

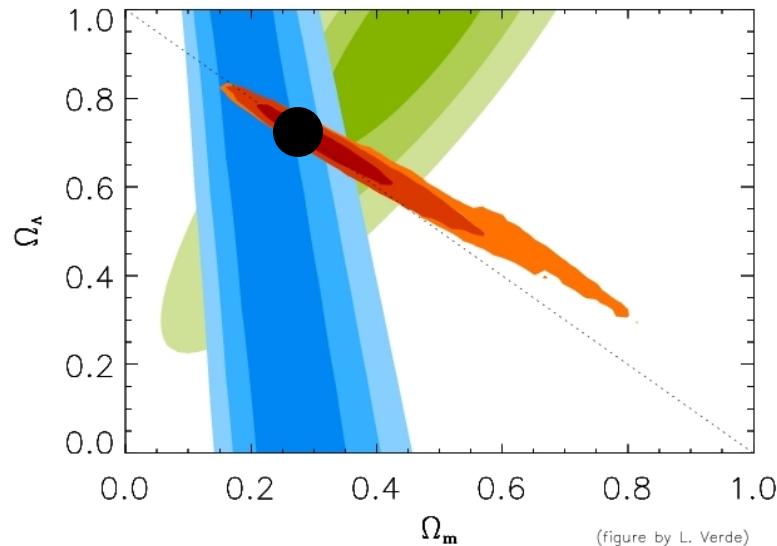
The dark side of gravity

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ESF Porto 2008

Observations are converging...



(figure by L. Verde)

...to an unexpected universe

The dark energy problem

$$F(g_{\mu\nu}) + R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi GT_{\mu\nu} + 8\pi GT_{\mu\nu}(\phi)$$

gravity

matter



$$\Omega_{tot} \approx 1$$

$$\Omega_{cluster} \approx 0.3$$

Solution: modify either the Matter sector \longrightarrow DE

or the Gravity sector \longrightarrow MG

...in such a way that : $\frac{P_X}{\rho_X} = w_X \approx -1$

Modified matter

Problem:

All the matter particles we know possess an effective interaction range that is much smaller than the cosmological scales

→ the effective pressure is always positive !

Solution:

add new forms of matter with strong interaction/self-interaction

→ the effective pressure can be large and negative

Dark Energy=scalar fields, generalized perfect fluids etc

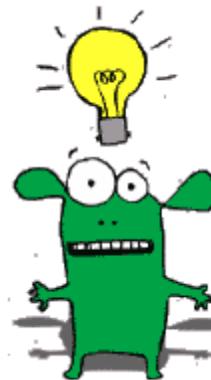
Modified gravity

Can we detect traces of modified gravity at $\left\{ \begin{array}{l} \text{background} \\ \text{linear} \\ \text{non-linear} \end{array} \right\}$ level ?

What is modified gravity ?

What is gravity ?

A universal force in 4D mediated by a massless tensor field



What is modified gravity ?

**A non-universal force in nD mediated by
(possibly massive) tensor, vector and scalar fields**

Cosmology and modified gravity



in laboratory

}

very limited time/space/energy scales;
only baryons



in the solar system



at astrophysical scales

complicated by non-linear/non-gravitational effects

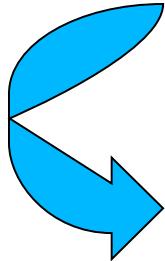


at cosmological scales

unlimited scales; mostly linear processes;
baryons, dark matter, dark energy !

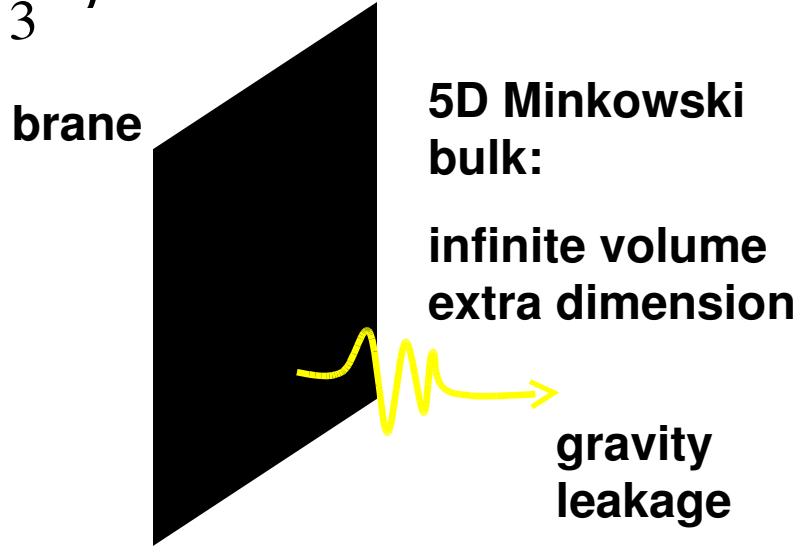
Simplest MG (I): DGP

(Dvali, Gabadadze, Porrati 2000)



$$S = \int d^5x \sqrt{-g^{(5)}} R^{(5)} + L \int d^4x \sqrt{-g} R$$

$$H^2 - \frac{H}{L} = \frac{8\pi G}{3} \rho$$



L = crossover scale:

$$r \ll L \Rightarrow V \propto \frac{1}{r}$$

$$r \gg L \Rightarrow V \propto \frac{1}{r^2}$$

- **5D gravity dominates at low energy/late times/large scales**
- **4D gravity recovered at high energy/early times/small scales**

Simplest MG (II): f(R)

Let's start with one of the simplest MG model: f(R)

$$\int dx^4 \sqrt{g} [f(R) + L_{matter}]$$

e.g higher order corrections

$$\int dx^4 \sqrt{g} (R + R^2 + R^3 + \dots)$$

- ✓ f(R) models are simple and self-contained (no need of potentials)
- ✓ easy to produce acceleration (first inflationary model)
- ✓ high-energy corrections to gravity likely to introduce higher-order terms
- ✓ particular case of scalar-tensor and extra-dimensional theory

Is this already ruled out by local gravity?

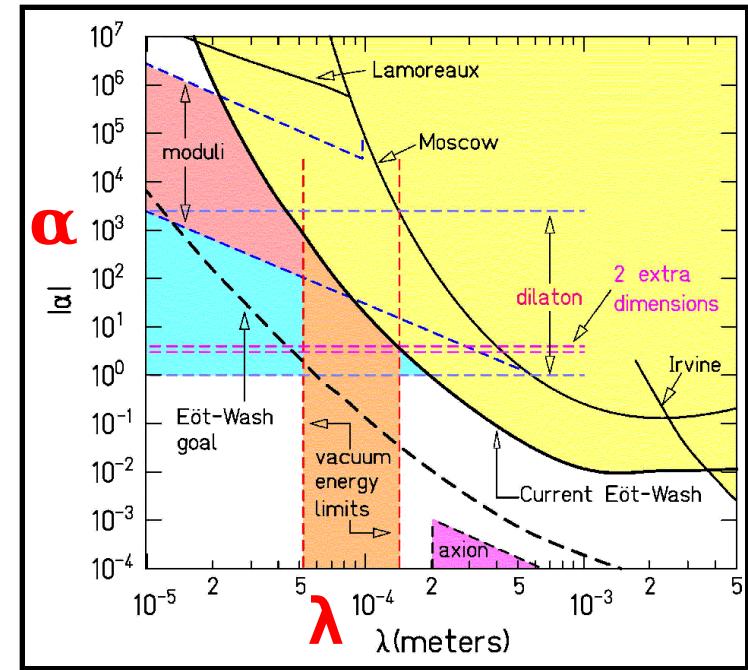
$$\int dx^4 \sqrt{g} (f(R) + L_{matter})$$

**is a scalar-tensor theory with Brans-Dicke parameter $\omega=0$ or
a coupled dark energy model with coupling $\beta=1/2$**

$$G^* = G\left(1 + \frac{4}{3}\beta^2 e^{-m_\phi r}\right) = G\left(1 + \alpha e^{-r/\lambda}\right)$$

$$m_\phi^2 = \frac{1}{f''} + \frac{Rf' - 4f}{f'^2} \rightarrow \frac{1}{f''}$$

(on a local minimum)



