



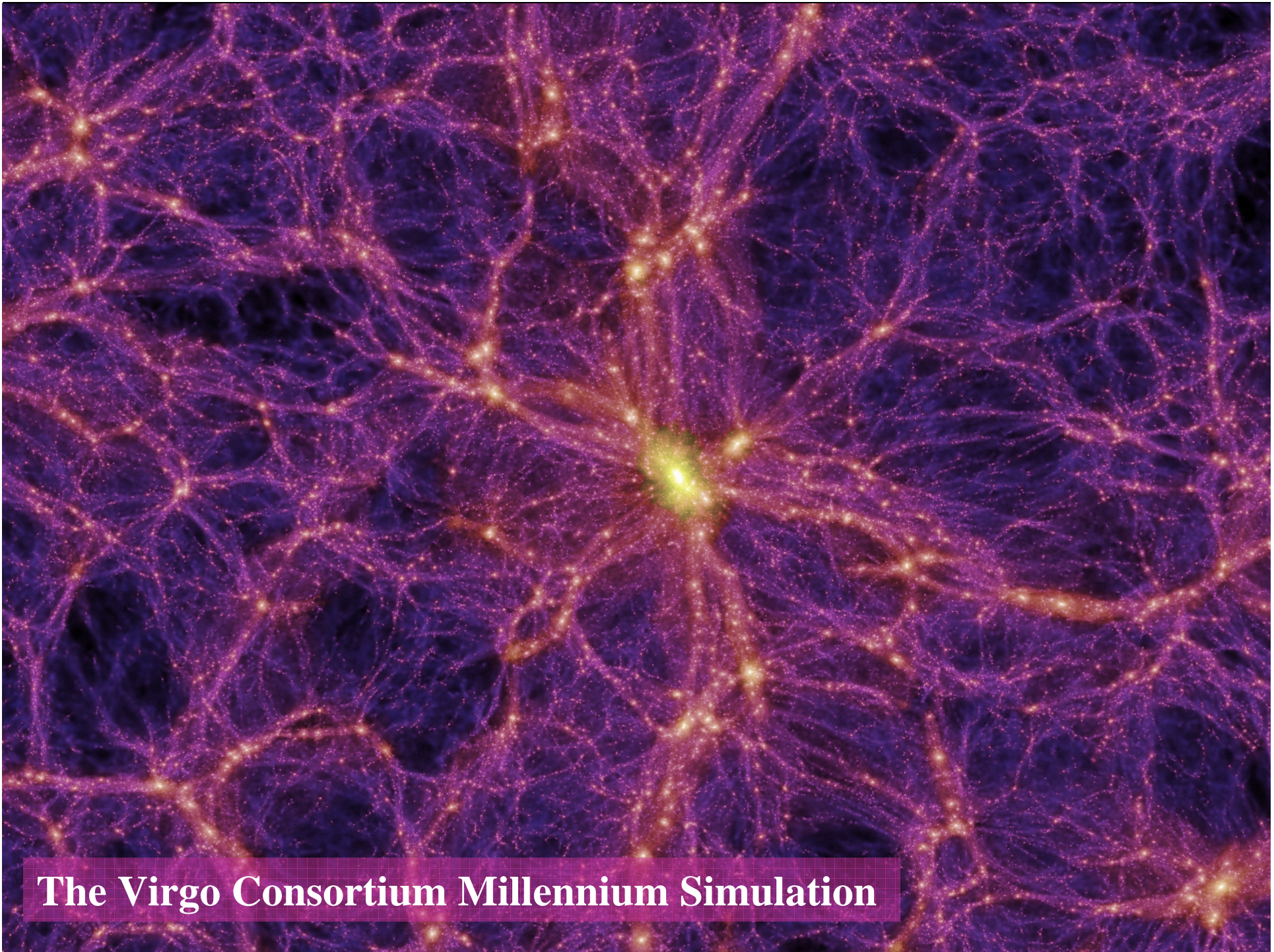
Probing the Universe with Cosmological Lensing

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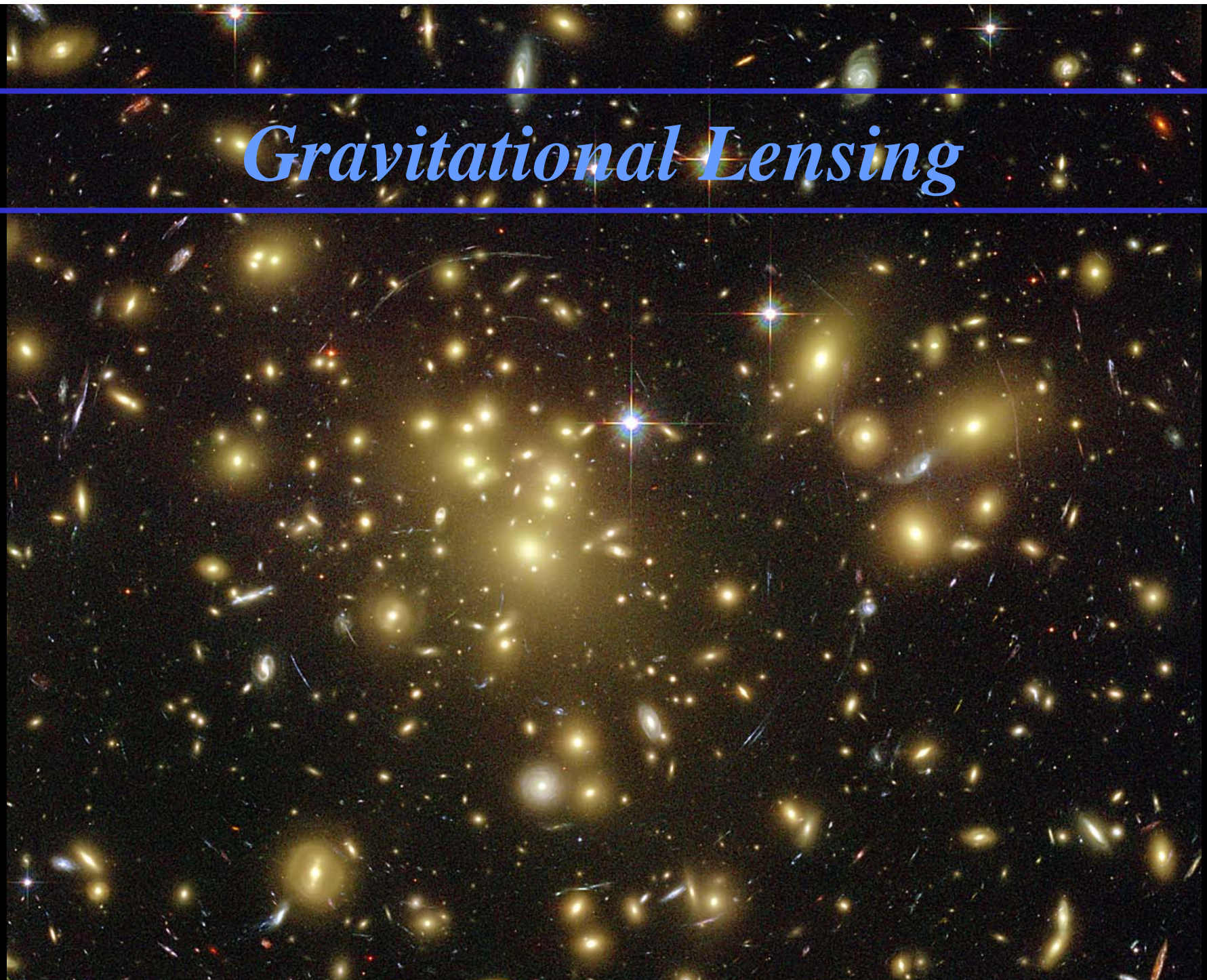
Acknowledgements

