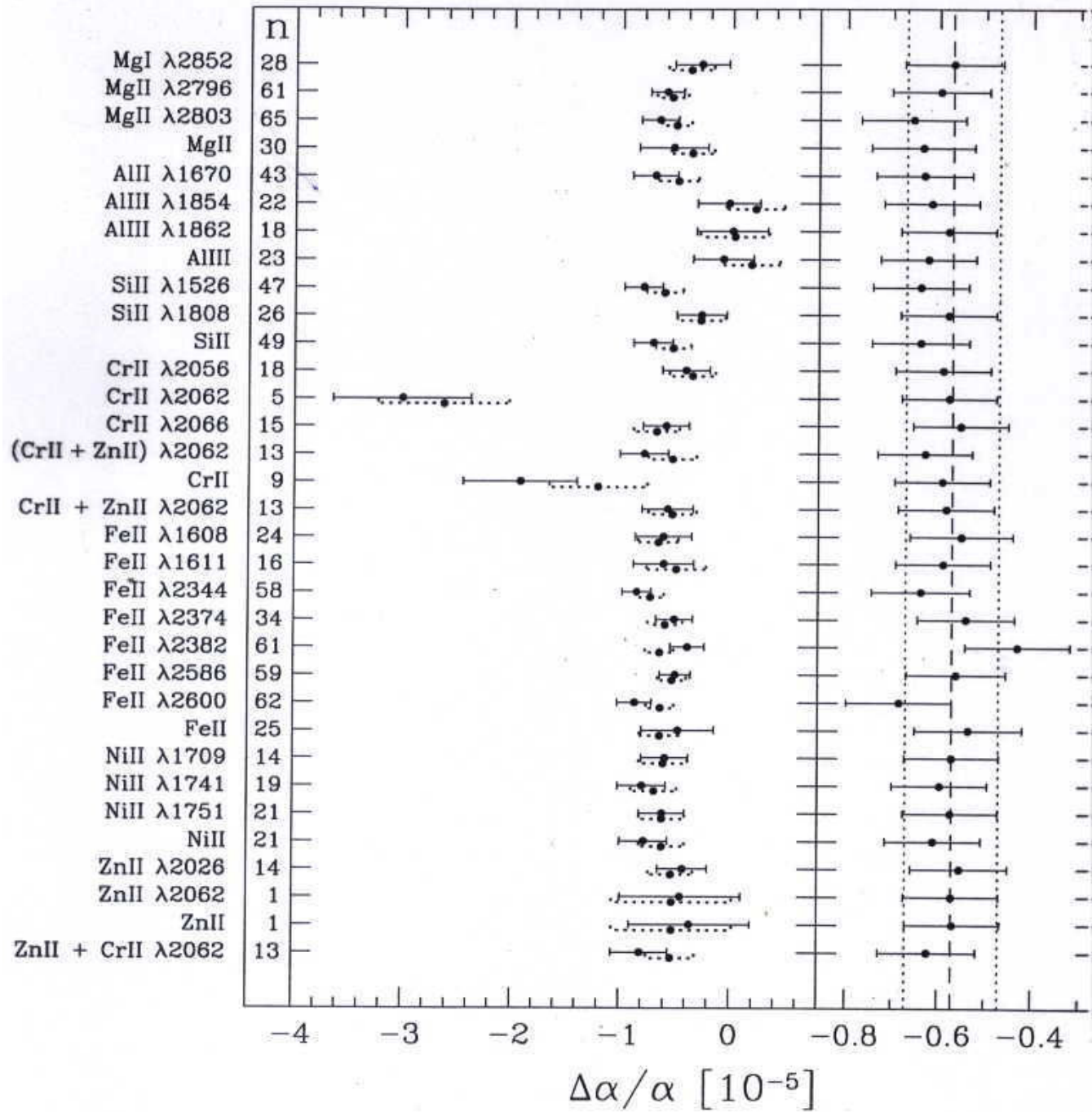
Measure, please!!!

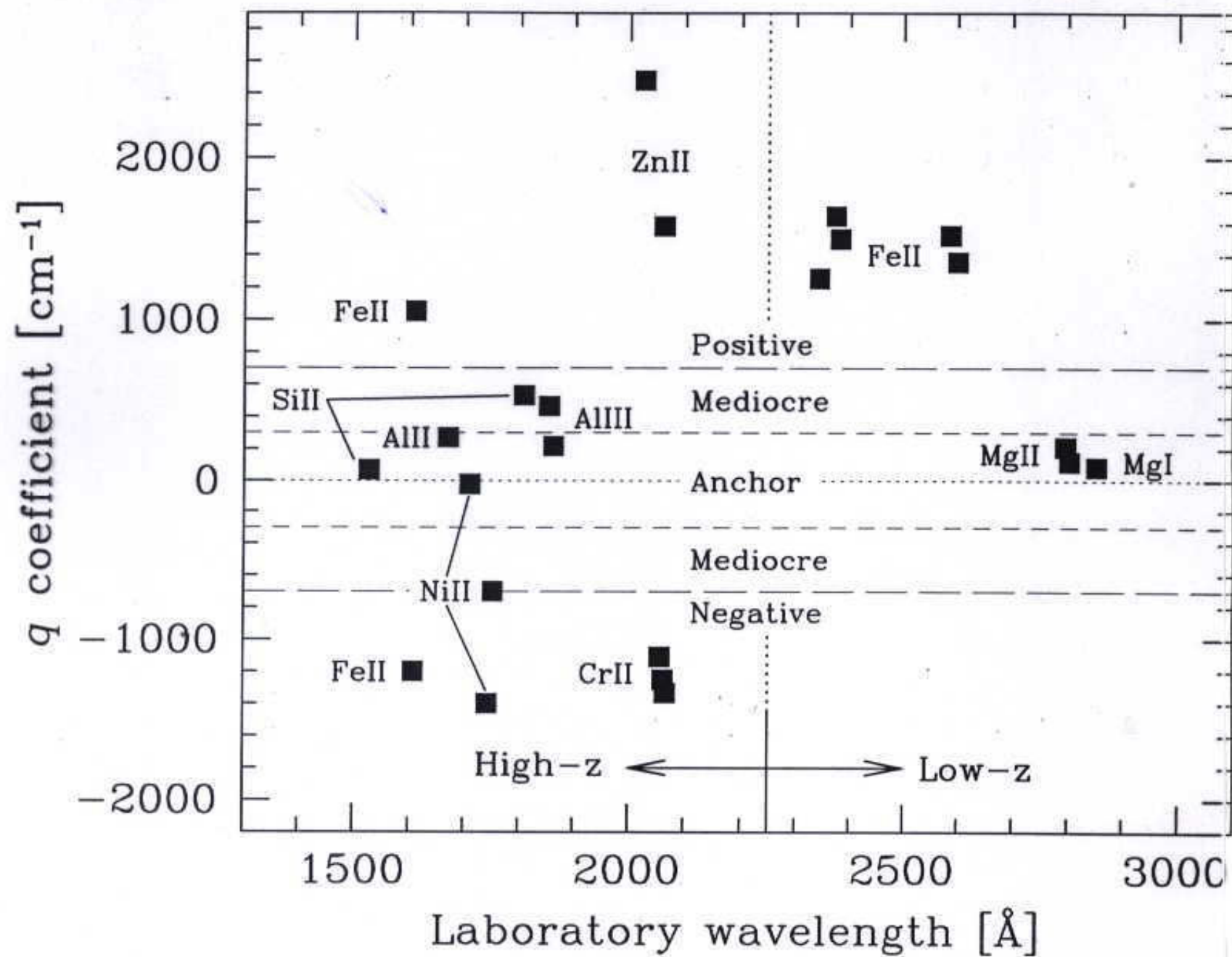
"Conspiracy" of isotopic shifts and
isotopic abundances?

Line removal test.

Checks on general, unknown systematics:

- **Line removal:** In each system, remove each transition and iterate to find $\Delta\alpha/\alpha$ again. Compare the $\Delta\alpha/\alpha$'s before and after line removal. We have done this for all species and see no inconsistencies. **Tests for:** Lab wavelength errors, line blending, isotopic ratio and hyperfine structure variation.
- **Positive-negative shifter test:** Find the subset of systems that contain an anchor line, a positive shifter AND a negative shifter. Remove each type of line collectively and recalculate $\Delta\alpha/\alpha$.
 - Results:** subset contains 12 systems (only in high z sample)
 - No lines removed:** $\Delta\alpha/\alpha = (-1.31 \pm 0.39) \times 10^{-5}$
 - Anchors removed:** $\Delta\alpha/\alpha = (-1.49 \pm 0.44) \times 10^{-5}$
 - +ve-shifters removed:** $\Delta\alpha/\alpha = (-1.54 \pm 1.03) \times 10^{-5}$
 - ve-shifters removed:** $\Delta\alpha/\alpha = (-1.41 \pm 0.65) \times 10^{-5}$





Two sets of line pairs

1. $\delta\alpha < 0$ imitated by compression of the spectrum
2. $\delta\alpha < 0$ imitated by expansion of the spectrum

Both sets give $\delta\alpha < 0$!