The simplest case

$$\int dx^4 \sqrt{g} \left(R - \frac{\mu^4}{R} + L_{matter} \right)$$

Turner, Carroll, Capozziello
etc. 2003

In Einstein Frame

$$\hat{g}_{\mu\nu} = (f')^2 g_{\mu\nu}$$

$$\begin{aligned}\ddot{\phi} + 3H\dot{\phi} + V(\phi)' &= \frac{\sqrt{3}}{2} \beta \rho_m \\ \dot{\phi} + 3H\phi + V(\phi)' &= 0\end{aligned}$$

$$V(\phi)' = \frac{fR - f'}{f'^2}$$

$$\dot{\rho}_m + 3H\rho_m = -\frac{\sqrt{3}}{2} \beta \dot{\phi} \rho_m$$

$$\phi = \log f'$$

$$\beta = 1/2$$

R-1/R model : the ϕ MDE

$$\ddot{\phi} + 3H\dot{\phi} + V(\phi)' = \frac{\sqrt{3}}{2} \beta \rho_m$$

$$\dot{\rho}_m + 3H\rho_m = -\frac{\sqrt{3}}{2} \beta \dot{\phi} \rho_m$$

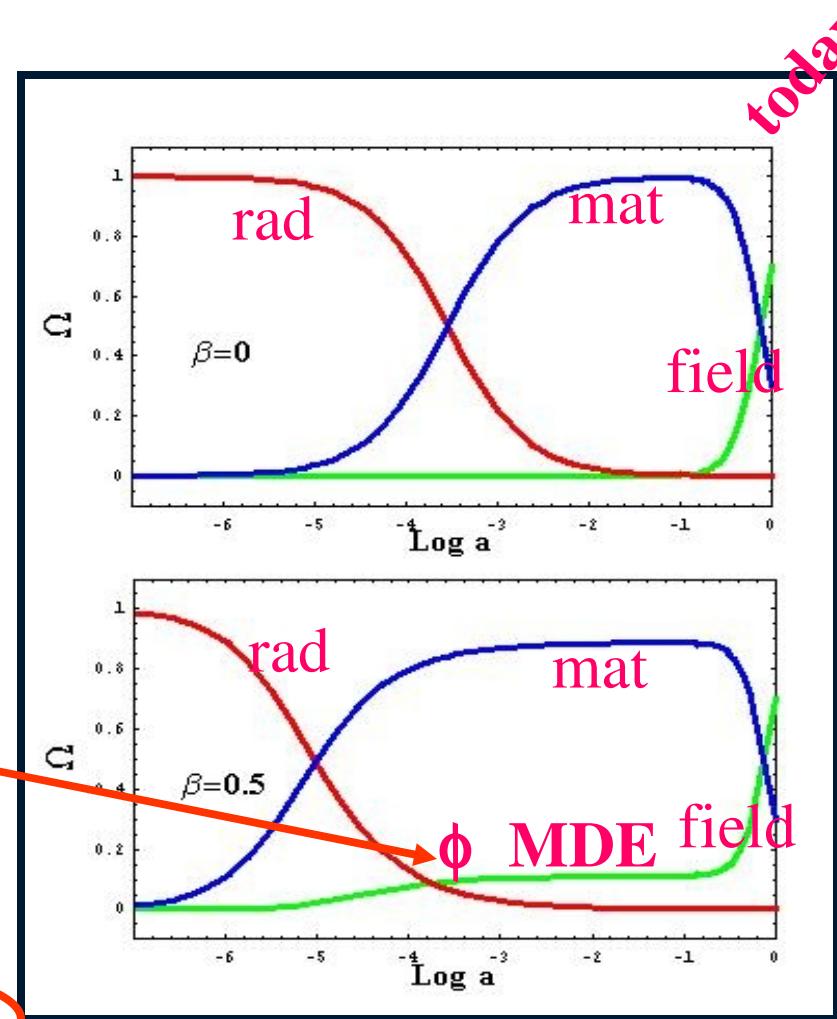
$$H^2 = \frac{8\pi}{3} (\rho_m + \rho_\phi)$$

$$\beta = 1/2$$

$$\Omega_\phi = 1/9$$

In Jordan frame: $a = t^{1/2}$

instead of $a = t^{2/3}$!!



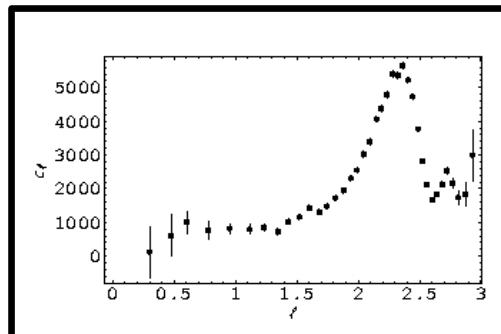
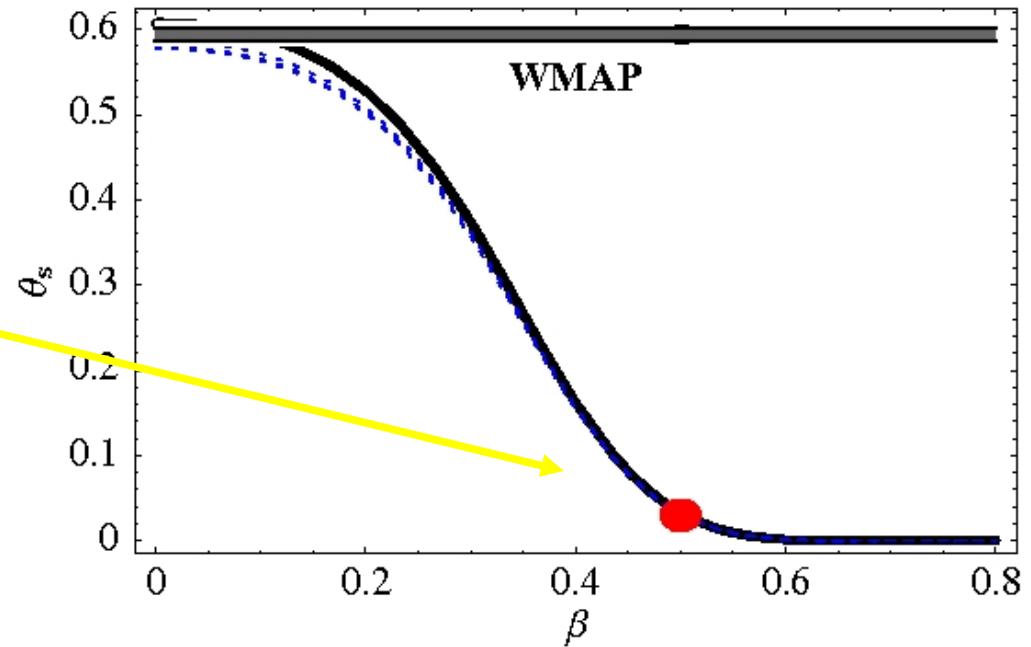
Caution:
Plots in the
Einstein frame!