- David Bacon (Portsmouth)
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- Patrick Simon (Edinburgh)
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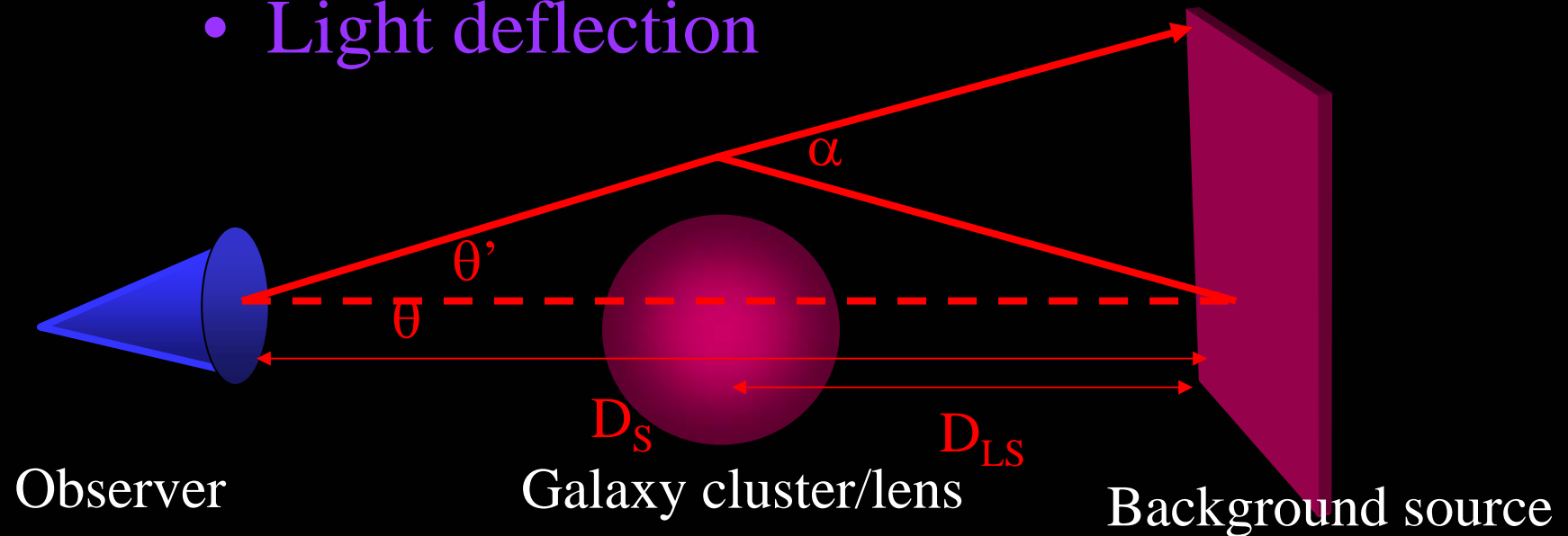
The Virgo Consortium Millennium Simulation

Gravitational Lensing



Basics of Gravitational Lensing

- Light deflection



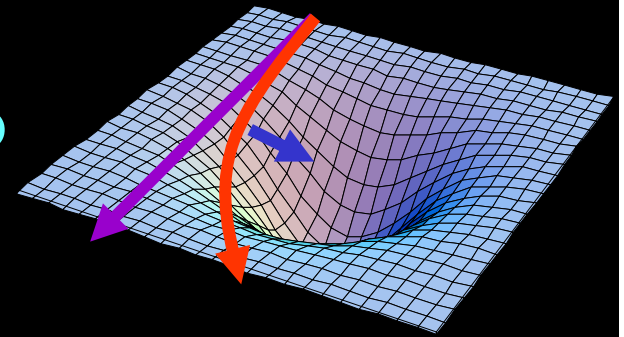
- Lens equation

$$\theta' = \theta + \frac{D_{LS}}{D_S} \alpha(\theta)$$

Basics of Gravitational Lensing

- Relativistic equation of motion

$$\underline{\ddot{\alpha}} = \frac{d}{d\underline{\eta}} r^2 \frac{d}{d\underline{\eta}} \underline{\alpha} = -2 \frac{\partial}{\partial \underline{\theta}} \Phi$$



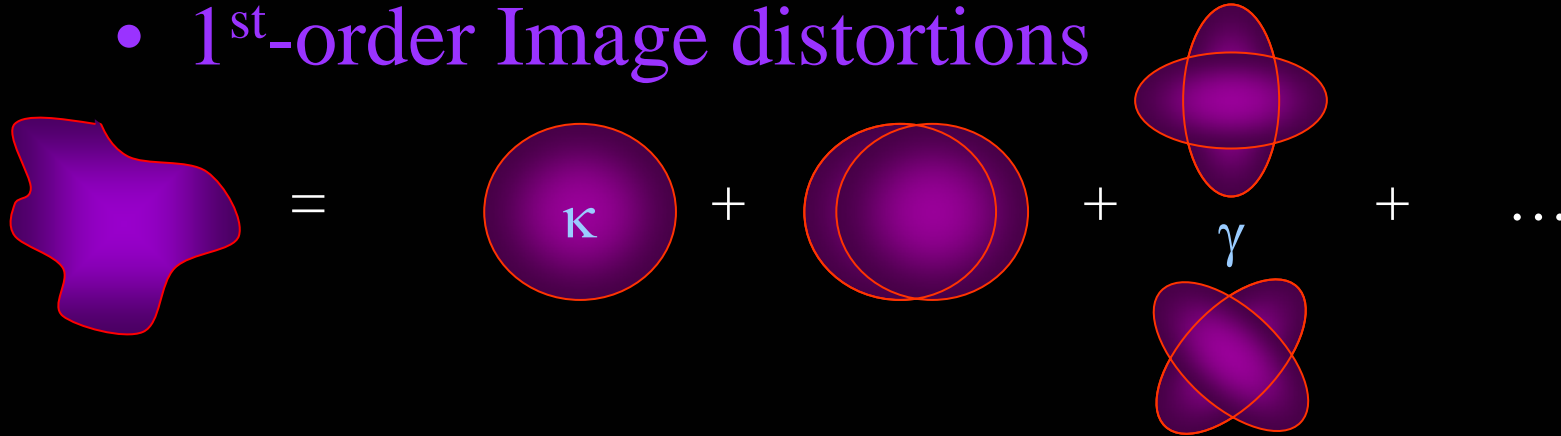
- Solve equation of motion ($\eta=r$):

$$\underline{\alpha} = \frac{\partial}{\partial \underline{\theta}} \phi, \quad \phi = 2 \int_0^r dr' \frac{r - r'}{rr'} \Phi(r', \underline{\theta})$$

Lensing potential

Basics of Gravitational Lensing

- 1st-order Image distortions



$$\Delta\theta_i' = \left(\frac{\partial\theta_i'}{\partial\theta_j} \right) \Delta\theta_j = \left[\delta_{ij}^K - \partial_i\partial_j\phi \right] \Delta\theta_j = \left[(1 - \kappa)\delta_{ij} - \gamma_{ij} \right] \Delta\theta_j$$

Convergence: $\kappa = \frac{1}{2} \partial^2\phi \propto \int_0^r dr' \delta\rho_m(\mathbf{r}')$ Surface mass density

Shear: $\gamma_{ij} = \partial_i\partial_j\phi - \frac{1}{2}\delta_{ij}\partial^2\phi = \begin{pmatrix} \gamma_1 & \gamma_2 \\ \gamma_2 & -\gamma_1 \end{pmatrix}$

Gravitational Lens Distortions

- Galaxy ellipticity, e :
- Lensing effect:

$$e' = e + \gamma$$

- On average $\langle e \rangle = 0$,
so $\langle e' \rangle = \gamma$.



- Shear matrix:

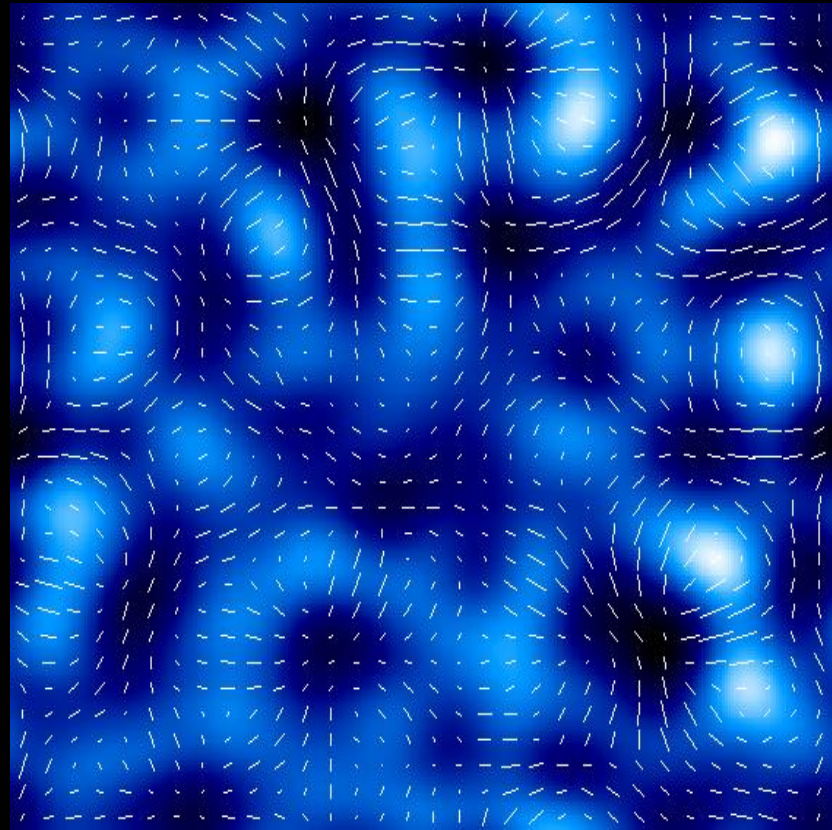
$$\gamma = \begin{matrix} \text{purple cross} \\ \gamma_1 \end{matrix} + i \begin{matrix} \text{purple cross} \\ \gamma_2 \end{matrix}$$