New interpretation: **Spatial variation**

Northern+(new)Southern hemisphere data: Linear variation with distance along some direction, $\alpha(x)=\alpha(0)+kx$,
 $x=r \cos(\phi)$, $r=ct$ (Gly),

$$\Delta\alpha/\alpha = 1.10(0.25) 10^{-6} r \cos(\phi)$$

gradient direction $17.6(0.6)^\circ$, $-58(6)^\circ$

4.2 σ deviation from zero. Data from two largest telescopes, Keck and VLT, give consistent results. 300 systems.

New interpretation: **Spatial variation**

Northern+(new)Southern hemisphere data:
Linear variation with distance along some
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$$x=r \cos(\phi), \quad r=ct \text{ (Gly)},$$

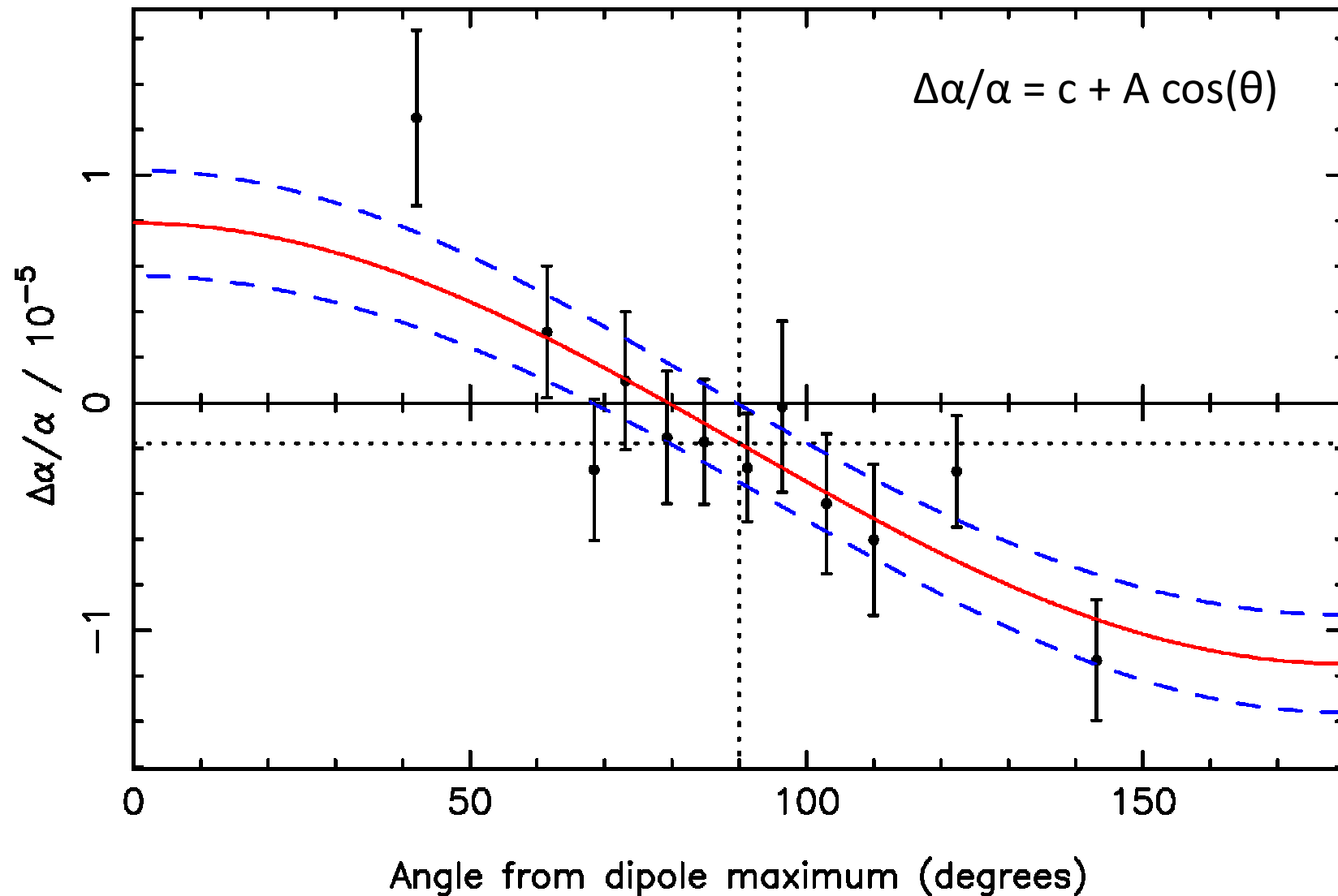
$$\Delta\alpha/\alpha = 1.2 \cdot 10^{-6} \cdot r \cos(\phi) \quad \text{dipole}$$

4.1 σ deviation from zero. Data from two largest
telescopes, Keck and VLT, give consistent
results. 300 systems.

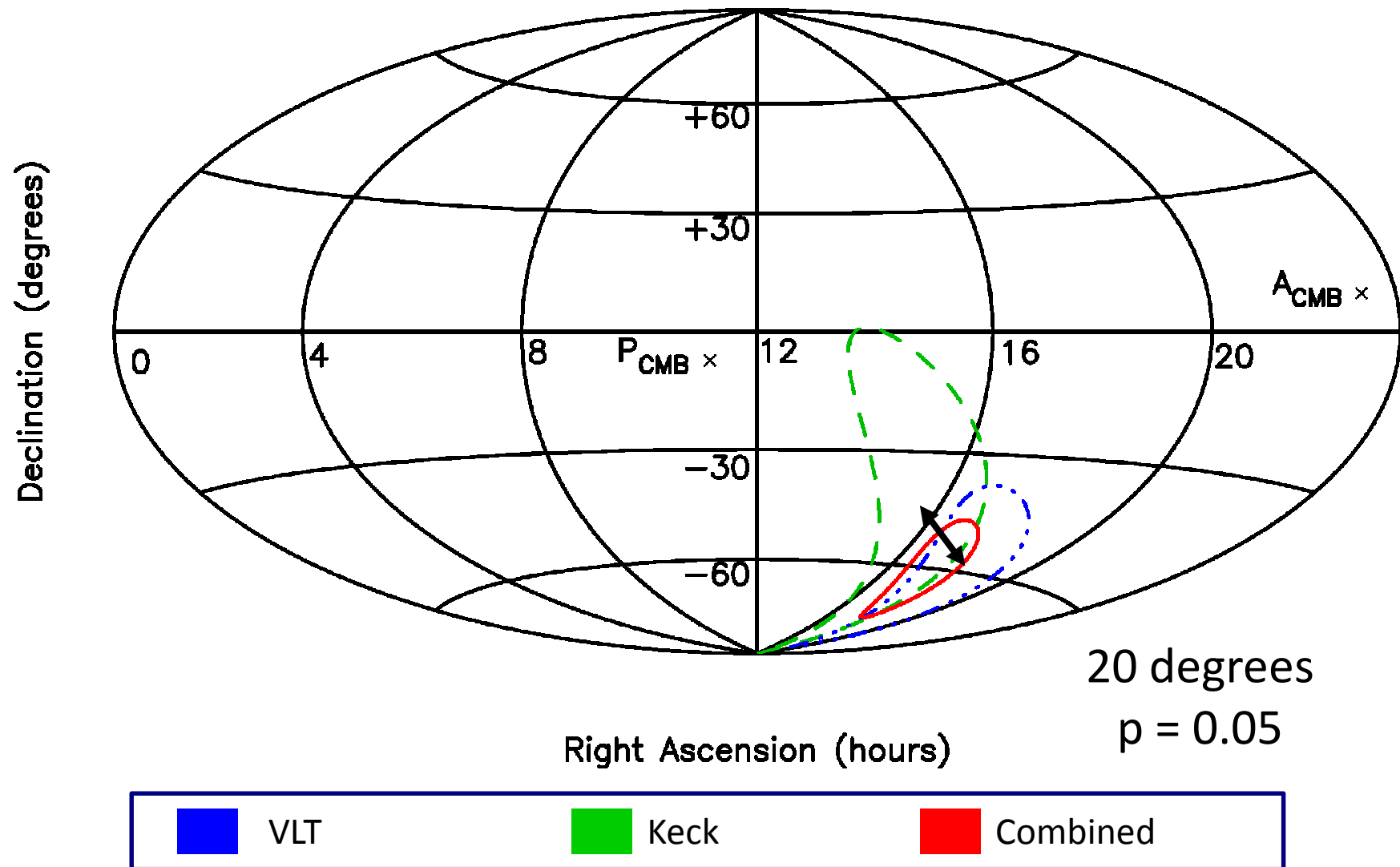
Results for m_q/Λ_{QCD} and m_e/m_p

Big Bang Nucleosynthesis data and H_2 molecule
data are consistent with the direction of the dipole.