Sound horizon in R+Rⁿ model

$$a = t^{1/2}$$

$$w_{eff} = 1/3$$

$$\theta = \int_{z_{dec}}^{\infty} \frac{c_s dz}{H(z)} / \int_0^{z_{dec}} \frac{dz}{H(z)}$$



008

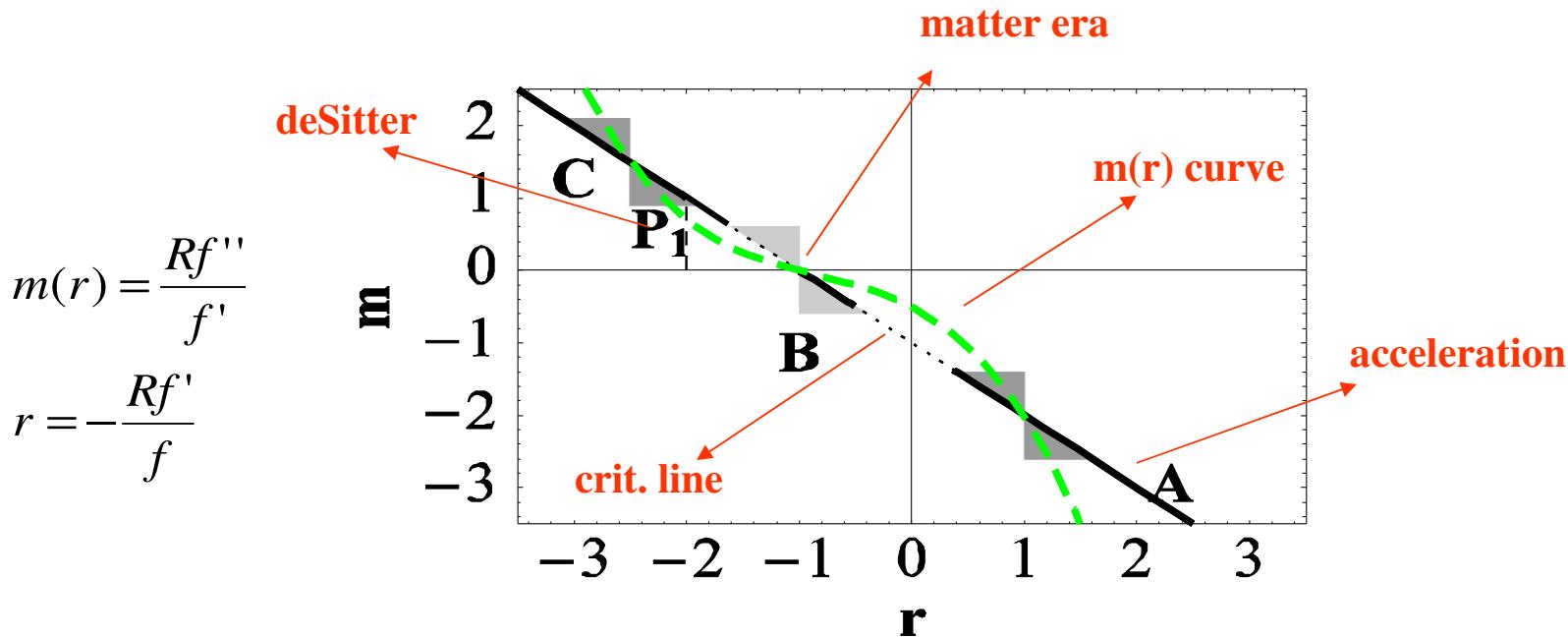
L.A., D. Polarski, S. Tsujikawa, PRL 98, 131302,
astro-ph/0603173

A recipe to modify gravity

Can we find $f(R)$ models that work?

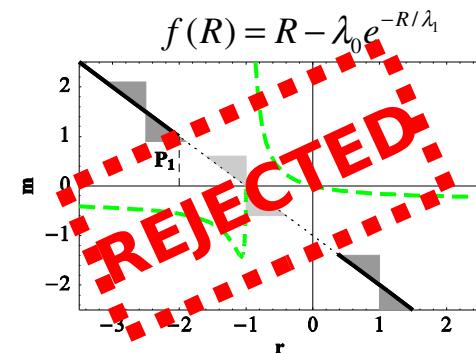
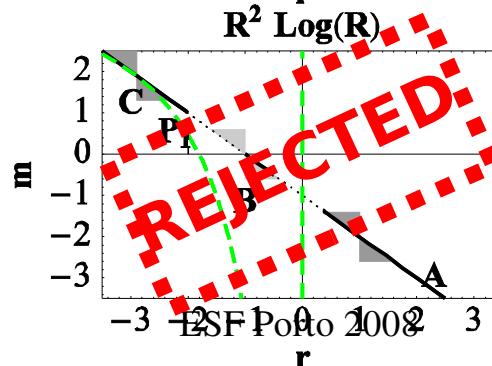
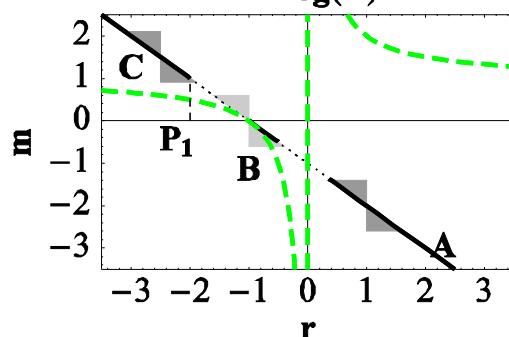
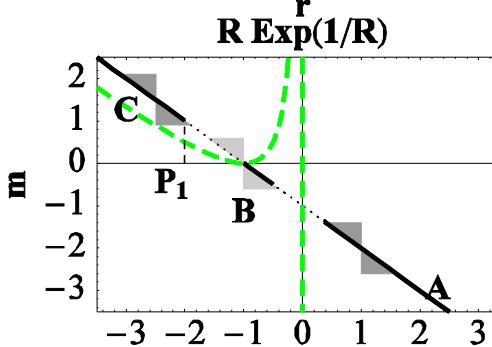
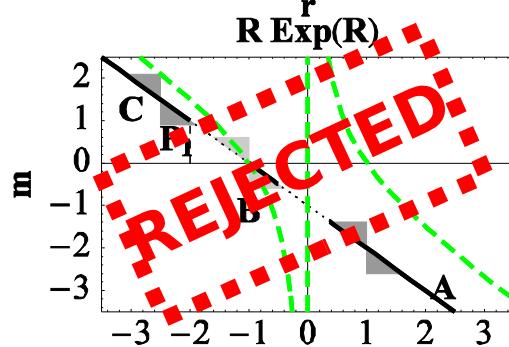
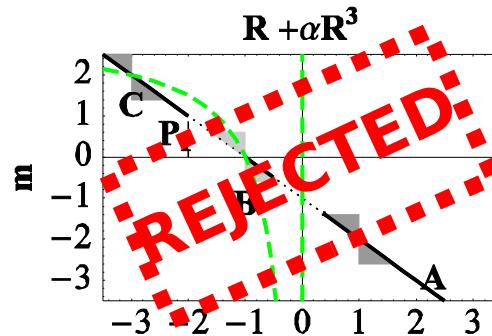
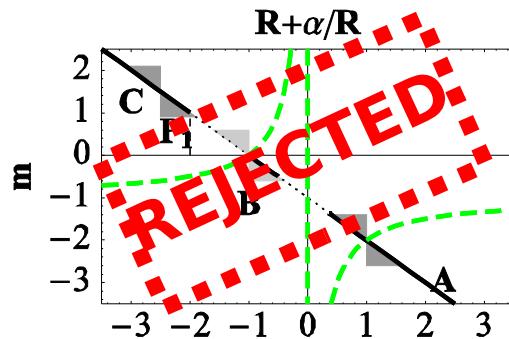
The m,r plane

The qualitative behavior of any $f(R)$ model can be understood by looking at the geometrical properties of the m,r plot