Mapping the Dark Matter

- From shear to surface density:

Kaiser-Squires (1993)

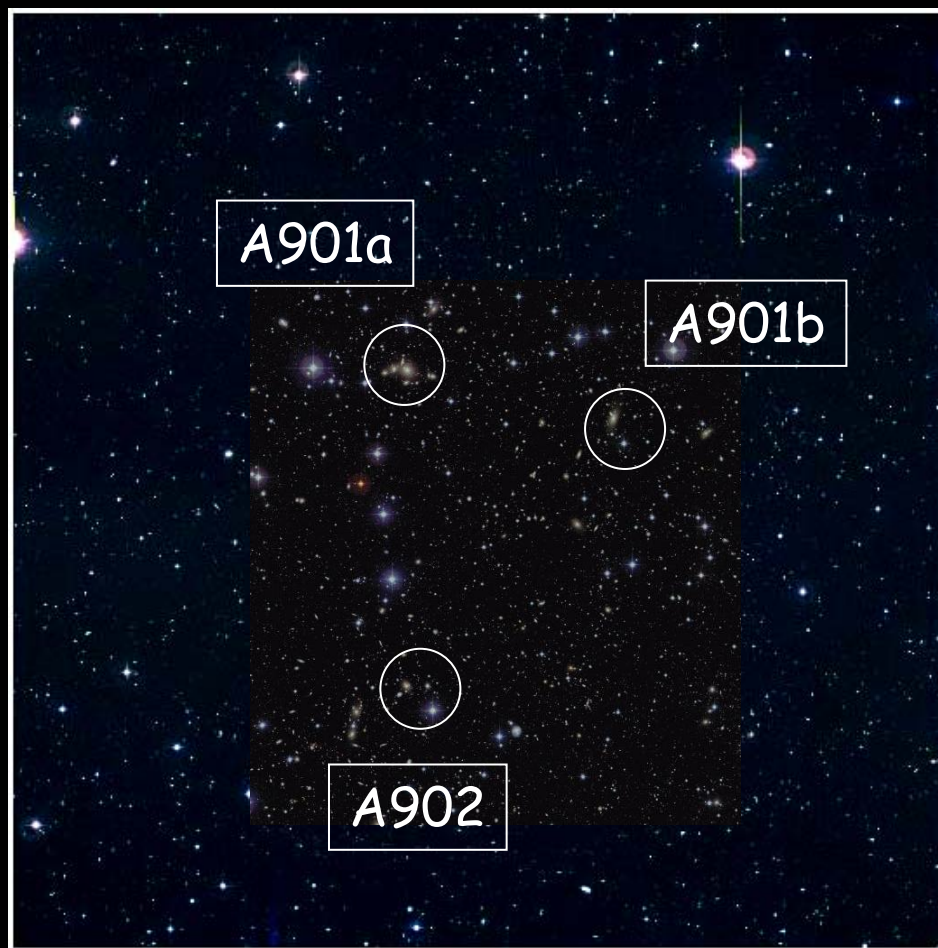
$$\kappa = \partial^{-2} \partial_i \partial_j \gamma_{ij}$$



Supercluster Abell 901/2

1/2 deg

3Mpc/h

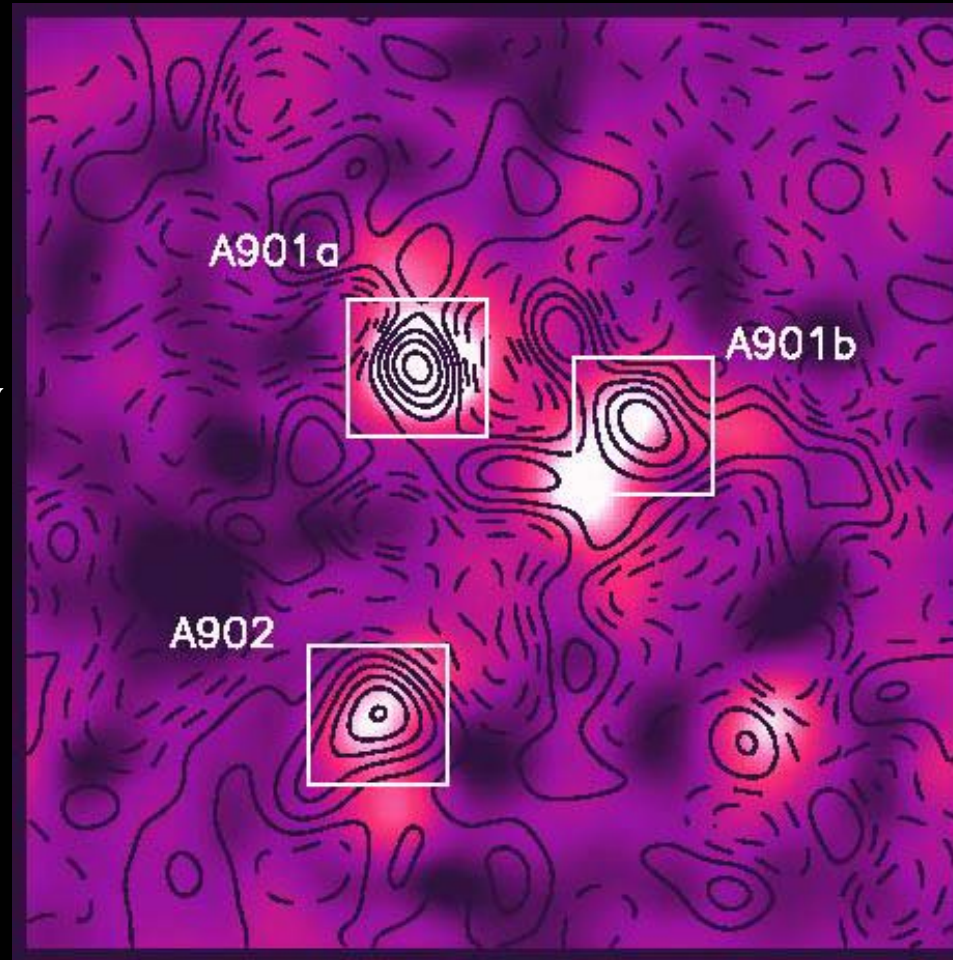


- $z=0.16$
- $\Delta z=0.01$

Mass and light in Supercluster A901/2

Dark Matter
contours, κ .

Elliptical galaxy
light shading.



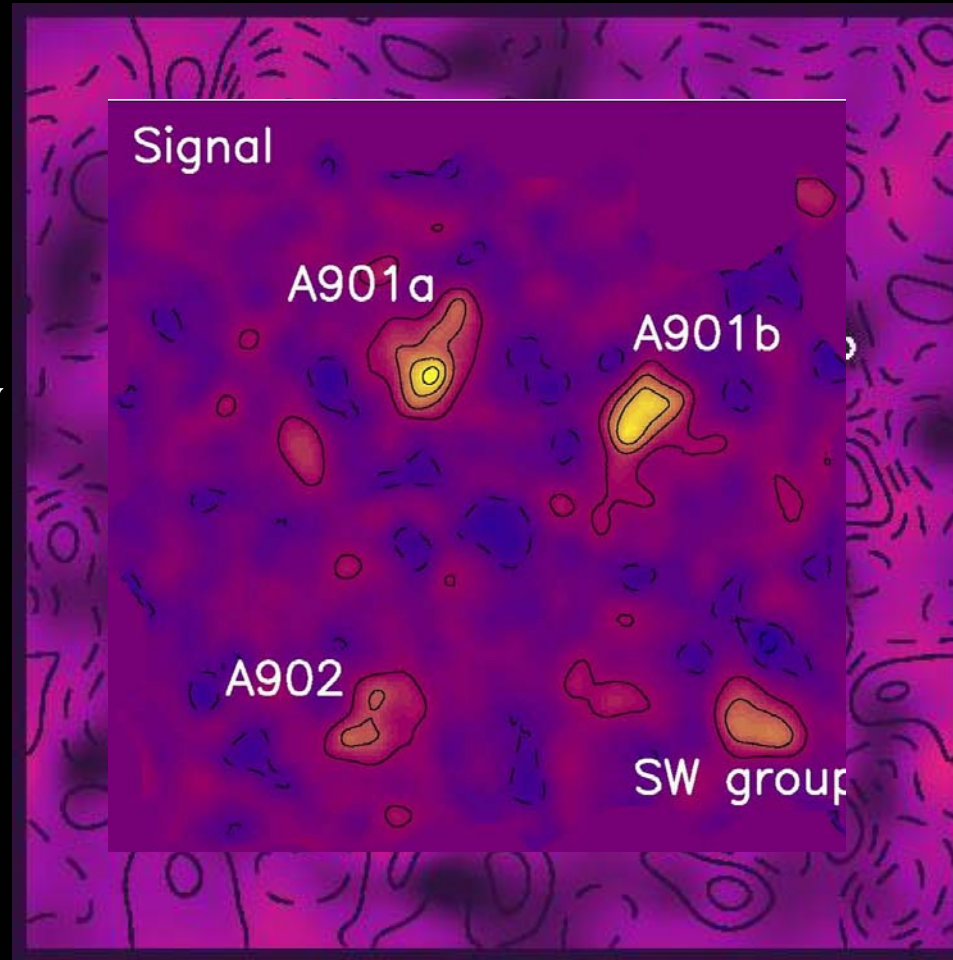
Error:
 $\Delta\kappa=0.02$
(1-contour)

Ground-based COMBO-17 data (Wolf et al 05)

Mass and light in Supercluster A901/2

Dark Matter
contours, κ .