4.1 σ evidence for a $\Delta\alpha/\alpha$ dipole from VLT + Keck



The Keck & VLT dipoles point in the same direction



m_e / M_p limit from NH_3 -2 systems

Inversion spectrum: exponentially small “quantum tunneling” frequency $\omega_{\text{inv}} = W \exp(-S(m_e / M_p))$

ω_{inv} is exponentially sensitive to m_e / M_p

Laboratory measurements proposed (Veldhoven et al)

Flambaum, Kozlov PRL 2007

First enhanced effect in quasar spectra

$\Delta(m_e / M_p) / (m_e / M_p) = -0.6(1.9)10^{-6}$ No variation

$z=0.68$, 6.5 billion years ago, $-1(3)10^{-16}$ /year

More accurate measurements

Murphy, Flambaum, Henkel, Muller. Science 2008 $-0.74(0.47)(0.76)10^{-6}$

Henkel et al AA 2009 $z=0.87$ $<1.4 \cdot 10^{-6}$ 3σ

Levshakov, Molaro, Kozlov 2008 our Galaxy $0.5(0.14)10^{-7}$

Hydrogen molecule - 4 systems

$$\Delta(m_e / M_p) / (m_e / M_p) =$$

$$3.3(1.5) \cdot 10^{-6} r \cos(\phi)$$

gradient direction $16.7(1.5)^\circ$, $-62(5)^\circ$

consistent with α gradient direction

$$17.6(0.6)^\circ$$

If we assume the same direction

$$2.6(1.3) \cdot 10^{-6} r \cos(\phi) \quad 4\% \text{ by chance}$$

Big Bang nucleosynthesis: dependence on quark mass

- Flambaum, Shuryak 2002
- Flambaum, Shuryak 2003
- Dmitriev, Flambaum 2003
- Dmitriev, Flambaum, Webb 2004
- Coc, Nunes, Olive, Uzan, Vangioni 2007
- Dent, Stern, Wetterich 2007
- Flambaum, Wirlinga 2007
- Berengut, Dmitriev, Flambaum 2009

Deuterium abundance – 7 points

Big Bang Nucleosynthesis data give direction of the gradient in the deuterium abundance consistent with the direction of the α gradient. However, the amplitude of the relative spatial variation 0.0045(35) is not statistically significant. This would result in relative variation of $X = m_q / \Lambda_{\text{QCD}}$

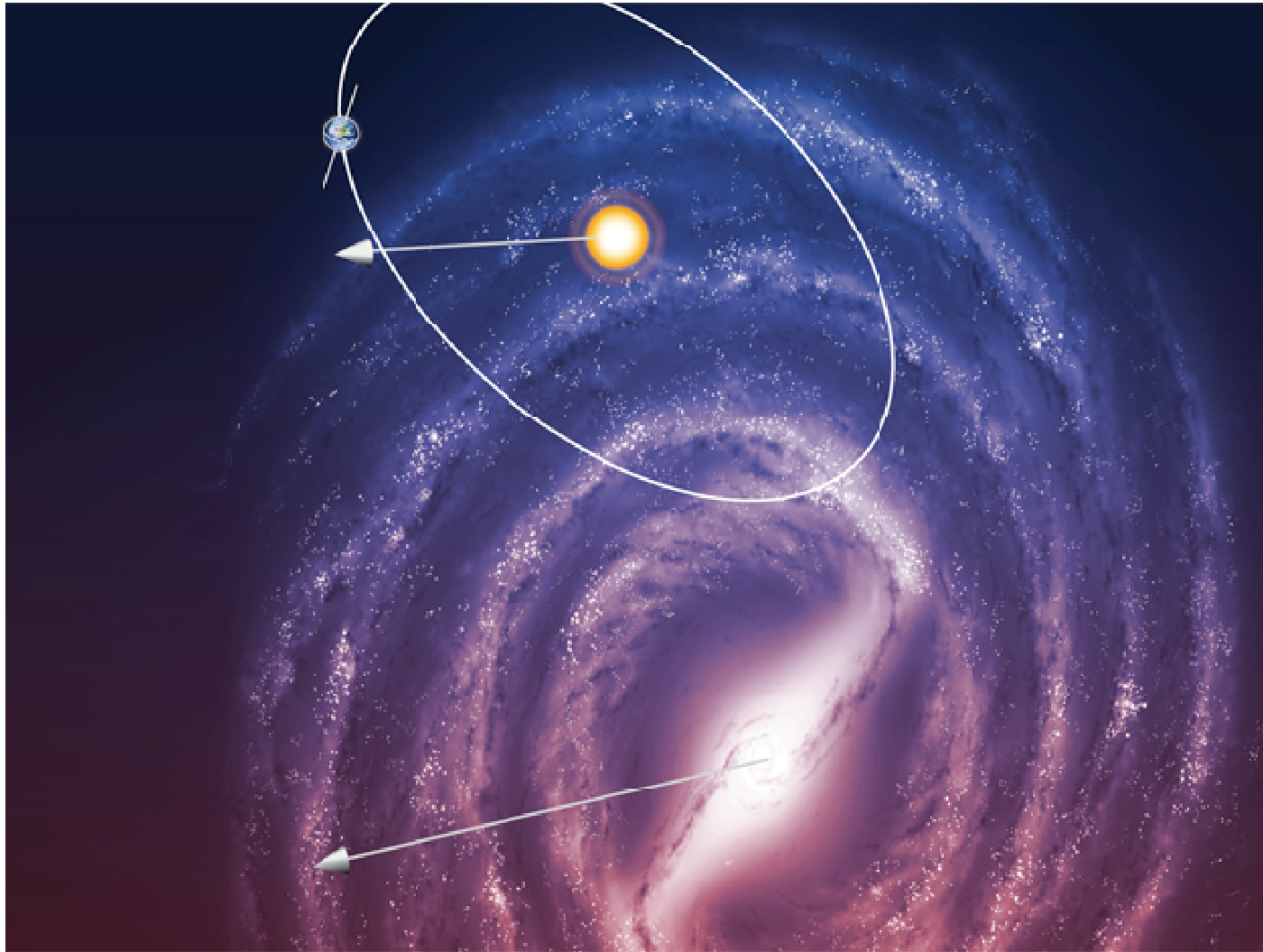
$$\Delta X/X = 0.0013(10) \, r \cos(\phi)$$

$$\Delta \alpha/\alpha = 0.003(3) \, r \cos(\phi)$$

Compare with QSO

$$\Delta \alpha/\alpha = 1.10(0.25) \, 10^{-6} \, r \cos(\phi)$$

Gradient α points down



Oklo natural nuclear reactor

$n + {}^{149}\text{Sm}$ capture cross section is dominated by $E_r = 0.1 \text{ eV}$ resonance.
Shlyakhter-limit on $\Delta\alpha/\alpha$ two billion years ago

Our QCD/nuclear calculations

$$\Delta E_r = 10 \text{ MeV} \Delta X_q / X_q - 1 \text{ MeV} \Delta\alpha/\alpha$$

$$X_q = m_q / \Lambda_{\text{QCD}}, \quad \text{enhancement } 10 \text{ MeV} / 0.1 \text{ eV} = 10^8$$

Galaxy moves 552 km/s relative to CMB, $\cos(\phi) = 0.23$

Dipole in space: $\Delta E_r = (10 R - 1) \text{ meV}$

Fujii et al $|\Delta E_r| < 20 \text{ MeV}$

Gould et al, $-12 < \Delta E_r < 26 \text{ meV}$

Petrov et al $-73 < \Delta E_r < 62 \text{ meV}$

Consequences for atomic clocks

- Sun moves 369 km/s relative to CMB
 $\cos(\phi)=0.1$

This gives average laboratory variation

$$\Delta\alpha/\alpha = 1.5 \cdot 10^{-18} \cos(\phi) \text{ per year}$$

- Earth moves 30 km/s relative to Sun-
 $1.6 \cdot 10^{-20} \cos(\omega t)$ annual modulation

Big Bang Nucleosynthesis: Dependence on $m_q / \Lambda_{\text{QCD}}$

- ^2H $1+7.7x=1.07(15)$ $x=0.009(19)$
- ^4He $1-0.95x=1.005(36)$ $x=-0.005(38)$
- ^7Li $1-50x=0.33(11)$ $x=0.013(02)$

Final result

$$x = \Delta X_q / X_q = 0.013 (02), \quad X_q = m_q / \Lambda_{\text{QCD}}$$

If we fit spatial dipole, the direction is the same as in quasar data.