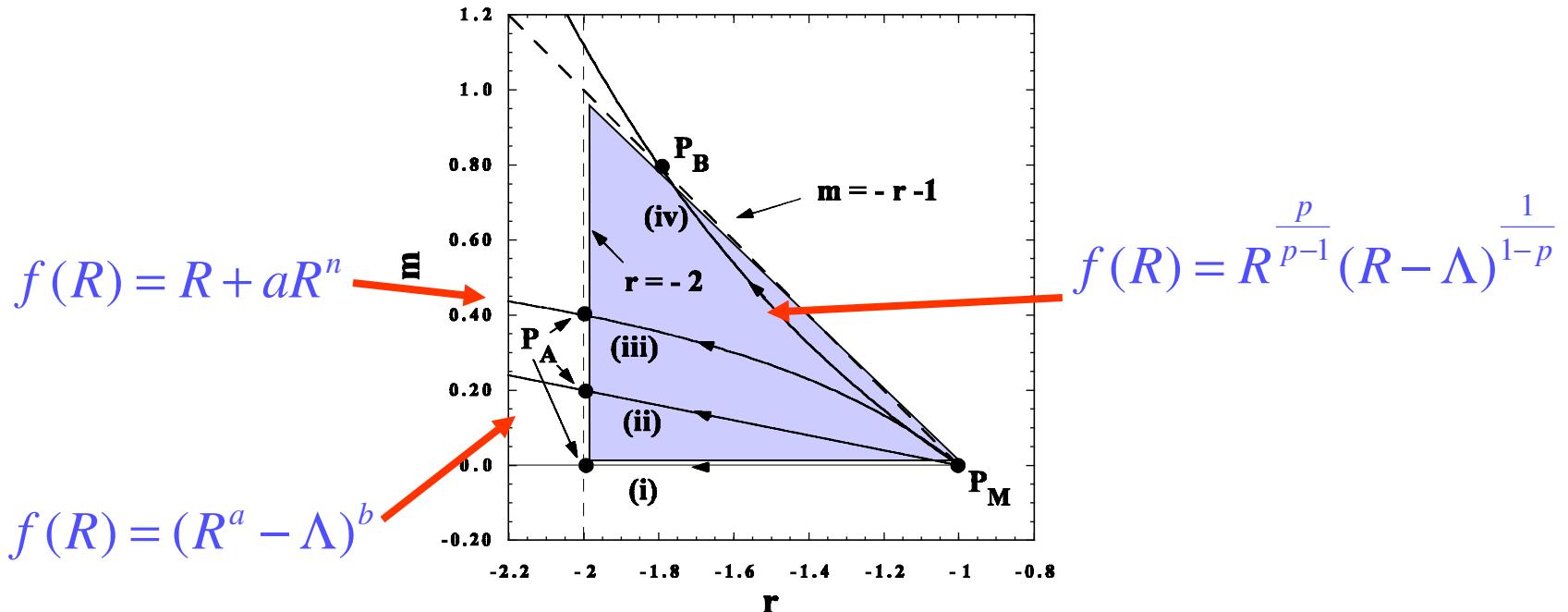
The dynamics becomes 1-dimensional !

The power of the $m(r)$ method



The triangle of viable trajectories

There exist only two kinds of cosmologically viable trajectories



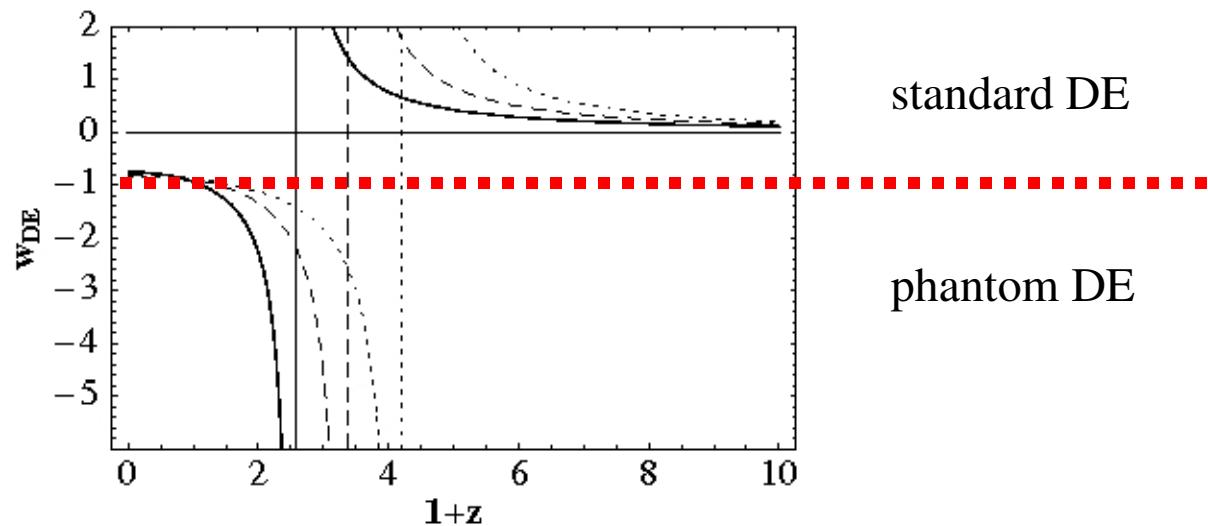
Notice that in the triangle $m > 0$

A theorem on phantom crossing

Theorem: for all **viable** $f(R)$ models

- there is a phantom crossing of w_{DE}
- there is a singularity of w_{DE}
- both occur typically at low z when $\Omega_m \rightarrow 1$

$$f(R) = (R^a - \Lambda)^b$$



L.A., S. Tsujikawa, 2007

Local Gravity Constraints are very tight

Depending on the local field configuration

$$m(R_s) = \frac{R_s f_s''}{f_s'} \ll 10^{-23} \div 10^{-6}$$

depending on the experiment: laboratory, solar system, galaxy

see eg. Nojiri & Odintsov 2003; Brookfield et al. 2006
Navarro & Van Acoyelen 2006; Faraoni 2006; Bean et al. 2006;
Chiba et al. 2006; Hu, Sawicky 2007;....

LGC+Cosmology

Take for instance the Λ CDM clone

$$f(R) = (R^a - \Lambda)^b$$

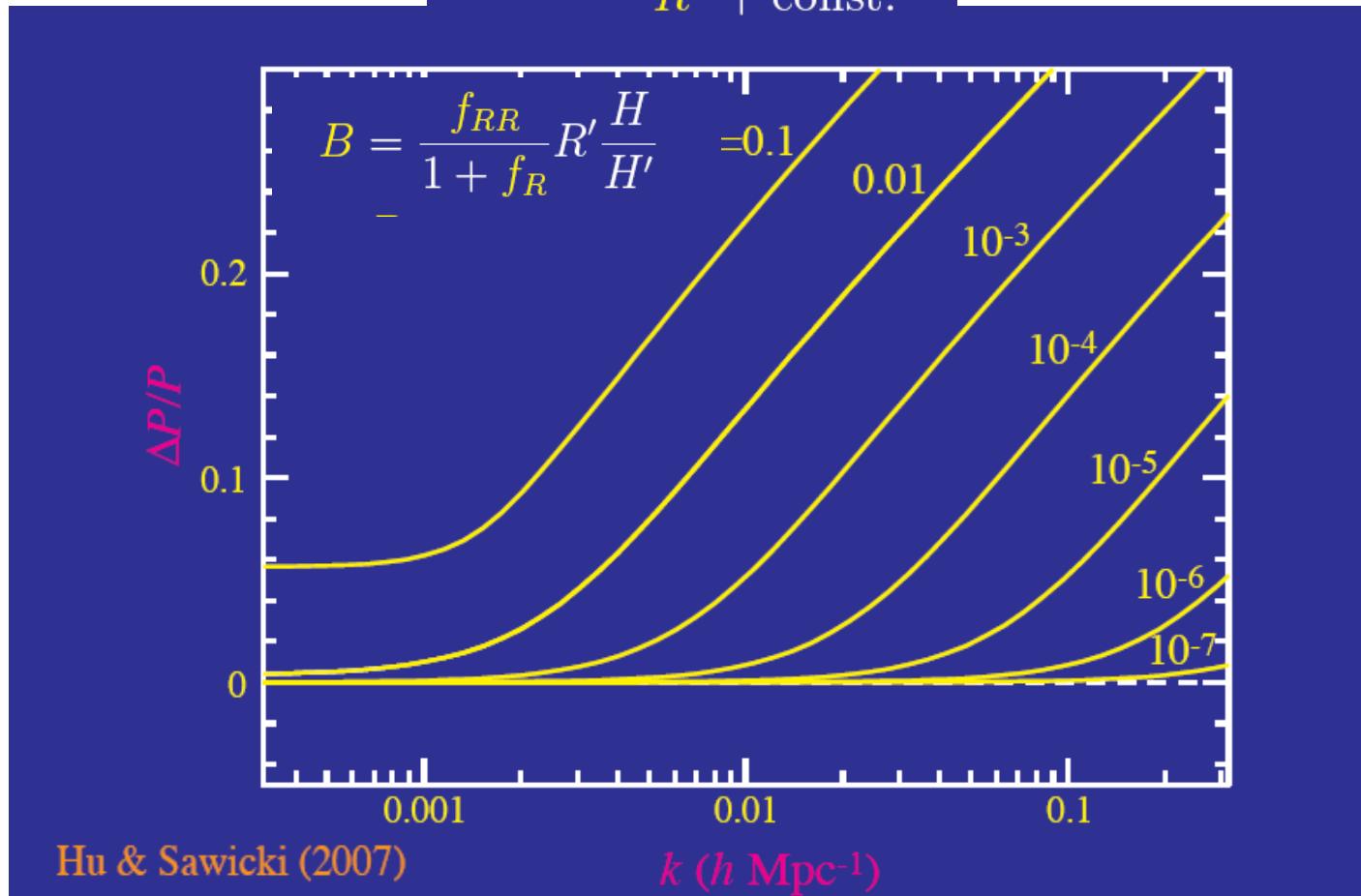
Applying the criteria of
LGC and Cosmology

$$a \approx b \approx 1 \pm 10^{-23}$$

i.e. Λ CDM to an incredible precision

However. . . perturbations

$$f(R) \propto \frac{R^n}{R^n + \text{const.}}$$



MG at the linear level

$$ds^2 = a^2[(1+2\phi)dt^2 - (1-2\psi)(dx^2 + dy^2 + dz^2)]$$

At the linear perturbation level and sub-horizon scales, a modified gravity model will