Elliptical galaxy
light shading.



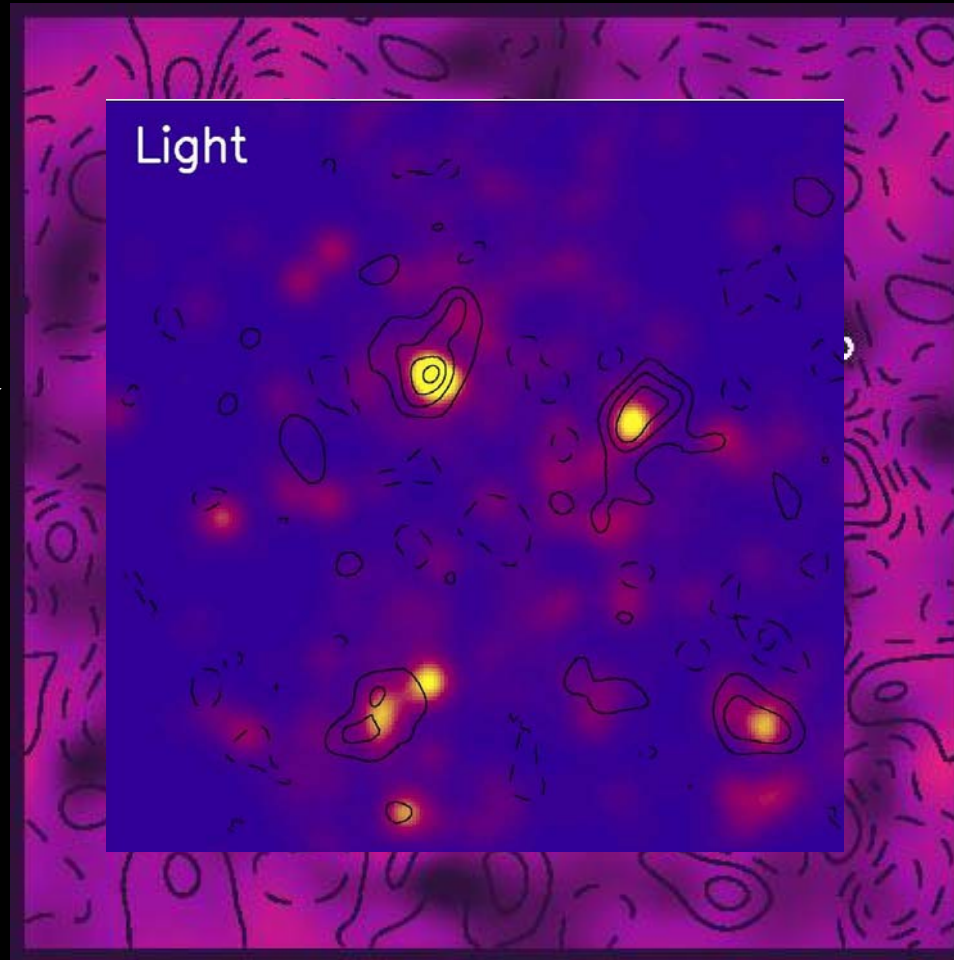
Error:
 $\Delta\kappa=0.02$
(1-contour)

Space-based HST- STAGES data (Grey et al 07, Heymans et al 2008)

Mass and light in Supercluster A901/2

Dark Matter
contours, κ .

Elliptical galaxy
light shading.

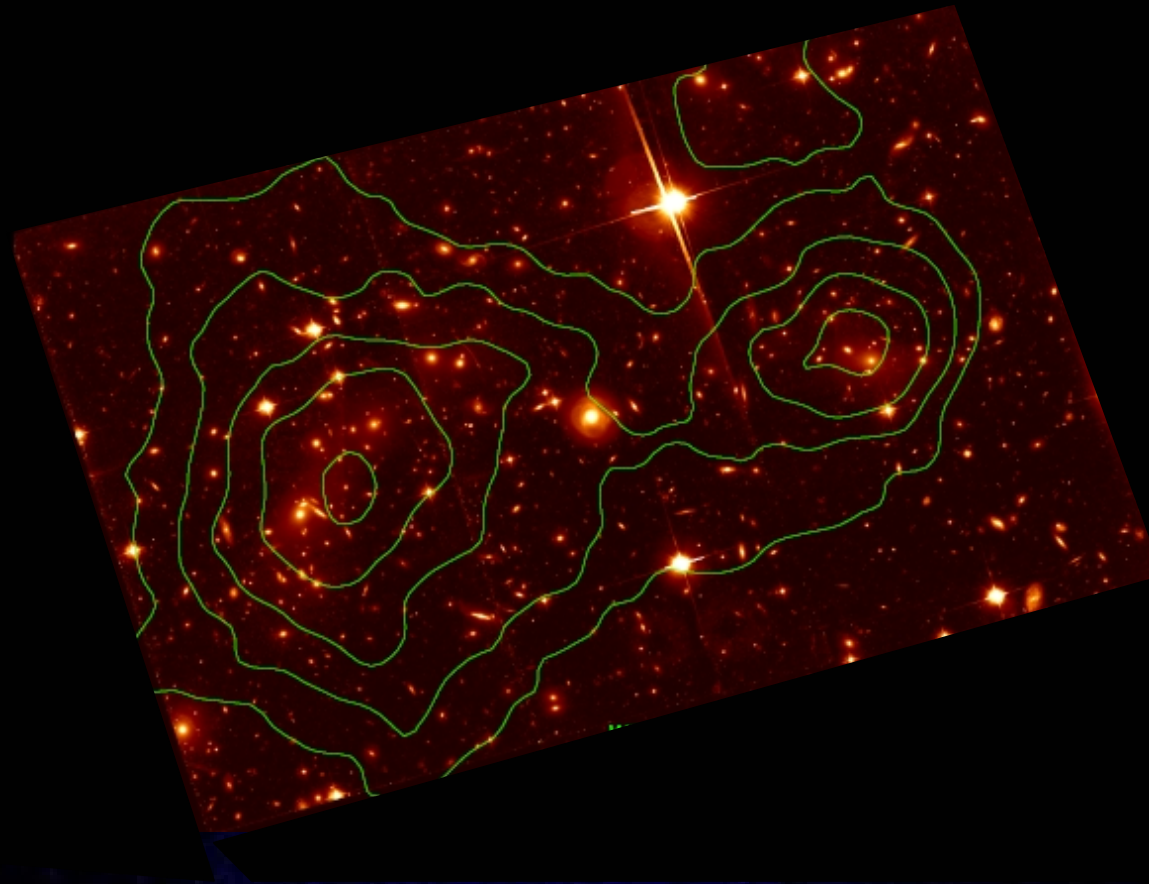


Error:
 $\Delta\kappa=0.02$
(1-contour)

Space-based HST- STAGES data (Grey et al 07, Heymans et al 2008)

The Bullet Cluster: Proof of Dark Matter?