Measurements m_e / M_p or $m_e / \Lambda_{\text{QCD}}$

- Tsanavaris, Webb, Murphy, Flambaum, Curran PRL 2005

Hyperfine H/optical , 9 quasar absorption systems with Mg, Ca, Mn, C, Si, Zn, Cr, Fe, Ni

Measured $X = \alpha^2 g_p m_e / M_p$

$\Delta X/X = 0.6(1.0)10^{-5}$ **No variation**

m_e / M_p limit from NH_3

Inversion spectrum: exponentially small “quantum tunneling” frequency

$$\omega_{\text{inv}} = W \exp(-S)$$

$$S = (m_e / M_p)^{-0.5} f(E_{\text{vibration}}/E_{\text{atomic}}), \quad E_{\text{vibration}}/E_{\text{atomic}} = \text{const} (m_e / M_p)^{-0.5}$$

ω_{inv} is exponentially sensitive to m_e / M_p

Flambaum, Kozlov PRL 2007

First enhanced effect in quasar spectra, 5 times

$$\Delta(m_e / M_p) / (m_e / M_p) = -0.6(1.9)10^{-6} \quad \text{No variation}$$

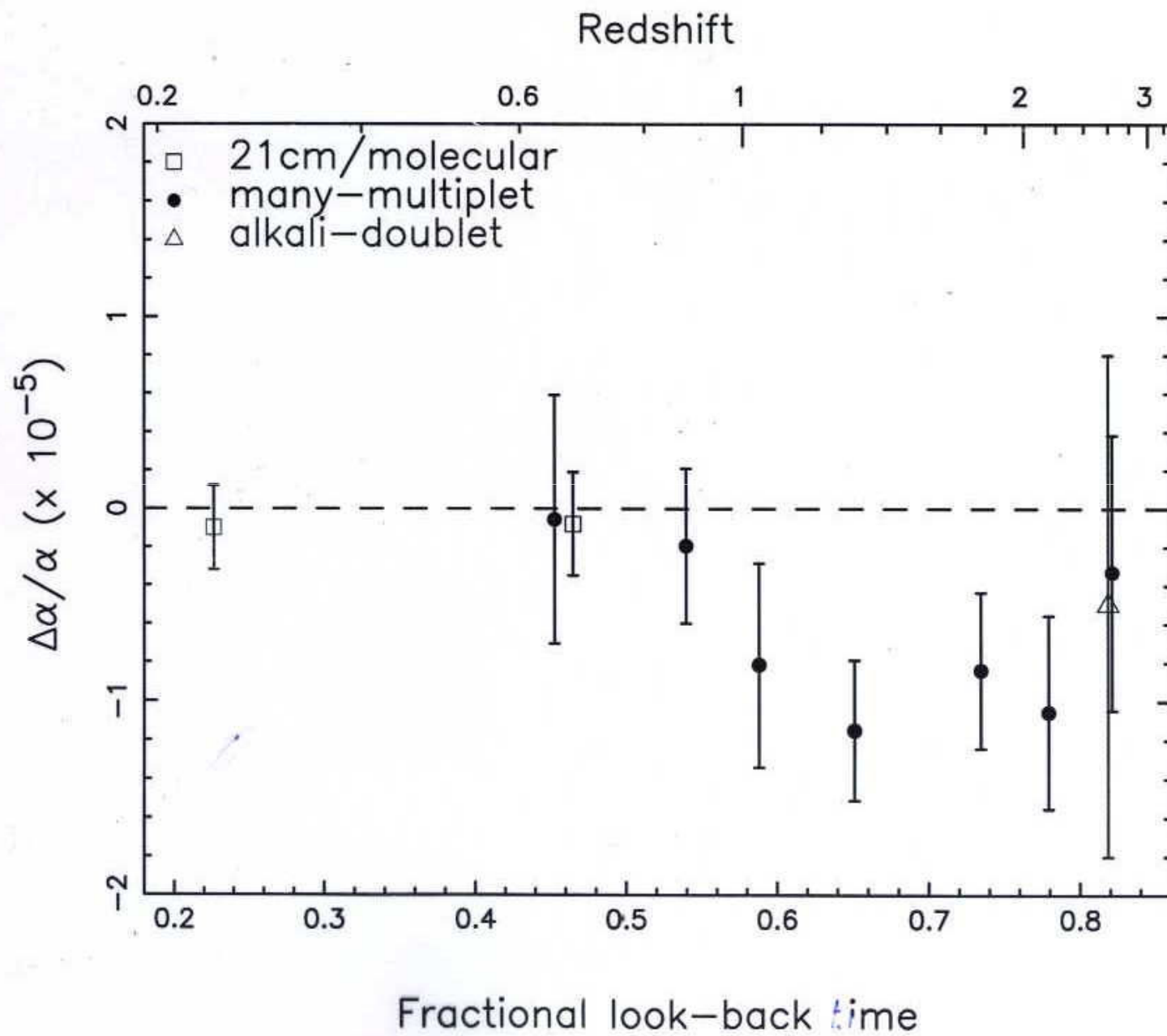
$z=0.68$, 6.5 billion years ago, $-1(3)10^{-16}$ /year

More accurate measurements

Murphy, Flambaum, Henkel, Muller. Science 2008 -
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Levshakov, Molaro, Kozlov 2008 our Galaxy $0.5(0.14)10^{-7}$



Measurements m_e / M_p or $m_e / \Lambda_{\text{QCD}}$

- Reinhold, Buning, Hollenstein, Ivanchik, Petitjean, Ubachs PRL 2006 , H_2 molecule, 2 systems

$$\Delta(m_e / M_p) / (m_e / M_p) = -2.4(0.6)10^{-5} \quad \text{Variation } 4 \sigma !$$

Higher redshift, $z=2.8$

Space-time variation? Grand Unification model?

2008 Wendt, Reimers $<4.9 \cdot 10^{-5}$

2008 Webb et al $0.26(0.30)10^{-5}$

Oklo natural nuclear reactor

$n + {}^{149}\text{Sm}$ capture cross section is dominated by

$E_r = 0.1 \text{ eV}$ resonance

Shlyakhter; Damour, Dyson; Fujii et al

Limits on variation of α

Flambaum, Shuryak 2002, 2003 Dmitriev, Flambaum 2003

Flambaum, Wirlinga 2008

$$\Delta E_r = 10 \text{ MeV} \Delta X_q / X_q - 1 \text{ MeV} \Delta \alpha / \alpha$$

$X_q = m_q / \Lambda_{\text{QCD}}$, enhancement $10 \text{ MeV} / 0.1 \text{ eV} = 10^8$

2006 Gould et al, Petrov et al $|\Delta E_r| < 0.1 \text{ eV}$,

$|\Delta X/X| < 10^{-8}$ two billion years ago, $10^{-17} / \text{year}$

There are non-zero solutions

Oklo natural nuclear reactor

1.8 billion years ago

$n + {}^{149}\text{Sm}$ capture cross section is dominated
by $E_r = 0.1 \text{ eV}$ resonance

Shlyakhter; Damour, Dyson; Fujii et al

$$\Delta E_r = 1 \text{ MeV } \Delta\alpha/\alpha$$

Limits on variation of alpha

Oklo: limits on $X_q = m_q / \Lambda_{\text{QCD}}$

Flambaum, Shuryak 2002, 2003 Dmitriev, Flambaum 2003

Flambaum, Wirlinga 2008

$$^{150}\text{Sm} \quad \Delta E_r = 10 \text{ MeV} \Delta X_q / X_q - 1 \text{ MeV} \Delta \alpha / \alpha$$

Limits on $x = \Delta X_q / X_q - 0.1 \Delta \alpha / \alpha$ from

$$\text{Fujii et al} \quad |\Delta E_r| < 0.02 \text{ eV} \quad |x| < 2 \cdot 10^{-9}$$

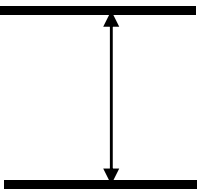
$$\text{Petrov et al} \quad |\Delta E_r| < 0.07 \text{ eV} \quad |x| < 8 \cdot 10^{-9}$$

$$\text{Gould et al} \quad |\Delta E_r| < 0.026 \text{ eV} \quad |x| < 3 \cdot 10^{-9}, < 1.6 \cdot 10^{-18} \text{ y}^{-1}$$

There is second, non-zero solution $x = 1.0(1) \cdot 10^{-8}$

Atomic clocks

Cesium primary frequency standard:

HFS of 6s: $F=4$  $F=3$ $\nu = 9\,192\,631\,770\text{ Hz}$

Also: Rb, Cd^+ , Ba^+ , Yb^+ , Hg^+ , etc.

E.g. $\nu(\text{Hg}^+) = 40\,507\,347\,996.841\,59(14)(41)\text{ Hz}$
(D. J. Berkeland *et al*, 1998).