- modify Poisson's equation

$$k^2\phi = -4\pi G a^2 Q(k, a) \rho_m \delta_m$$

- induce an anisotropic stress

$$\eta(k, a) = \frac{\phi - \psi}{\psi}$$

- modify the growth of perturbations

$$\delta_k'' + (1 + \frac{H'}{H})\delta_k' - 4\pi G Q(k, a) \rho \delta = 0$$

MG at the linear level

| | | |
|------------------------|---|---|
| ▪ standard gravity | $Q(k, a) = 1$ $\eta(k, a) = 0$ | |
| ▪ scalar-tensor models | $Q(a) = \frac{G^*}{FG_{cav,0}} \frac{2(F + F'^2)}{2F + 3F'^2}$ $\eta(a) = \frac{F'^2}{F + F'^2}$ | Boisseau et al. 2000 Acquaviva et al. 2004 Schimd et al. 2004 L.A., Kunz & Sapone 2007 |
| ▪ $f(R)$ | $Q(a) = \frac{G^*}{FG_{cav,0}} \frac{1+4m\frac{k^2}{a^2R}}{1+3m\frac{k^2}{a^2R}}, \quad \eta(a) = \frac{m\frac{k^2}{a^2R}}{1+2m\frac{k^2}{a^2R}}$ | Bean et al. 2006 Hu et al. 2006 Tsujikawa 2007 |
| ▪ DGP | $Q(a) = 1 - \frac{1}{3\beta}; \quad \beta = 1 + 2Hr_c w_{DE}$ $\eta(a) = \frac{2}{3\beta - 1}$ | Lue et al. 2004; Koyama et al. 2006 |
| ▪ coupled Gauss-Bonnet | $Q(a) = \dots$ $\eta(a) = \dots$ | see L. A., C. Charmousis, S. Davis 2006 |

Growth of fluctuations as a measure of modified gravity

$$\delta_k'' + \left(1 + \frac{H'}{H}\right)\delta_k' - 4\pi G Q(k, a)\rho \delta = 0$$



good fit

$$\frac{d \log \delta}{d \log a} = \Omega_m(a)^\gamma$$

Peebles 1980
Lahav et al. 1991
Wang et al. 1999
Bernardeau 2002
L.A. 2004
Linder 2006

Instead of

$$Q(k, a)$$

we parametrize

$$\gamma = \text{const}$$

LCDM

$$\gamma = 0.55$$

DE

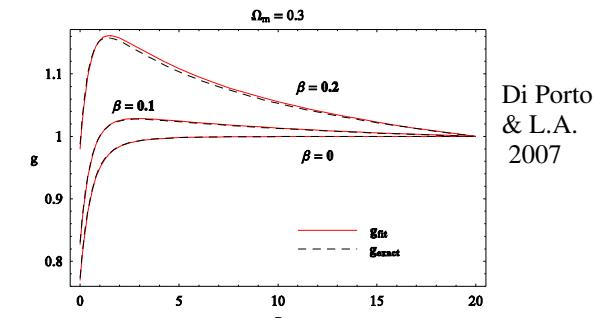
$$\gamma = 0.55[1 + 0.05(w+1)]$$

DGP

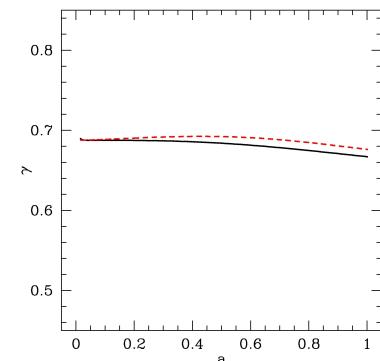
$$\gamma = 0.67$$

ST

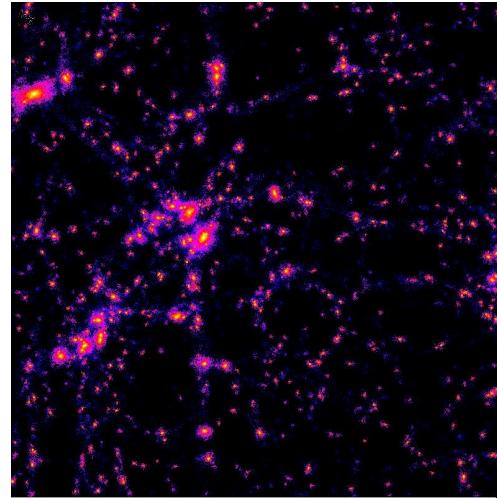
$$\Omega_m^\gamma (1 + 0.5\beta^2)$$



$\gamma \neq 0.55$ is an indication of modified gravity

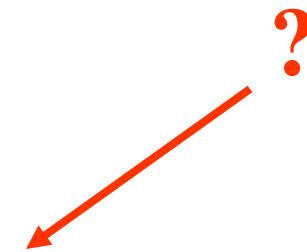


Two MG observables



Correlation of galaxy positions:
galaxy clustering

$$P_{gal}(k, z) = b^2 P_{matt}(k, z) \propto \Psi^2$$

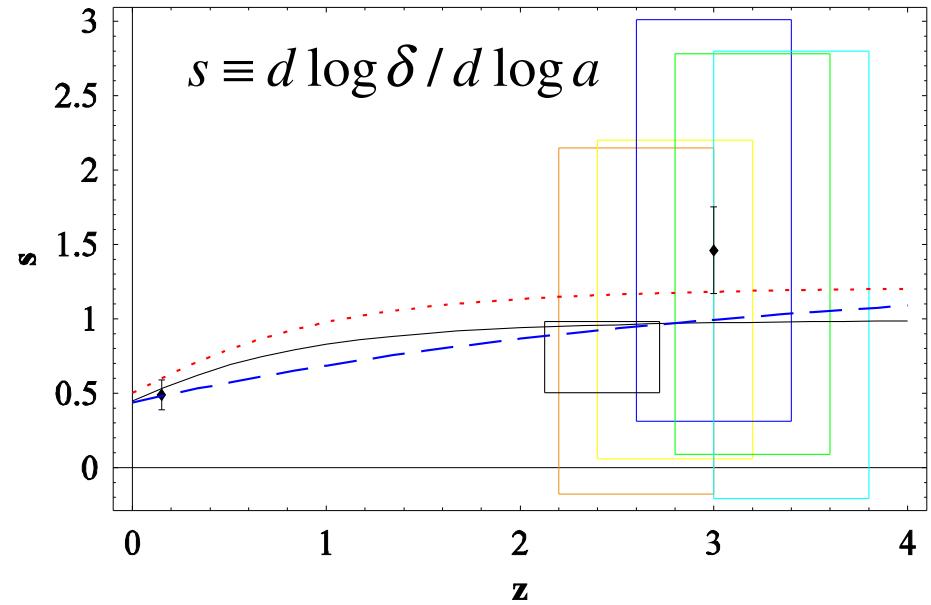


Correlation of galaxy ellipticities:
galaxy weak lensing

$$P_{ellipt}(k, z) \propto (\Phi + \Psi)^2$$

Present constraints on gamma

| z | s |
|------------|-----------------|
| ref. [23] | |
| 2.125-2.72 | 0.74 ± 0.24 |
| ref. [25] | |
| 2.2 - 3 | 0.99 ± 1.16 |
| 2.4 - 3.2 | 1.13 ± 1.07 |
| 2.6 - 3.4 | 1.66 ± 1.35 |
| 2.8 - 3.6 | 1.43 ± 1.34 |
| 3 - 3.8 | 1.30 ± 1.50 |
| ref. [24] | |
| 3 | 1.46 ± 0.29 |
| ref. [27] | |
| 0.15 | 0.49 ± 0.10 |