Clowes et al 2006

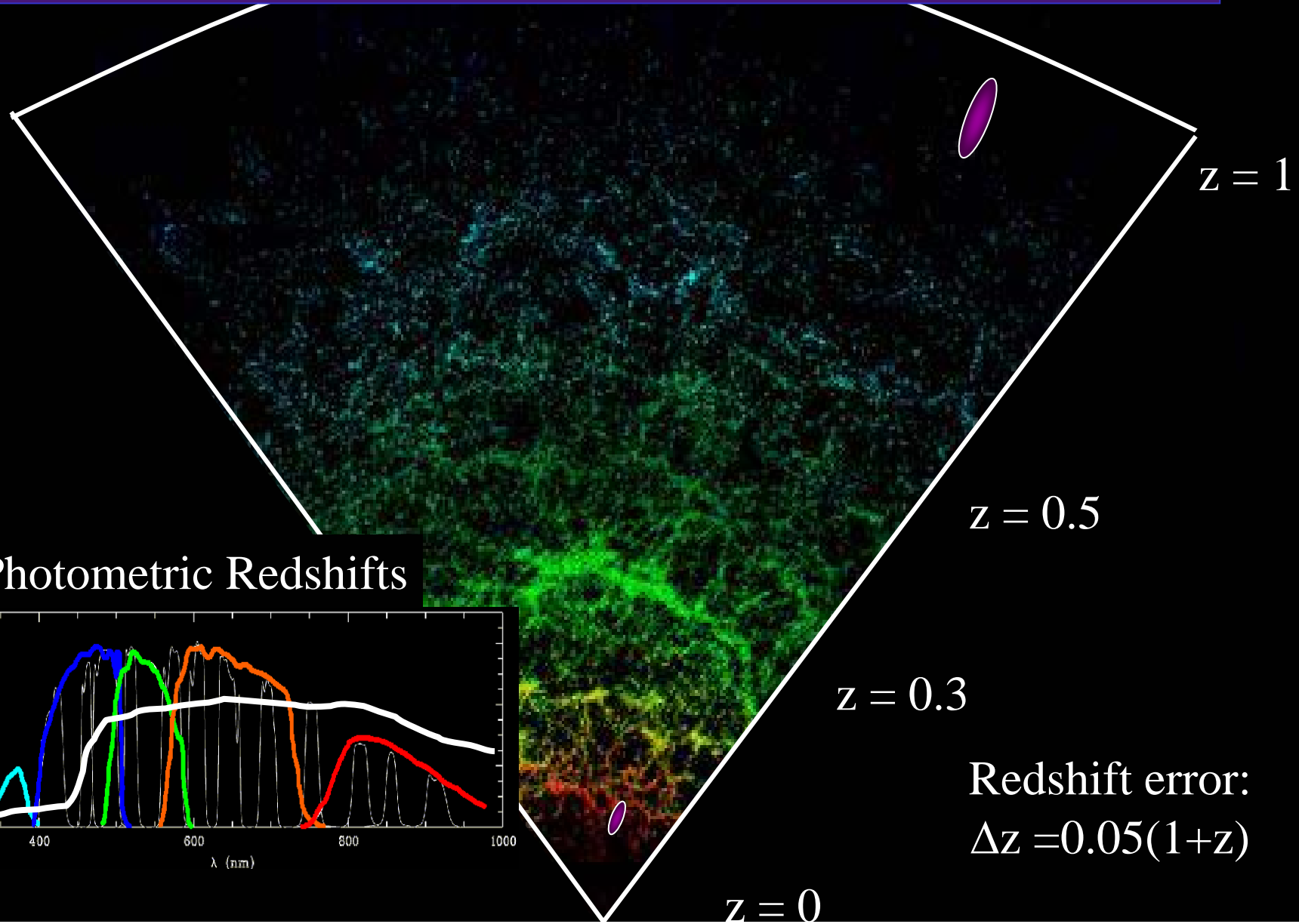


Chandra 0.5 Msec image

0.5 Mpc

$z=0.3$

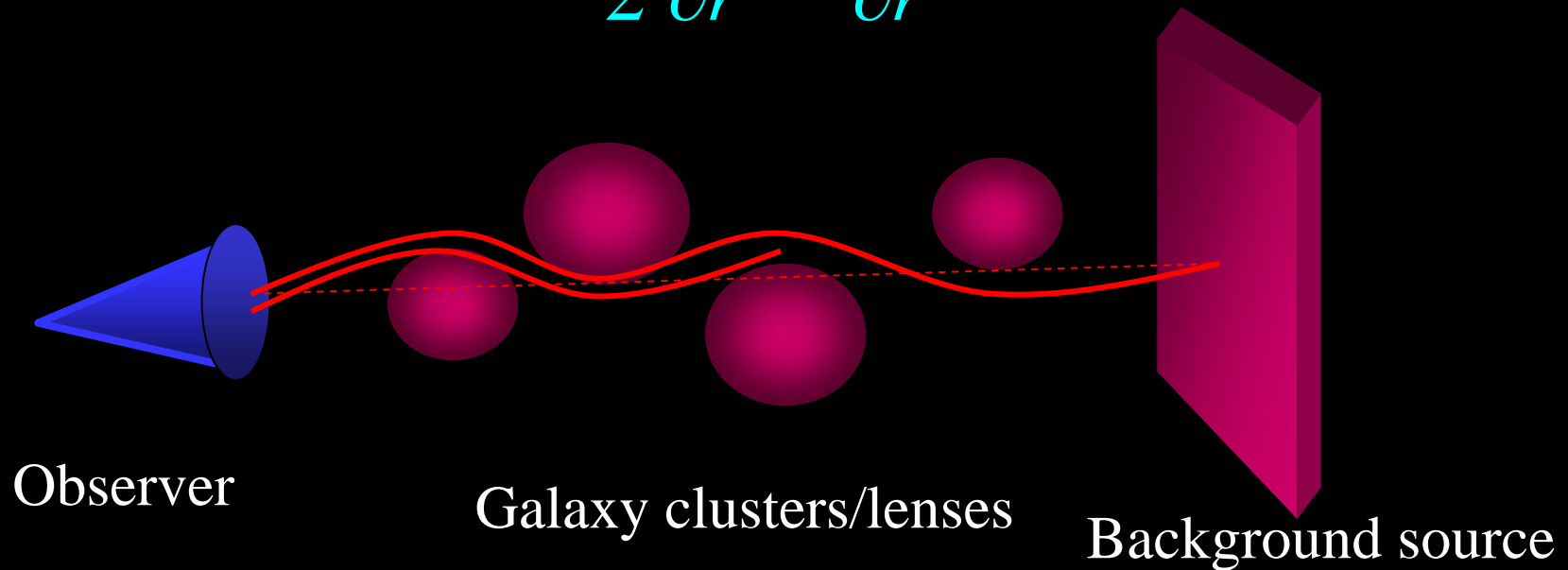
3D Lensing: Shear + Redshifts



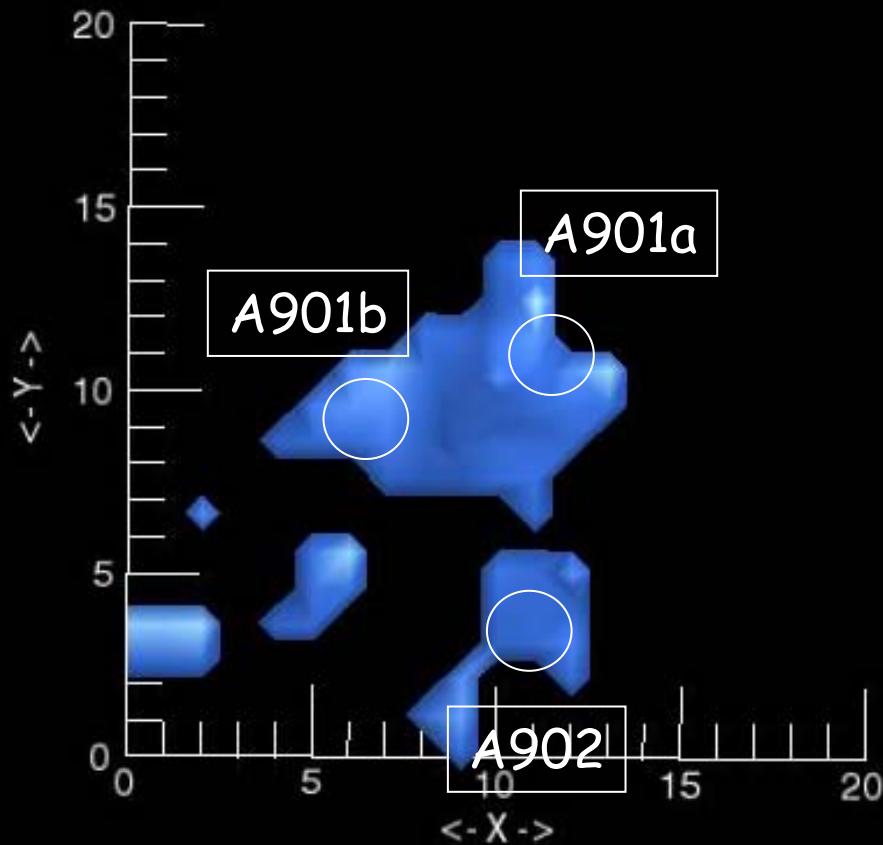
Mapping the Dark Matter in 3-D

- With source redshifts, z , solve Φ exactly from the relativistic equation of motion (Taylor, 2001):