Optical frequency standards:

Z	Atom	Transition	Frequency	Source
20	Ca	1S_0 - 3P_1	455 986 240 494 144(5.3) Hz	Degenhardt et al, 2005
38	Sr ⁺	1S_0 - 3P_1	434 829 121 311(10) kHz	Ferrari et al, 2003
49	In ⁺	1S_0 - 3P_0	1 267 402 452 899 920(230) Hz	von Zanthier et al, 2005
70	Yb ⁺	$^2S_{1/2}$ - $^2F_{7/2}$	642 121 496 772 300(600) Hz	Hosaka et al, 2005

Also: H, Al⁺, Sr, Ba⁺, Yb, Hg, Hg⁺, Tl⁺, Ra⁺, etc.

Accuracy about **10⁻¹⁵** can be further improved to **10⁻¹⁸!**

Atomic clocks:

Comparing rates of different clocks over long period of time can be used to study time variation of fundamental constants!

Optical transitions: α

Microwave transitions: $\alpha, (m_e, m_q)/\Lambda_{\text{QCD}}$

Advantages:

- Very narrow lines, high accuracy of measurements.
- Flexibility to choose lines with larger sensitivity to variation of fundamental constants.
- Simple interpretation (local time variation).

Calculations to link change of frequency to change of fundamental constants:

Optical transitions: atomic calculations (as for quasar absorption spectra) for many narrow lines in Al II, Ca I, Sr I, Sr II, In II, Ba II, Dy I, Yb I, Yb II, Yb III, Hg I, Hg II, Tl II, Ra II, ThIV

$$\omega = \omega_0 + q(\alpha^2/\alpha_0^2 - 1)$$

Microwave transitions: hyperfine frequency is sensitive to nuclear magnetic moments and nuclear radii

We performed atomic, nuclear and QCD calculations of powers κ, β for H, D, Rb, Cd⁺, Cs, Yb⁺, Hg⁺

$$V = C(Ry)(m_e/M_p)\alpha^{2+\kappa} (m_q/\Lambda_{QCD})^\beta, \quad \Delta\omega/\omega = \Delta V/V$$

Calculations to link change of frequency to change of fundamental constants:

Optical transitions: atomic calculations (as for quasar absorption spectra) for many narrow lines in Al II, Ca I, Sr I, Sr II, In II, Ba II, Dy I, Yb I, Yb II, Yb III, Hg I, Hg II, Tl II, Ra II ...

$$\omega = \omega_0 + q(\alpha^2/\alpha_0^2 - 1)$$

Microwave transitions: hyperfine frequency is sensitive to α , nuclear magnetic moments and nuclear radii

We performed atomic, nuclear and QCD calculations

of powers κ, β for H, D, He, Rb, Cd⁺, Cs, Yb⁺, Hg⁺...

$$V = C(\text{Ry})(m_e/M_p)\alpha^{2+\kappa} (m_q/\Lambda_{\text{QCD}})^\beta, \quad \Delta\omega/\omega = \Delta V/V$$

$$^{133}\text{Cs}: \kappa = 0.83, \beta = 0.002$$

Cs standard is insensitive to variation of m_q/Λ_{QCD} !

$$^{87}\text{Rb}: \kappa = 0.34, \beta = -0.02$$

$$^{171}\text{Yb}^+: \kappa = 1.5, \beta = -0.10$$

$$^{199}\text{Hg}^+: \kappa = 2.28, \beta = -0.11$$

$$^1\text{H}: \kappa = 0, \beta = -0.10$$

Complete Table in Phys.Rev.A79,054102(2009)

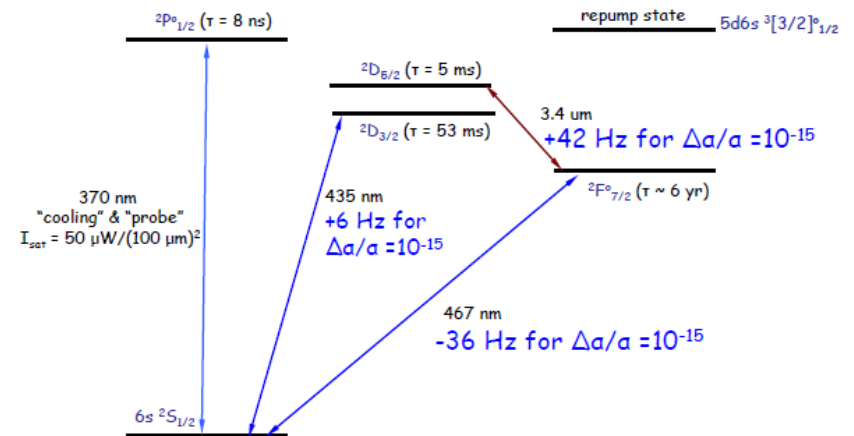
Results for variation of fundamental constants

Source	Clock ₁ /Clock ₂	$d\alpha/dt/\alpha(10^{-16} \text{ yr}^{-1})$
Blatt <i>et al</i> , 2007	Sr(opt)/Cs(hfs)	-3.1(3.0)
Fortier <i>et al</i> 2007	Hg+(opt)/Cs(hfs)	-0.6(0.7) ^a
Rosenband <i>et al</i> /08	Hg+(opt)/Al+(opt)	-0.16(0.23)
Peik <i>et al</i> , 2006	Yb+(opt)/Cs(hfs)	4(7)
Bize <i>et al</i> , 2005	Rb(hfs)/Cs(hfs)	1(10) ^a

^aassuming $m_{q,e}/\Lambda_{QCD} = \text{Const}$

Combined results: $d/dt \ln \alpha = -1.6(2.3) \times 10^{-17} \text{ yr}^{-1}$
 $d/dt \ln(m_q/\Lambda_{QCD}) = 3(25) \times 10^{-15} \text{ yr}^{-1}$
 $m_e/M_p \text{ or } m_e/\Lambda_{QCD} -1.9(4.0) \times 10^{-16} \text{ yr}^{-1}$

Larger q in Yb II



Ground state $f^{14}\ 6s\ ^2S_{1/2} \leftrightarrow f^{13}\ 6s^2\ ^2F_{7/2}$ $q_1 = -60$
000

$f^{13}\ 6s^2\ ^2F_{7/2}$ to higher metastable states q_2 up to 85
000

Difference $q = q_2 - q_1$ may exceed 140 000,
so the sensitivity to alpha variation using
comparison of two transitions in Yb II exceeds

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Transition frequency shifts with fine-structure constant variation for Yb II

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Larger q in Yb II

Transition from ground state $f^{14} 6s^2 S_{1/2}$ to metastable state $f^{13} 6s^2 {}^2F_{7/2}$ $q_1 = -60\,000$

For transitions from metastable state $f^{13} 6s^2 {}^2F_{7/2}$ to higher metastable states q_2 are positive and large, up to 85 000

Difference $q = q_2 - q_1$ may exceed 140 000,

so the sensitivity to alpha variation using comparison of two transitions in Yb II exceeds that in HgII/AlI comparison (measurements at NIST) 2.7 times.

Shift of frequency difference is 2.7 times larger

Porsev, Flambaum, Torgerson

Largest q in multiply charged ions, narrow lines

q increases as $Z^2 (Z_i+1)^2$

To keep frequencies in optical range we use configuration crossing as a function of Z

Crossing of 5f and 7s

Th IV: $q_1 = -75\ 300$

Crossing of 4f and 5s

Sm¹⁵⁺, Pm¹⁴⁺, Nd¹³⁺

Difference $q = q_2 - q_1$ is 260 000

5 times larger than in Hg II/Al II

Relative sensitivity enhancement up to 500

Berengut, Dzuba, Flambaum, Porsev

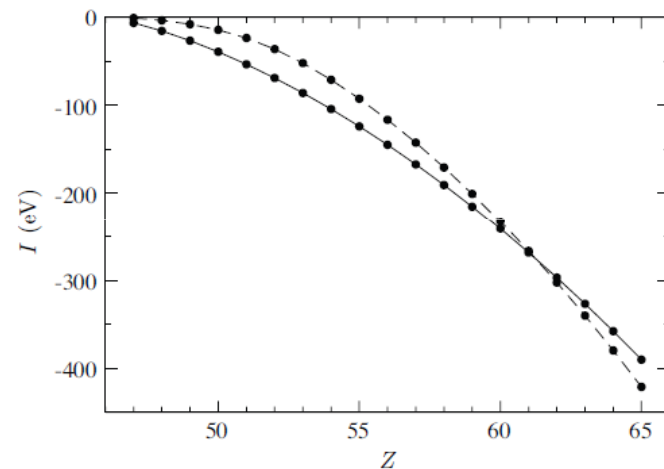


FIG. 2. Dirac-Fock ionisation energies of 5s (solid) and 4f_{7/2} (dashed) levels for the Ag isoelectronic sequence.