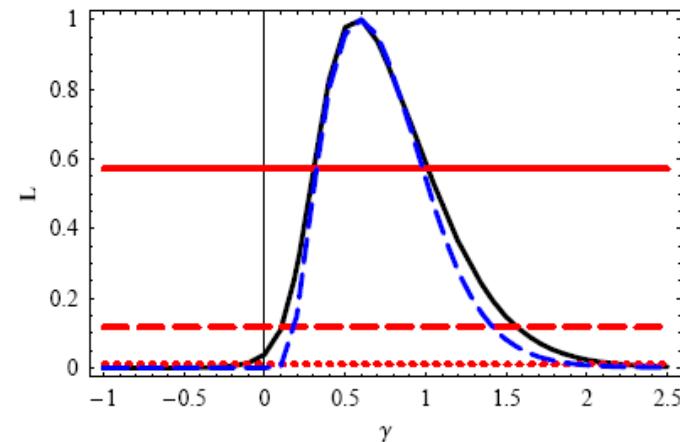
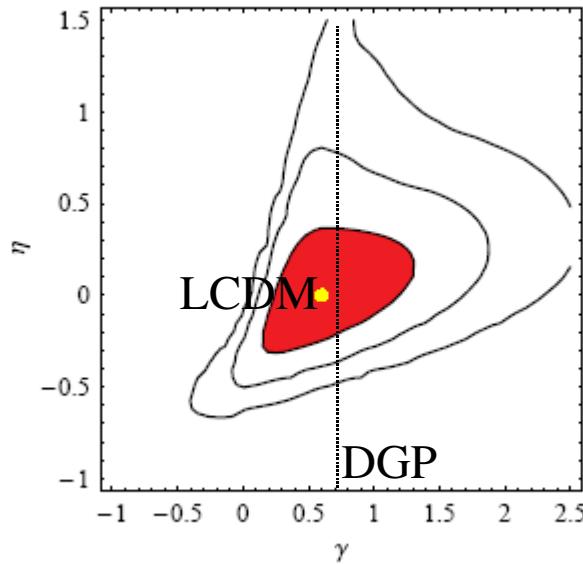


We consider the following data: *a*) Lyman- α power spectra at an average redshift $z = 2.125$, $z = 2.72$ [23], $z = 3$ [24]; *b*) the normalization σ_8 inferred from Lyman- α at z ranging between 2 and 3.8 [25]; *c*) galaxy power spectra at low z from SDSS [26] and 2dF [27]. From the three Lyman- α and the SDSS spectra we estimate the ratios

Viel et al. 2004,2006; McDonald et al. 2004; Tegmark et al. 2004

Present constraints on gamma

$$s_{fit} \equiv \Omega_m^\gamma (1 + \eta)$$



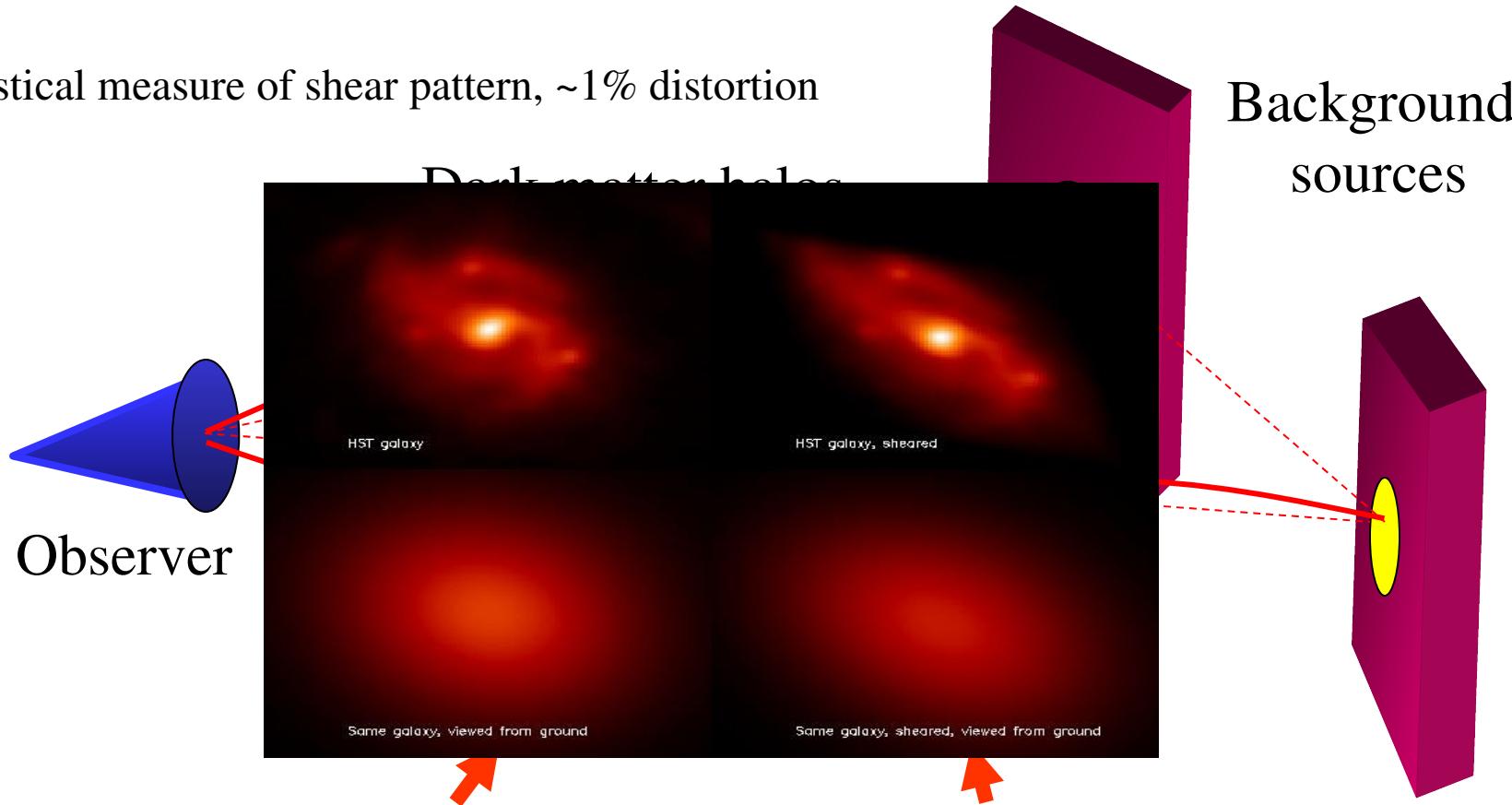
| | 1σ | 2σ | 3σ |
|---------------------|------------------------|------------------------|------------------------|
| η | $0.00^{+0.28}_{-0.18}$ | $+0.58^{+1.1}_{-0.38}$ | $-0.58^{+1.1}_{-0.58}$ |
| γ | $0.60^{+0.41}_{-0.30}$ | $+0.97^{+1.6}_{-0.49}$ | $-0.74^{+1.6}_{-0.74}$ |
| $\gamma_{standard}$ | $0.60^{+0.34}_{-0.26}$ | $+0.77^{+1.4}_{-0.40}$ | $-0.50^{+1.4}_{-0.50}$ |