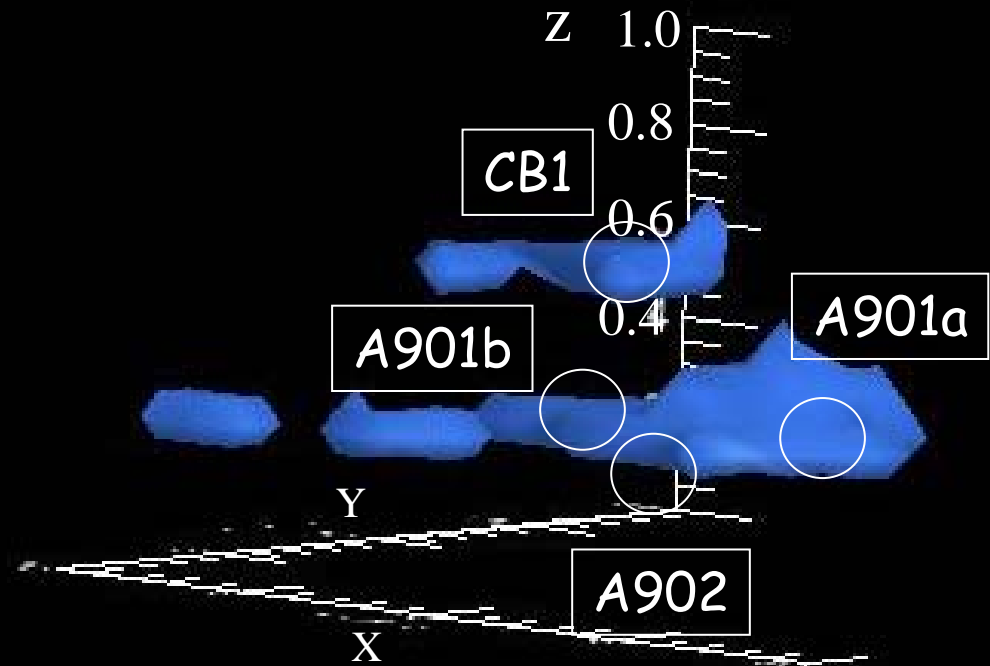
$$\Phi(r, \underline{\theta}) = \frac{1}{2} \frac{\partial}{\partial r} r^2 \frac{\partial}{\partial r} \phi(r, \underline{\theta})$$



3-D Dark Matter Mapping



(2- σ threshold)

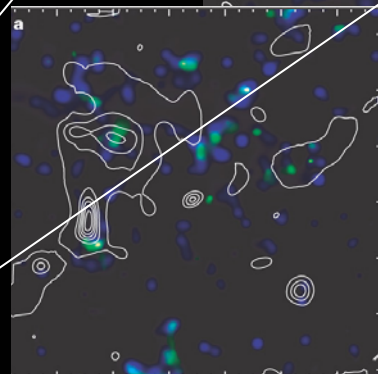


Taylor, et al, 2004 MN

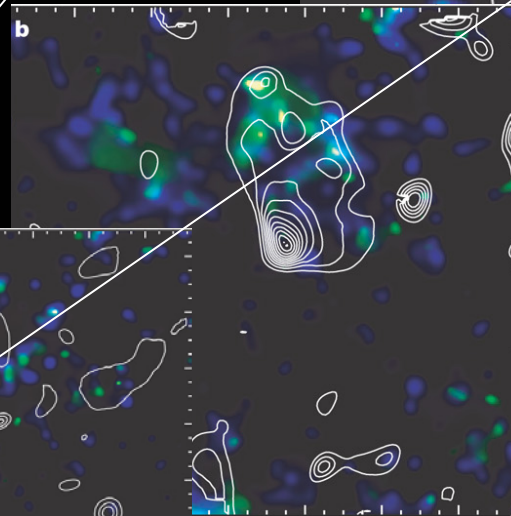
Evolution of Dark Matter Clustering in COSMOS



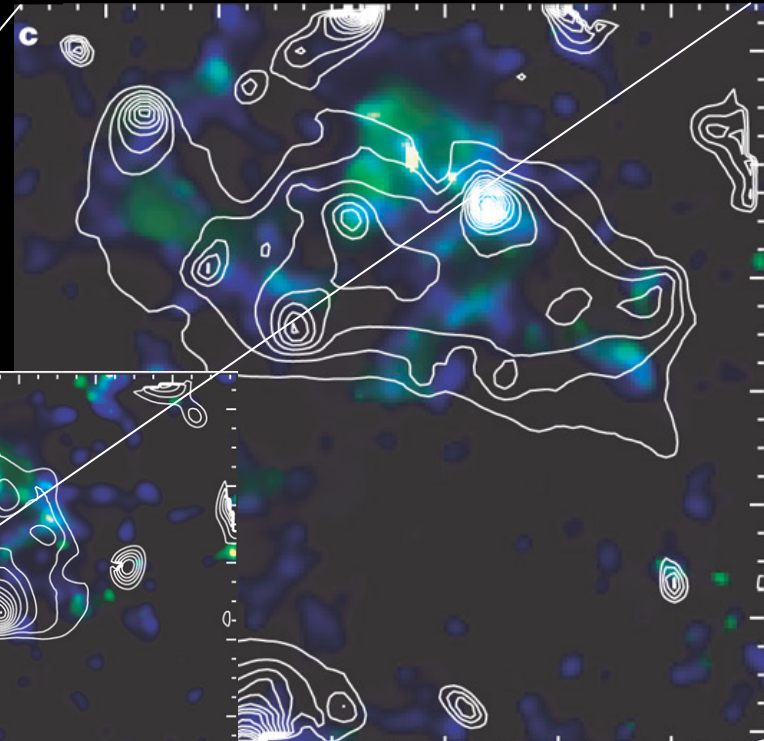
$z = 0.3$



$z = 0.5$



$z = 0.7$



$L = 30 \text{ Mpc}$

$L = 25 \text{ Mpc}$

$L = 20 \text{ Mpc}$

2 square degrees

Massey, Taylor et al, Nature, 2007

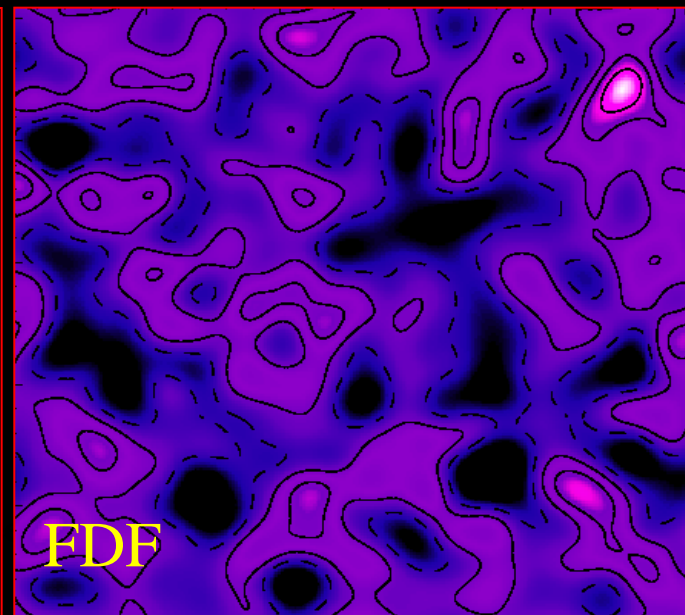
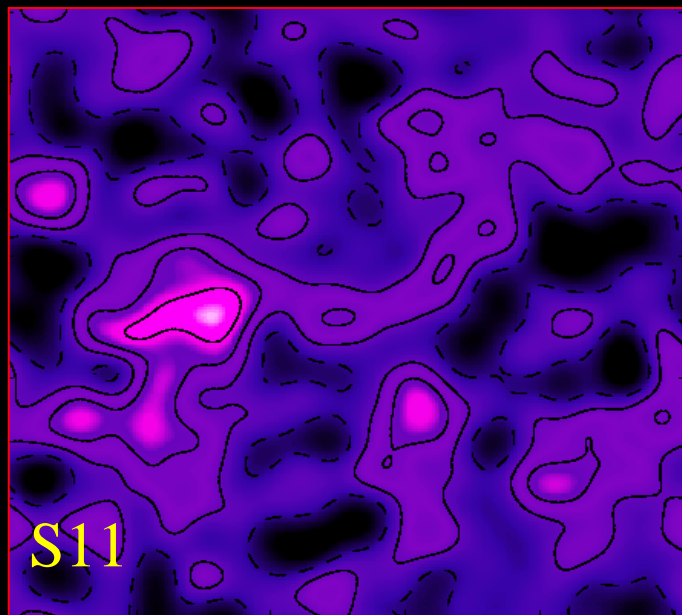
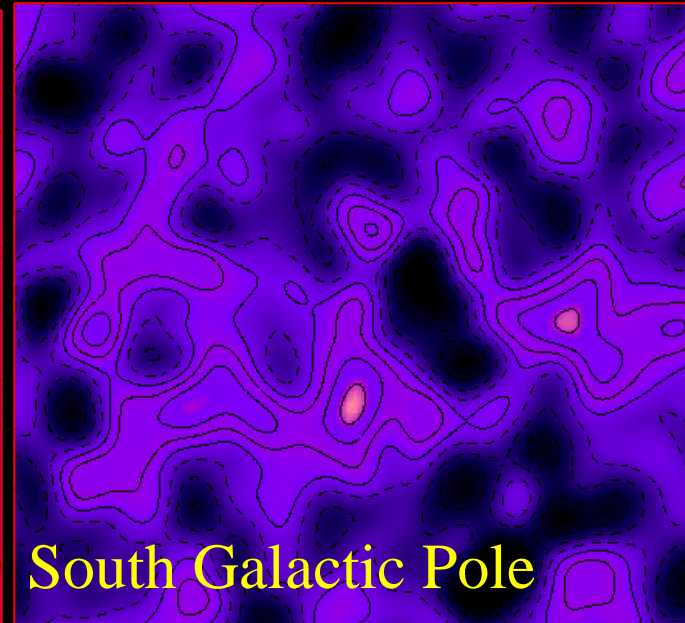
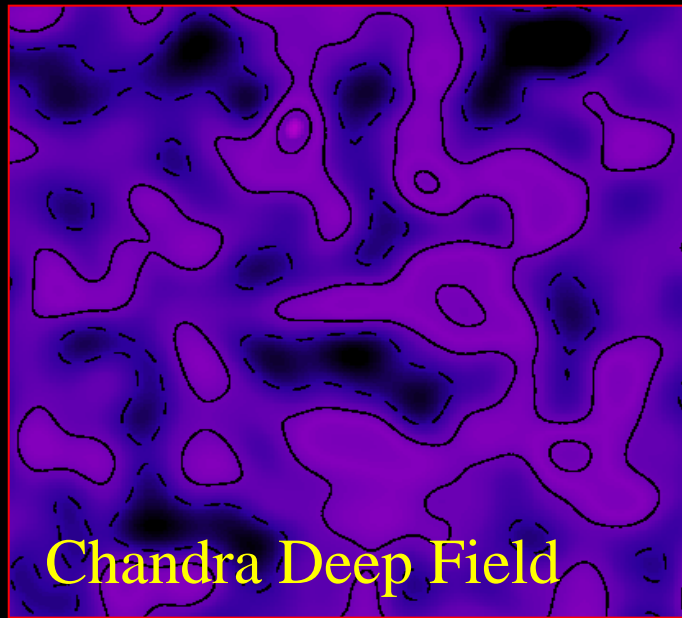
3-D Dark Matter Mapping with HST-COSMOS