[arXiv:1007.1068](https://arxiv.org/abs/1007.1068)

Enhancement of relative effect

Dy: $4f^{10}5d6s$ $E=19797.96... \text{ cm}^{-1}$, $q= 6000 \text{ cm}^{-1}$

$4f^95d^26s$ $E=19797.96... \text{ cm}^{-1}$, $q= -23000 \text{ cm}^{-1}$

Interval $\Delta\omega = 10^{-4} \text{ cm}^{-1}$



Relative enhancement $\Delta\omega/\omega_0 = 10^8 \Delta\alpha/\alpha$

Measurement Berkeley $d\ln\alpha/dt = -2.9(2.6) \times 10^{-15} \text{ yr}^{-1}$

Close narrow levels in molecules and nucleus ^{229}Th

Dysprosium miracle

Dy: $4f^{10}5d6s$ $E=19797.96... \text{ cm}^{-1}$, $q= 6000 \text{ cm}^{-1}$
 $4f^95d^26s$ $E=19797.96... \text{ cm}^{-1}$, $q= -23000 \text{ cm}^{-1}$
Interval $\Delta\omega = 10^{-4} \text{ cm}^{-1}$



Our calculations: Enhancement factor **$K = 10^8$** (!), i.e.
 $\Delta\omega/\omega_0 = 10^8 \Delta\alpha/\alpha$

Measurements (Berkeley, Los Alamos)

$$d\ln\alpha/dt = -2.7(2.6) \times 10^{-15} \text{ yr}^{-1}$$

Problem: states are not narrow!
There are close narrow levels in molecules.

More suggestions ...

Atom	State ₁		State ₂		K
Ce I	⁵ H ₃	2369.068	¹ D ₂	2378.827	2000
	³ H ₄	4762.718	³ D ₂	4766.323	13000
Nd I	⁵ K ₆	8411.900	⁷ L ₅	8475.355	950
Nd I	⁷ L ₅	11108.813	⁷ K ₆	11109.167	10 ⁵
Sm I	⁵ D ₁	15914.55	⁷ G ₂	12087.17	300
Gd II	⁸ D _{11/2}	4841. 106	¹⁰ F _{9/2}	4852.304	1800
Tb I	⁶ H _{13/2}	2771.675	⁸ G _{9/2}	2840.170	600

Enhancement in molecular clocks

DeMille et al 2004, 2008 – enhancement in Cs_2 ,
**cancellation between electron excitation and
vibration energies**

Flambaum 2006 Cancellations between rotational
and hyperfine intervals

$$\Delta\omega/\omega_0 = K \Delta\alpha/\alpha \quad \text{Enhancement } \mathbf{K = 10^2 - 10^3}$$

Flambaum, Kozlov 2007 Cancellations between
fine structure and vibrations

$$\Delta\omega/\omega_0 = K (\Delta\alpha/\alpha - 1/4 \Delta\mu/\mu)$$

$$\text{Enhancement } \mathbf{K = 10^4 - 10^5}$$

Enhancement in molecular clocks

DeMille 2004, DeMille et al 2008 – enhancement in Cs_2 , **cancellation between electron excitation and vibration energies**

Flambaum 2006 Cancellations between rotational and hyperfine intervals in very narrow microwave transitions in LaS, LaO, LuS, LuO, YbF, etc.

$$\omega_0 = E_{\text{rotational}} - E_{\text{hyperfine}} = E_{\text{hyperfine}} / 100 - 1000$$

$$\Delta\omega/\omega_0 = K \Delta\alpha/\alpha \quad \text{Enhancement } \mathbf{K = 10^2 - 10^3}$$

Cancellation between fine structure and vibrations in molecules

Flambaum, Kozlov PRL2007 **$K = 10^4 - 10^5$** ,

SiBr, Cl_2^+ ... microwave transitions between narrow excited states, sensitive to α and $\mu = m_e/M_p$

$$\omega_0 = E_{\text{fine}} - E_{\text{vibrational}} = E_{\text{fine}}/K$$

$$\Delta\omega/\omega_0 = K (\Delta\alpha/\alpha - 1/4 \Delta\mu/\mu)$$

Enhancement **$K = 10^4 - 10^5$**

E_{fine} is proportional to $Z^2\alpha^2$

$E_{\text{vibrational}} = n\omega$ is proportional to $n\mu^{0.5}$, $n=1,2,\dots$

Enhancement for all molecules along the lines $Z(\mu, n)$

Shift 0.003 Hz for $\Delta\alpha/\alpha = 10^{-16}$; **width 0.01 Hz**

Compare with Cs/Rb hyperfine shift 10^{-6} Hz

HfF^+ **$K = 10^3$** shift 0.1 Hz

Cancellation between fine structure and rotation in light molecules

Bethlem, Bunning, Meijer, Ubach 2009

OH, OD, CN, CO, CH, LiH, ...

E_{fine} is proportional to $Z^2 \alpha^2$

$E_{\text{rotational}}$ is proportional to $L \mu$, $L=0,1,2,\dots$

$$\mu = m_e / M_p$$

Enhancement for all molecules along the lines $Z(\mu, L)$

Nuclear clocks

(suggested by Peik, Tamm 2003)

Very narrow UV transition between first excited and ground state in ^{229}Th nucleus

Energy 7.6(5) eV, width 10^{-4} Hz

Flambaum PRL2006

Nuclear/QCD estimate: Enhancement 10^5 ,

$$\Delta\omega/\omega_0 = 10^5 (0.1\Delta\alpha/\alpha + \Delta X_q/X_q)$$

$$X_q = m_q / \Lambda_{\text{QCD}},$$

Shift 10^5 Hz for $\Delta\alpha/\alpha = 10^{-15}$

Compare with atomic clock shift 1 Hz

^{235}U energy 76 eV, width $6 \cdot 10^{-4}$ Hz

Nuclear clocks

Peik, Tamm 2003: UV transition between first excited and ground state
in ^{229}Th nucleus Energy **7.6(5) eV**, width **10^{-3} Hz. Perfect clock!**

Flambaum 2006: Nuclear/QCD estimate- Enhancement **10^5**

He, Re; Flambaum, Wiringa; Flambaum, Auerbach, Dmitriev;
Hayes, Friar, Moller; Litvinova, Felmeier, Dobaczewski, Flambaum;

$\Delta\omega = \mathbf{10^{19}}$ Hz ($\Delta\alpha/\alpha + 10 \Delta X_q/X_q$), $X_q = m_q / \Lambda_{\text{QCD}}$,

Shift 10-100 Hz for $\Delta\alpha/\alpha = 10^{-18}$

Compare with atomic clock shift 0.001 Hz

Berengut, Dzuba, Flambaum, Porsev: Sensitivity to $\Delta\alpha/\alpha$ is expressed
via isomeric shifts of ^{229}Th atomic lines,

frequency in ^{229}Th - frequency in $^{229}\text{Th}^*$. Measure, please!

Enhancement of relative effect

Dy: $4f^{10}5d6s$ $E=19797.96... \text{ cm}^{-1}$, $q= 6000 \text{ cm}^{-1}$

$4f^95d^26s$ $E=19797.96... \text{ cm}^{-1}$, $q= -23000 \text{ cm}^{-1}$

Interval $\Delta\omega = 10^{-4} \text{ cm}^{-1}$



Relative enhancement $\Delta\omega/\omega_0 = 10^8 \Delta\alpha/\alpha$

Measurement Berkeley $d\ln\alpha/dt = -2.9(2.6) \times 10^{-15} \text{ yr}^{-1}$

Close narrow levels in molecules

Conclusions

- Spatial gradient from quasar data provides alpha variation for atomic clocks due to Earth motion at the level 10^{-18} per year and 1 meV shift in Oklo resonance. One-two orders of magnitude improvement in the measurement accuracy is needed. Three orders for meteorites.

New systems with higher absolute sensitivity include:

- transitions between ground and metastable states in highly charged ions. Frequencies are kept in laser spectroscopy range due to the configuration crossing phenomenon. An order of magnitude gain.
- ^{229}Th nucleus – highest **absolute** enhancement (10^5 times larger shift), UV transition 7eV.
- Many systems with relative enhancement due to transition between close levels: Dy atom, a number of molecules with narrow close levels,...
- Very weak indications for the spatial variation in H_2 quasar spectra and BBN abundance of deuterium. The same direction of the gradient!
- Search for anisotropy in CMB, expansion of the Universe, structure formation

Conclusions

- Spatial dipole in quasar data provides alpha variation for atomic clocks due to Earth motion at the level 10^{-18} per year.

New systems with higher absolute sensitivity include:

- transitions between metastable states in Yb II
 - transitions between ground state and metastable state in Th 3+ and many highly charged ions. Frequencies are kept in laser spectroscopy range due to the configuration crossing phenomenon. An order of magnitude gain.
 - ^{229}Th nucleus – highest **absolute** enhancement (10^5 times larger shift), UV transition 7eV.
-
- Many systems with relative enhancement due to transition between close levels: Dy atom, a number of molecules with narrow close levels,...