C. Di Porto & L.A. 2007

ESF Porto 2008

Probing gravity with weak lensing

Statistical measure of shear pattern, ~1% distortion



Radial distances depend on
geometry of Universe

Foreground mass distribution depends on
growth/distribution of structure

Probing gravity with weak lensing

In General Relativity, lensing is caused by the “lensing potential”

$$\Phi = \phi + \psi$$

and this is related to the matter perturbations via Poisson’s equation.
Therefore the lensing signal depends on two modified gravity functions

$$\begin{cases} \Sigma = Q(1 + \frac{\eta}{2}) \\ \eta(k, a) \end{cases}$$

in the WL power spectrum 

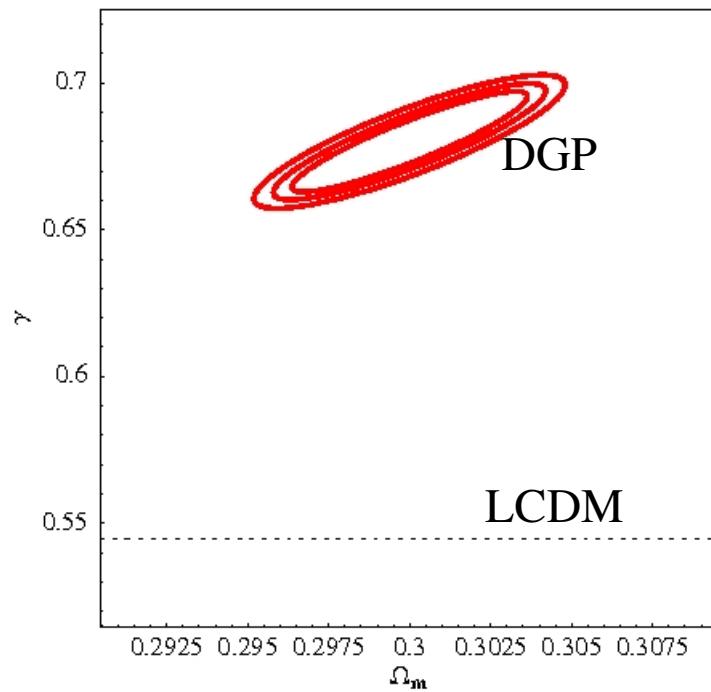
$$P_{ell}(\ell) = \int dz F(z; \Omega_{m, \Lambda, etc}) Q(1 + \frac{\eta}{2}) P_m(z, k = \frac{H_0 \ell}{r(z)})$$

and in the growth function 

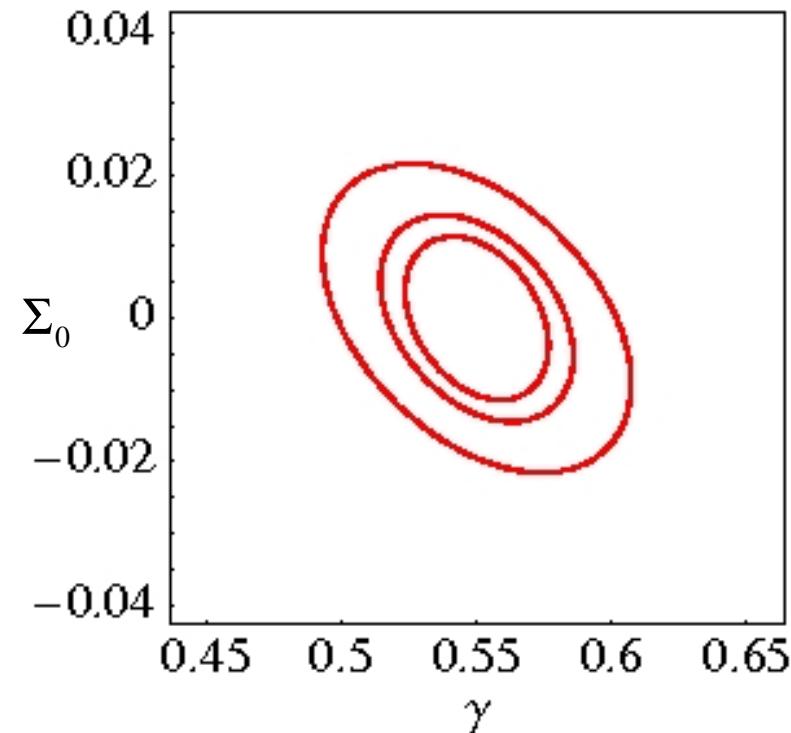
$$P_m(z, k) = D(z, Q)^2 P_m(z = 0, k)$$

Weak lensing measures Dark Gravity

DGP ($\Sigma_0 = 0$)



Phenomenological DE

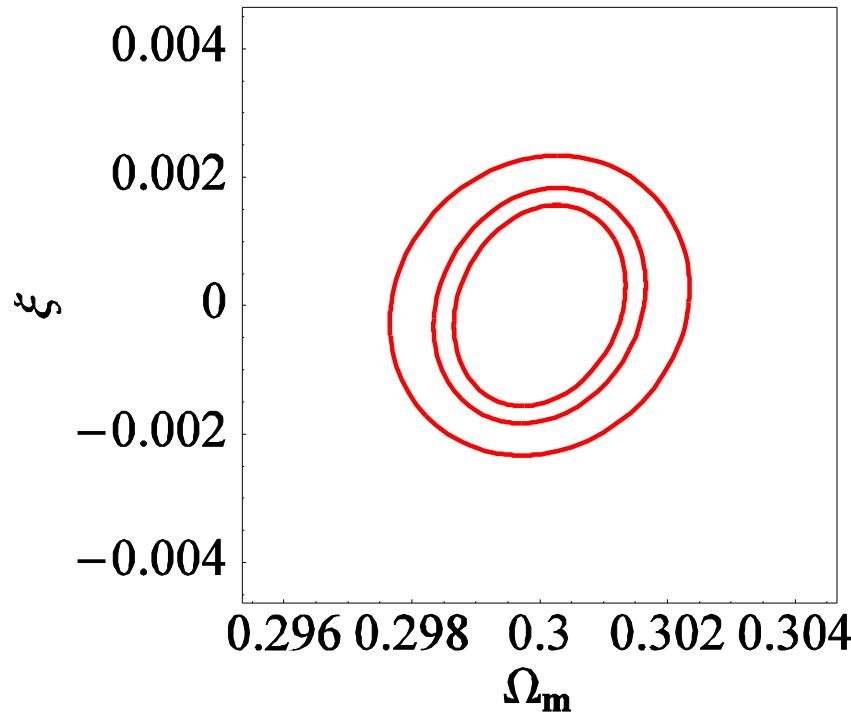


Weak lensing tomography over half sky

L.A., M. Kunz, D. Sapone
arXiv:0704.2421

Weak lensing measures Dark Gravity

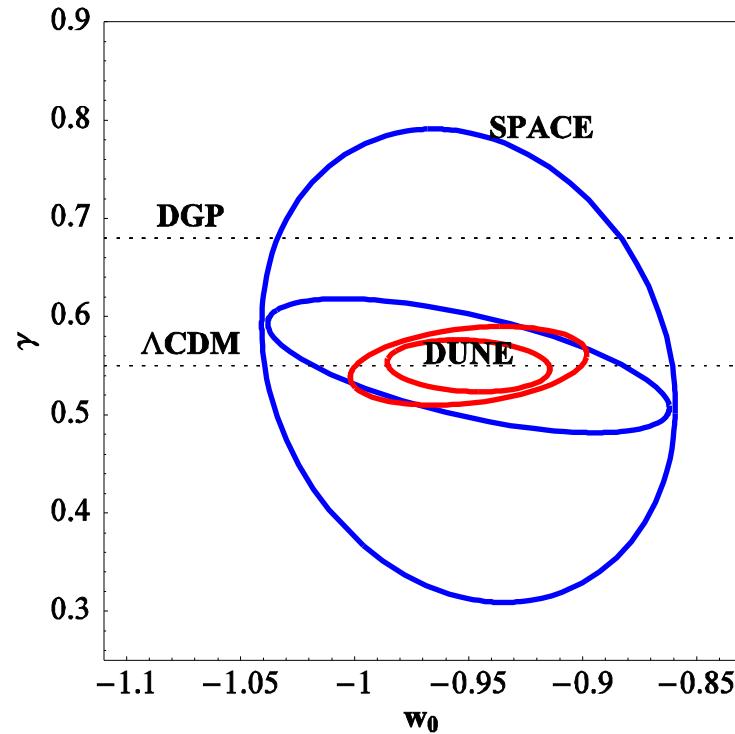
scalar-tensor model $(1 + \frac{1}{2} \xi \dot{\phi})R$