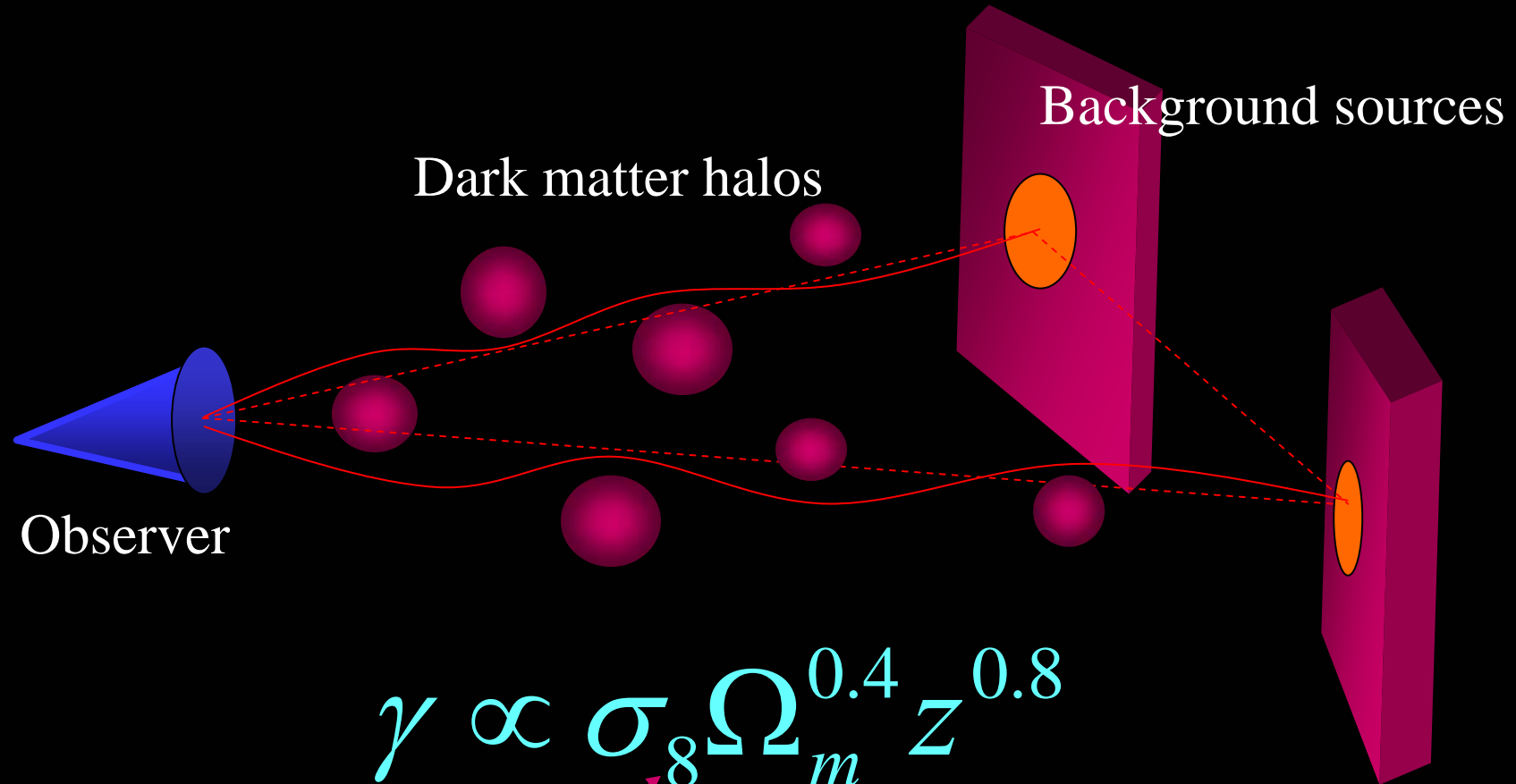
Massey, Taylor et al, Nature (2007)

Random Mass Fields on the Sky

- 1 sq deg.



Geometry & Clustering: Cosmic Shear



Variance of matter variations

Matter density parameter

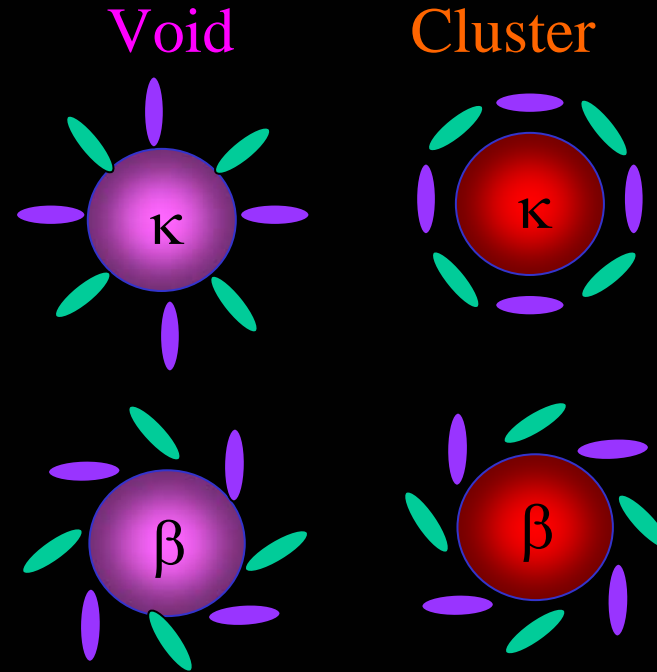
$$\Omega_m \propto \rho_m H_0^2$$

The κ/β (E/B) Decomposition

- Can decompose γ_1, γ_2 into:

κ -modes (even-parity):
(or grad)

β -modes (odd-parity):
(or curl)



- Gravitational lensing produces only κ -modes.
- Noise & systematics produces both κ & β -modes.