Nuclear clocks

Peik, Tamm 2003: UV transition between first excited and ground state in ^{229}Th nucleus. Energy **7.6(5) eV**, width **10^{-4} Hz**. **Perfect clock!**

Our nuclear/QCD calculations - Enhancement **10^5**

$$\Delta\omega/\omega_0 = \mathbf{10^5} \left(0.1\Delta\alpha/\alpha + \Delta X_q/X_q \right)$$

$$X_q = m_q / \Lambda_{\text{QCD}},$$

Shift 2000 Hz for $\Delta\alpha/\alpha = 10^{-16}$

Compare with atomic clock shift 0.1 Hz

Problem – to find this narrow transition using laser

Search: Peik et al, Lu et al, Habs et al, DeMille et al, Beck et al

^{229}Th : why enhancement?

$\omega = Q + E_{\text{pk}} + E_{\text{so}} = 7.6 \text{ eV}$ huge cancellations!

$Q = \text{Coulomb} = 100 \text{ KeV}$ 10^{-4} total Coulomb

$E_{\text{so}} = \langle V_s L S \rangle = \text{spin-orbit} = -1.0 \text{ MeV}$

$E_{\text{pk}} = \text{potential} + \text{kinetic} = 1 \text{ MeV}$

Extrapolation from light nuclei

$$\Delta E_{\text{pk}} / E_{\text{pk}} = -1.4 \Delta m_q / m_q$$

$$\Delta E_{\text{so}} / E_{\text{so}} = -0.24 \Delta m_q / m_q$$

$$\Delta \omega / \omega_0 = 10^5 (0.14 \Delta \alpha / \alpha + 1.6 \Delta X_q / X_q)$$

Dependence on α

$$\Delta\omega = Q \Delta\alpha/\alpha$$

- Total Coulomb energy 10^3 MeV in ^{229}Th
- Difference of moments of inertia between ground and excited states is 4%
- If difference in the Coulomb energy would be 0.01%, $Q=100$ KeV, estimate for the enhancement factor

$$Q/\omega_0 = 10^5 \text{ eV} / 7 \text{ eV} = 1.4 \cdot 10^4$$

Enhancement in ^{229}Th

	α	$X_q = m_q / \Lambda_{\text{QCD}}$	
Flambaum 2006	$\sim 10^5$	$0.5 \cdot 10^5$	estimate
Hayes, Frier 2007	0	impossible	arguments
He, Ren 2007	$0.04 \cdot 10^5$	$0.8 \cdot 10^5$	rel.mean field
Main effect (dependence of deformation on α) missed, change of mean-field potential only			
Dobaczewski et al 2007	$0.15 \cdot 10^5$		Hartree-Fock preliminary

²²⁹Th: Flambaum, Wiringa 2007

$\omega = E_{pk} + E_{so} = 7.6 \text{ eV}$ huge cancellations!

$E_{so} = \langle V_s L S \rangle = \text{spin-orbit} = -1.04 \text{ MeV}$

$E_{pk} = \text{potential} + \text{kinetic} = 1 \text{ MeV}$

Extrapolation from light nuclei

$\Delta E_{pk} / E_{pk} = -1.4 \Delta m_q / m_q$

$\Delta E_{so} / E_{so} = -0.24 \Delta m_q / m_q$

$\Delta \omega / \omega_0 = 1.6 \text{ } 10^5 \Delta X_q / X_q$

Difference of Coulomb energies

$$\Delta\omega = Q \Delta\alpha/\alpha$$

Hayes, Frier, Moller <30 Kev

He, Ren 30 KeV

Flambaum, Auerbach, Dmitriev

-500 Kev < Q < 1500 KeV

Litvinova, Feldmeier, Dobaczewski,

Flambaum

-300 Kev < Q < 450 KeV

Sensitivity to $\Delta\alpha$ may be obtained
from measurements

$$\Delta\omega = Q \Delta\alpha / \alpha$$

Berengut, Dzuba, Flambaum, Porsev PRL 2009

$$Q/\text{MeV} = -506 \Delta\langle r^2 \rangle / \langle r^2 \rangle + 23 \Delta Q_2 / Q_2$$

Difference of squared charge radii $\Delta\langle r^2 \rangle$ may
be extracted from isomeric shifts of
electronic transitions in Th atom or ions

Difference of electric quadrupole moments
 ΔQ_2 from hyperfine structure

Experimental progress in ^{229}Th

- Transition energy measured in Livermore
7.6 (5) eV instead of 3.5(1.0) eV
- Intensive search for direct radiation
Argonne
Peik et al,
Habs et al, ...

Ultracold atomic and molecular collisions.

Cheng Chin, Flambaum PRL2006

Enhancement near Feshbach resonance.

Variation of scattering length

$$\Delta a/a = K \Delta\mu/\mu, \quad K = 10^2 - 10^{12}$$

$$\mu = m_e/M_p$$

Hart, Xu, Legere, Gibble Nature 2007

Accuracy in scattering length 10^{-6}

Evolution fundamental constants and their dependence on scalar and gravitational potential

Fundamental constants depend on scalar field ϕ –
dark energy, Higgs, dilaton, distance between
branes, size of extra dimensions.

Cosmological evolution of ϕ in space and time is
linked to evolution of matter.

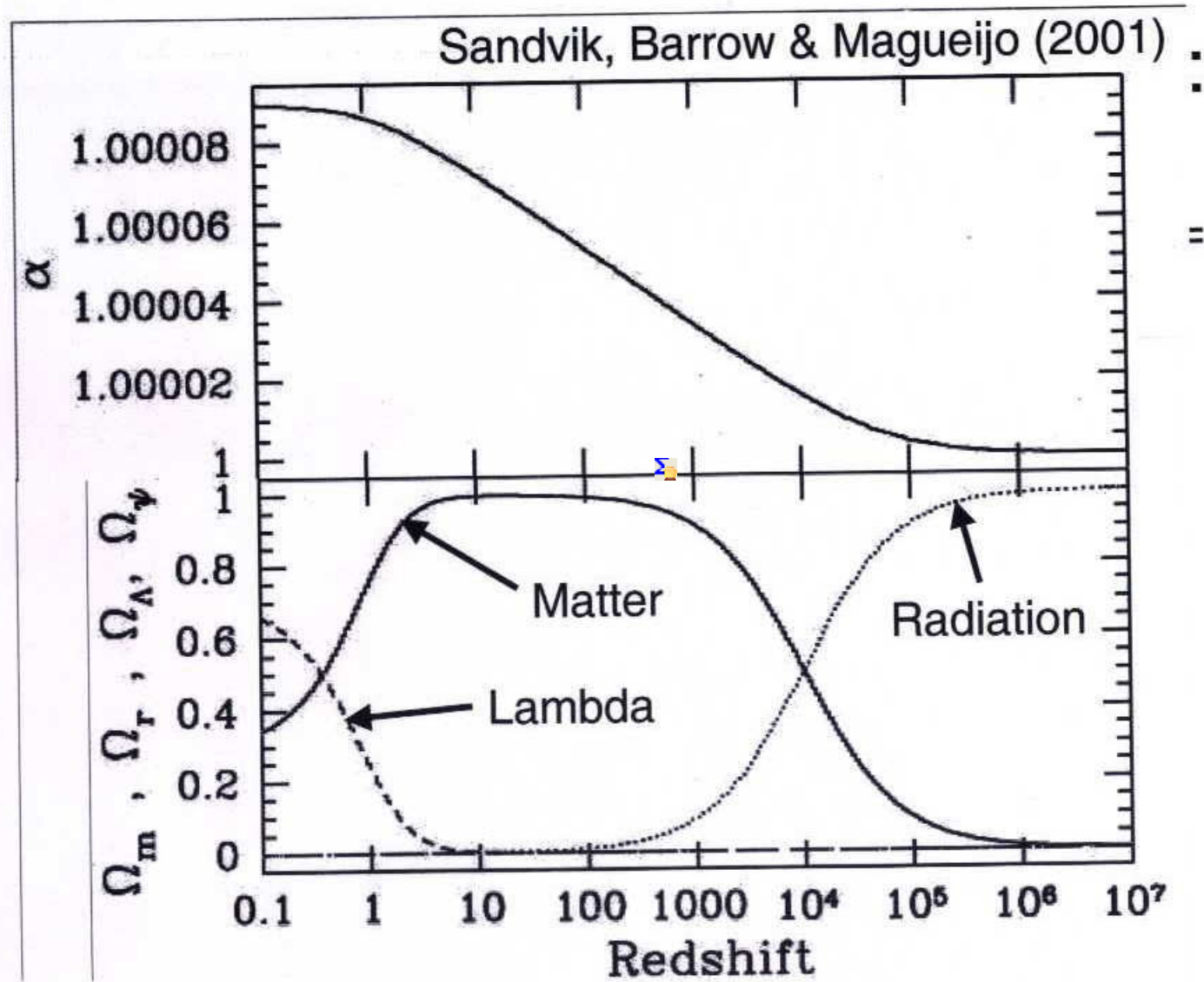
Changes of Universe equation of state:

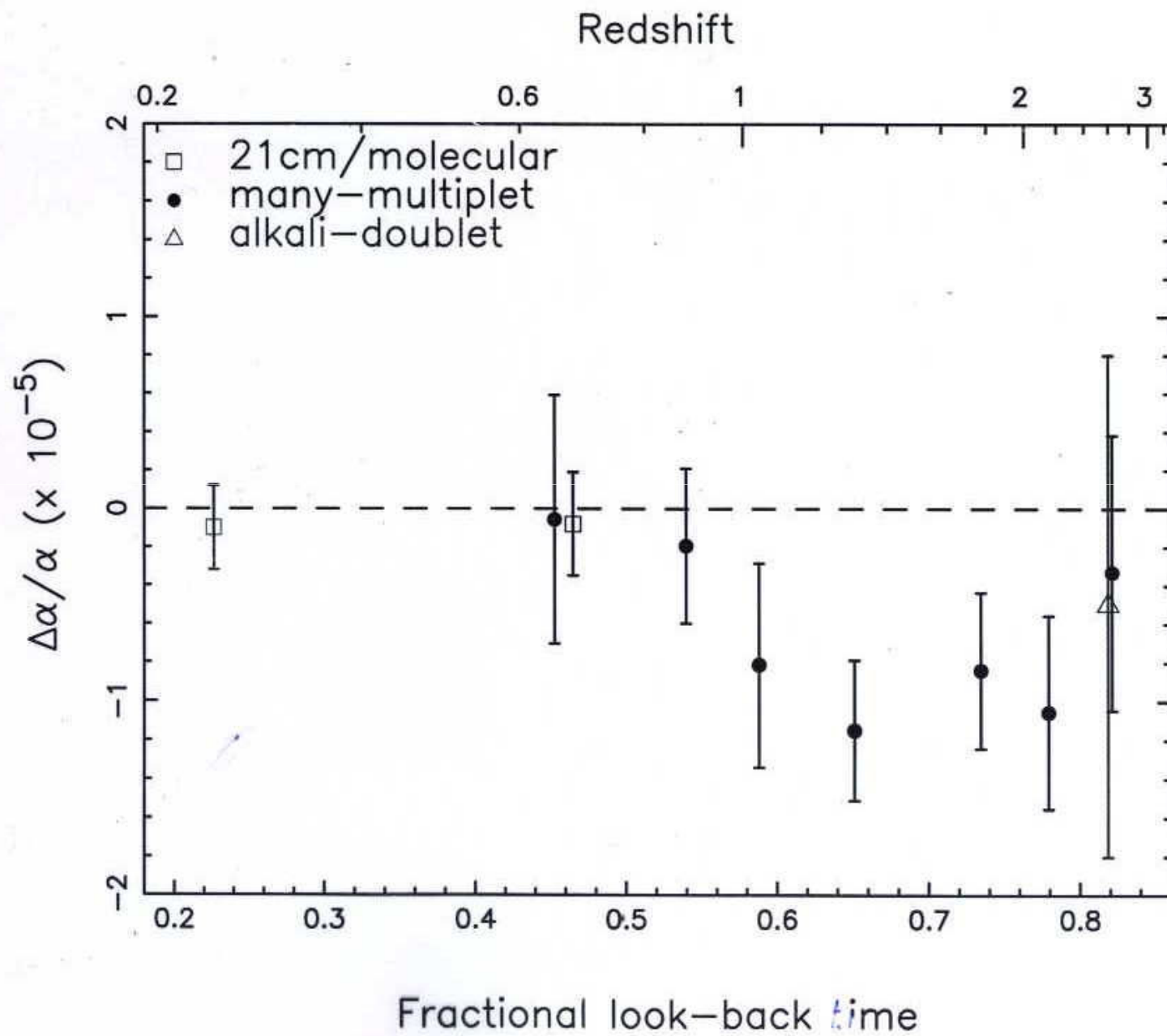
Radiation domination, cold matter domination, dark
energy domination-

Change of ϕ – change of $\alpha(\phi)$

Bekenstein model

Olive, Pospelov - driven by dark matter





Scalar charge-source of ϕ

Massive bodies have scalar charge S
proportional to the number of particles

Scalar field $\phi = S/r$, proportional to
gravitational potential GM/r -

Variation of α proportional to gravitational
potential

$$\delta\alpha/\alpha = K_\alpha \delta(GM/rc^2)$$

Neutron star, white/brown dwarfs, galaxy,
Earth, Sun – compare spectra, $\omega(\alpha)$

Dependence of fundamental constants on gravitational or scalar potential

Projects –atomic clocks at satellites in space or close to Sun (JPL project)

Earth orbit is elliptic, 3% change in distance to Sun

Fortier et al – $\text{Hg}^{+(\text{opt})}/\text{Cs}$, Ashby et al -H/Cs

Flambaum, Shuryak : limits on dependence of α , m_e/Λ_{QCD} and m_q/Λ_{QCD} on gravity

$$\delta\alpha/\alpha = K_\alpha \delta(GM/rc^2)$$

$$K_\alpha + 0.17 K_e = -3.5(6.0) \cdot 10^{-7}$$

$$K_\alpha + 0.13 K_q = 2(17) \cdot 10^{-7}$$

New results from Dy, Sr/Cs

Dysprosium $\delta\alpha/\alpha = K_\alpha \delta(GM/rc^2)$

Dy: $4f^{10}5d6s$ $E=19797.96... \text{ cm}^{-1}$, $q= 6000 \text{ cm}^{-1}$

$4f^95d^26s$ $E=19797.96... \text{ cm}^{-1}$, $q= -23000 \text{ cm}^{-1}$

Interval $\Delta\omega = 10^{-4} \text{ cm}^{-1}$



Enhancement factor **$K = 10^8$** , i.e. $\Delta\omega/\omega_0 = 10^8 \Delta\alpha/\alpha$

Measurements Ferrel et al 2007

$$K_\alpha = -8.7(6.6) \cdot 10^{-6}$$

$$K_e = 4.9(3.9) \cdot 10^{-6} \quad K_q = 6.6(5.2) \cdot 10^{-6}$$

Sr(optical)/Cs comparison :

S.Blatt et al 2008

New best limits

$$K_{\alpha}=2.5(3.1) \ 10^{-6}$$

$$K_e=-1.1(1.7) \ 10^{-6}$$

$$K_q=-1.9(2.7) \ 10^{-6}$$

Microwave clocks in optical lattice

- Sr, Hg, ... in optical lattice. Optical clocks.

Magic wavelength-cancellation of dynamical Stark shifts, very accurate optical frequencies.

Katory, Kimble, Ye, ...

- Hyperfine transitions, linear polarization - no magic wavelength in atoms with valence s-electron: Cs, Rb, ...

There is magic wavelength for atoms with $p_{1/2}$ electron - due to hyperfine mixing $p_{1/2}$ - $p_{3/2}$ Al, Ga, ...

Beloy, Derevinako, Dzuba, Flambaum PRL 2009

- Circular polarisation - all wavelengths are magic for a certain direction of magnetic field - "magic angle"
Cs (primary standard), Rb, ... PRL 2008

Conclusions

- Quasar data: MM method provided sensitivity increase 100 times. Anchors, positive and negative shifters-control of systematics. Keck-variation of α , VLT-?. Systematics or spatial variation.
- m_e/M_p : hyperfine H/optical, NH_3 — no variation, H_2 - variation 4σ ? Space-time variation? Grand Unification model?
- Big Bang Nucleosynthesis: may be interpreted as a variation of m_q/Λ_{QCD}
- Oklo: sensitive to m_q/Λ_{QCD} , effect $<10^{-8}$
- Atomic clocks: present time variation of α , m/Λ_{QCD}
- Transitions between narrow close levels in atoms and molecules – huge enhancement of the **relative** effect
- ^{229}Th nucleus – **absolute** enhancement (10^5 times larger shift)
- Dependence of fundamental constants on gravitational potential

No variation for small red shift, hints for variation at high red shift

Conclusions

- Quasar data: MM method provided sensitivity increase 100 times. Anchors, positive and negative shifters-control of systematics. Keck-variation of α , VLT-?. Systematics or spatial variation.
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- Big Bang Nucleosynthesis: may be interpreted as a variation of m_q/Λ_{QCD}
- Oklo: sensitive to m_q/Λ_{QCD} , effect $<10^{-8}$
- Atomic clocks: present time variation of α , m/Λ_{QCD}
- Highest sensitivity is in Yb II and Th IV, compare transitions from ground and metastable states
- Transitions between narrow close levels in atoms and molecules – huge enhancement of the **relative** effect
- ^{229}Th nucleus – **absolute** enhancement (10^5 times larger shift)
- Dependence of fundamental constants on gravitational potential

No variation for small red shift, hints for variation at high red shift