Weak lensing tomography over half sky

V. Acquaviva, L.A., C.
Baccigalupi, in prep.

Comparing BAO with WL

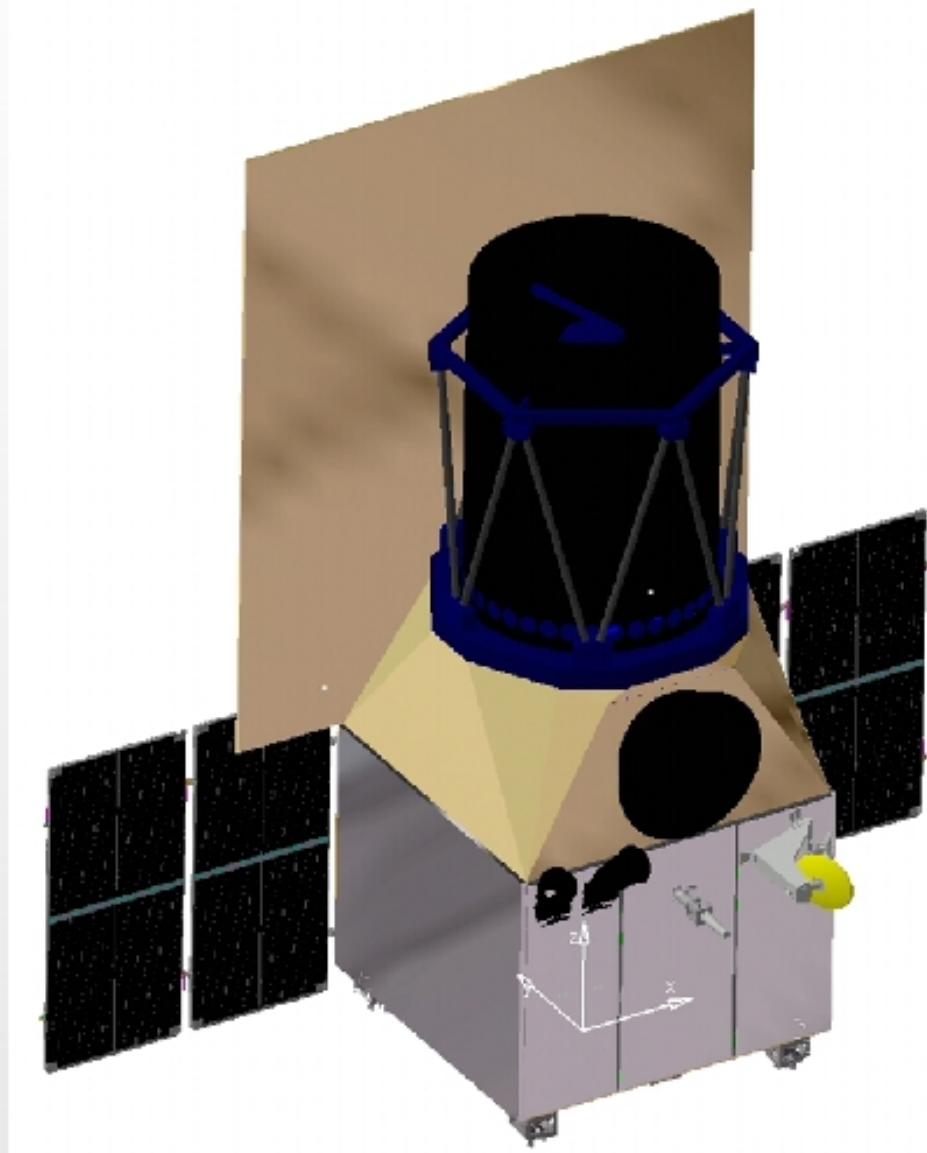


Weak lensing/ BAO over half sky

Dark Universe Explorer



- 1.2m telescope
- FOV 0.5 deg^2
- PSF FWHM $0.23''$
- Weak Lensing Survey:
 - $20,000 \text{ deg}^2$
 - 1 Broad band
 - $35 \text{ Galaxies/arcmin}^2$
 - median $z \sim 1$
 - Ground based Photo-z
- Super Novae Survey:
 - $2 \times 60 \text{ deg}^2$
 - Observed every 4 days for 9 months
 - 6 Bands
 - $10,000 \text{ SNe}$
 - Out to $z \sim 1$



Conclusions: the teachings of DE

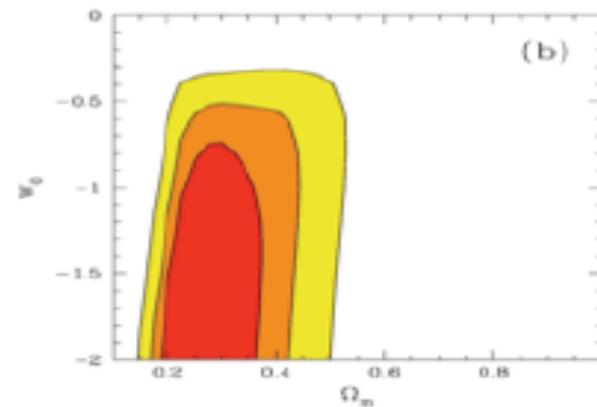
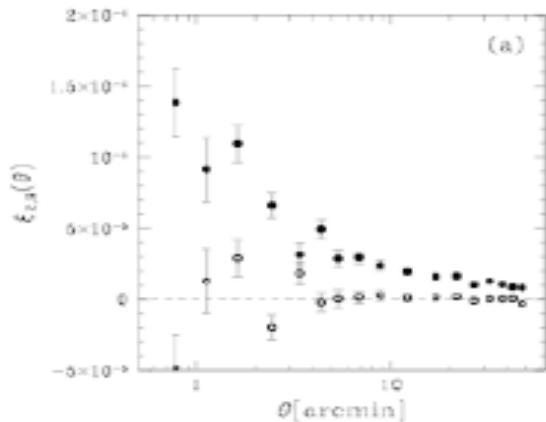
- There is much more than meets the eyes in the Universe
- Two solutions to the DE mismatch: either add “dark energy” or “dark gravity”
- New MG parameters: γ, Σ
- The high precision data of present and near-future observations allow to test for dark energy/gravity
- It is crucial to combine background and perturbations
- Weak Lensing with DUNE is a good bet...

Current Observational Status: CFHTLS

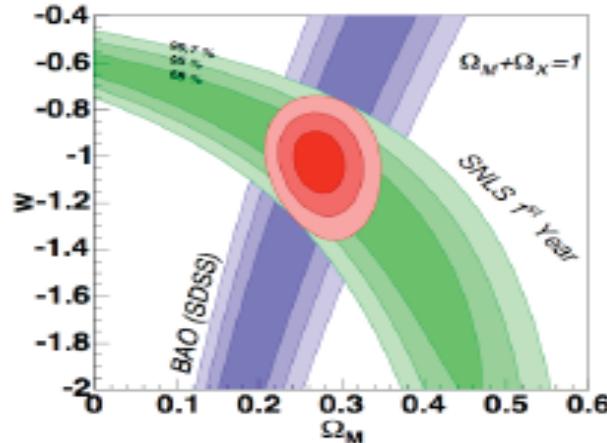
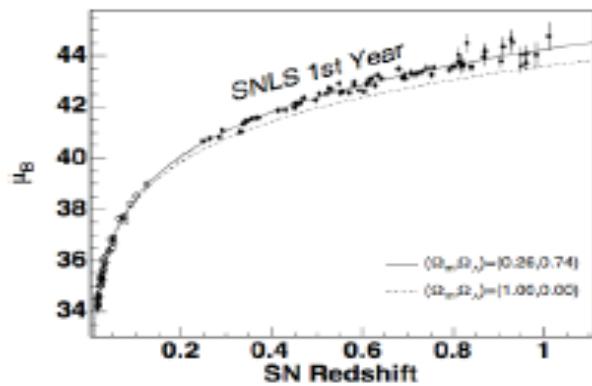
Hoekstra et al. 2005
Semboloni et al. 2005

Weak
Lensing

First results
From CFHT
Legacy
Survey with
Megacam



($w = \text{constant}$
and other
priors
assumed)



Type Ia
Super-
novae