Cosmic Shear Correlations

Fu et al, 2008: Canada-France-Hawaii Legacy Survey 57 sq deg

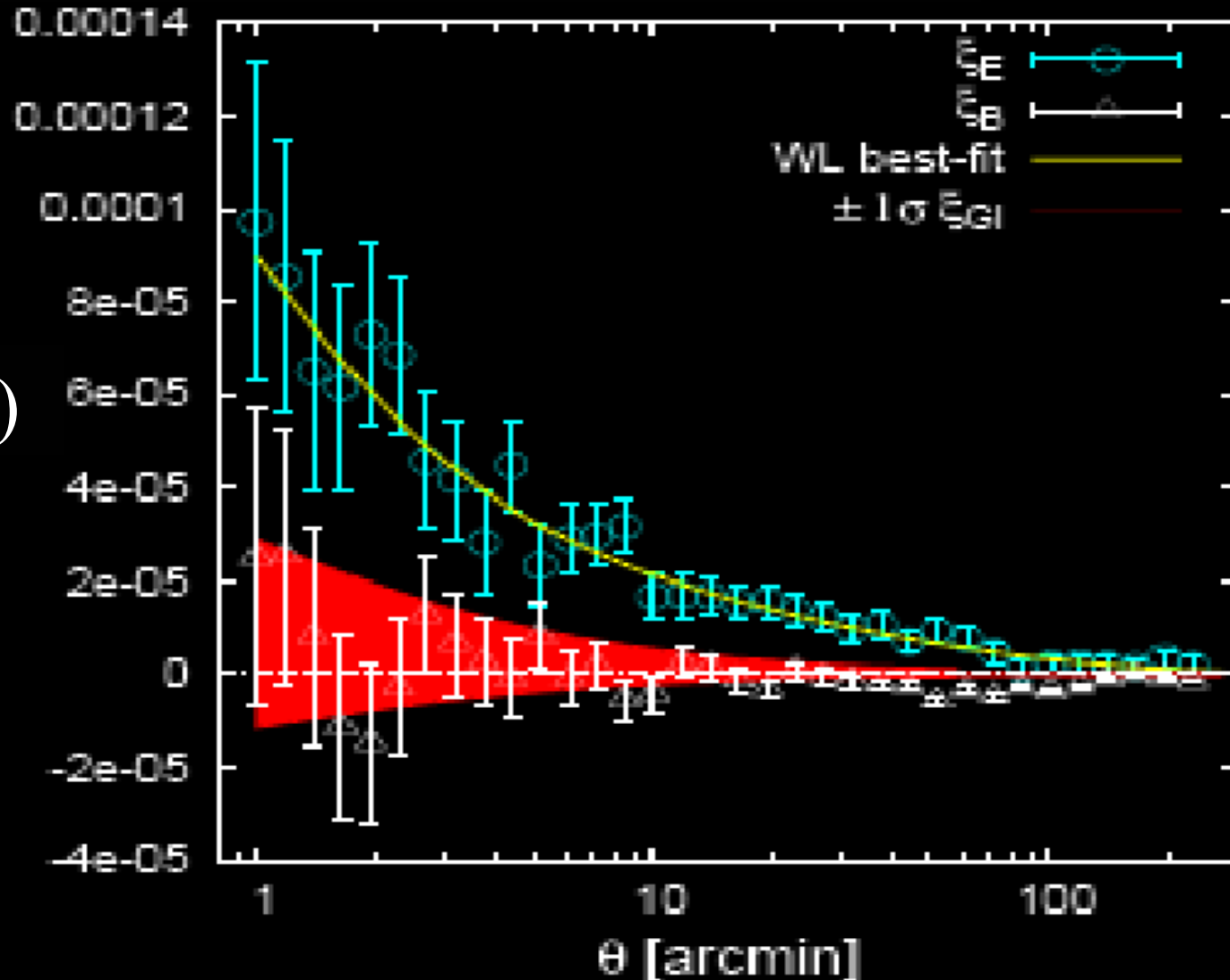
0.6Mpc/h

6Mpc/h

30Mpc/h

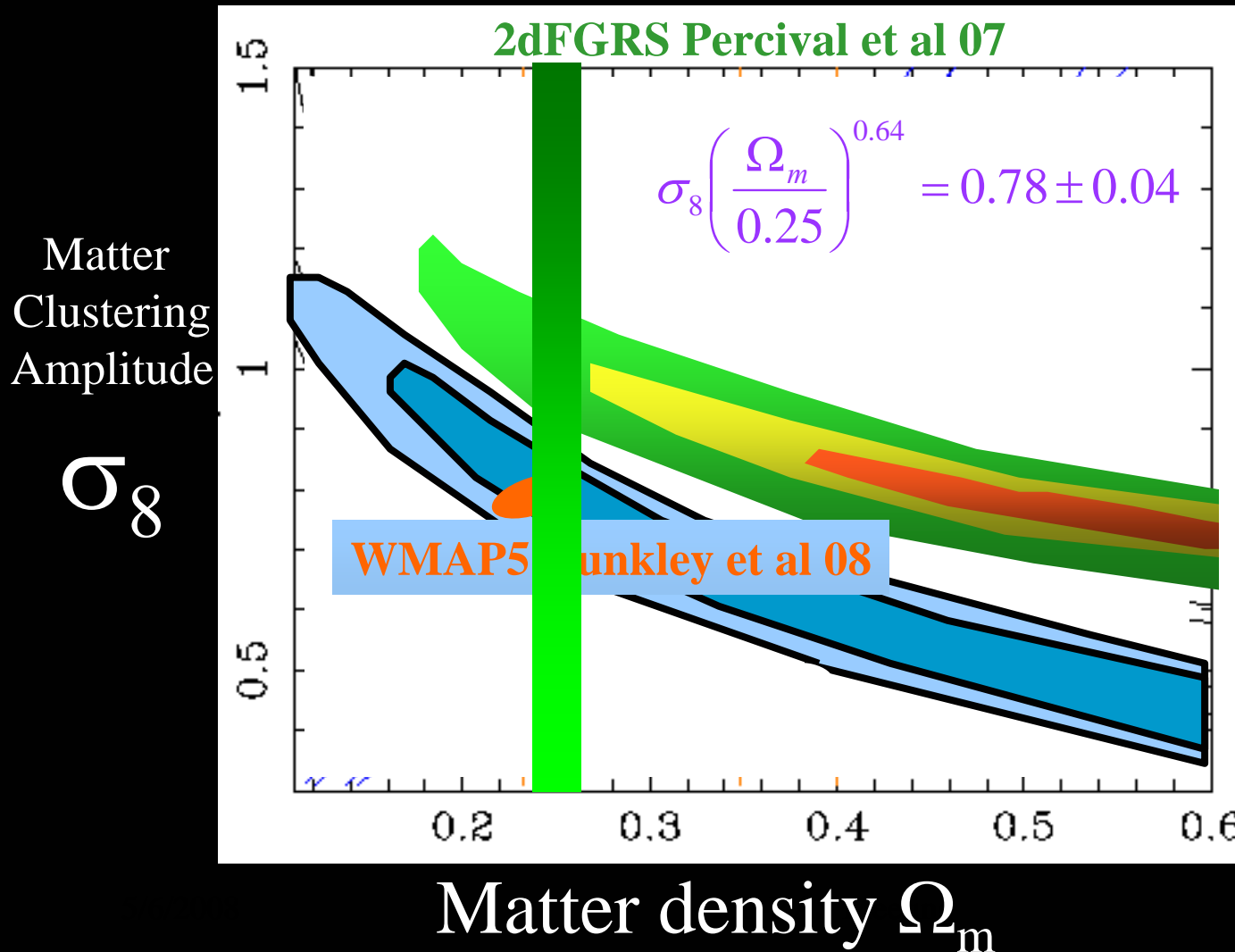
Shear-Shear
Correlations

$$C_{\gamma\gamma}(\theta)$$



Cosmological Parameters from Cosmic Shear

Cosmic Shear from 3yr CFHTLS 57 square degrees (Fu et al '08)



Spatially flat
Universe.

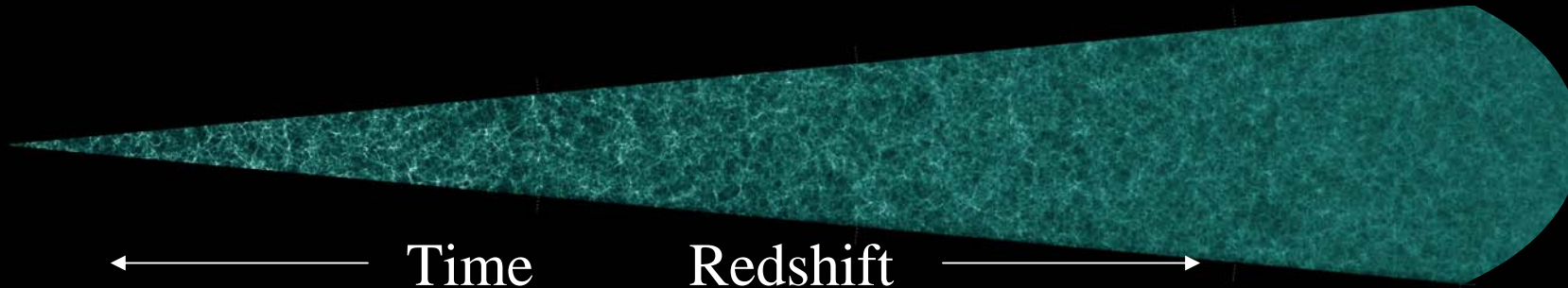
$$\Omega_m = 0.25 \pm 0.02$$

$$\sigma_8 = 0.77 \pm 0.03$$

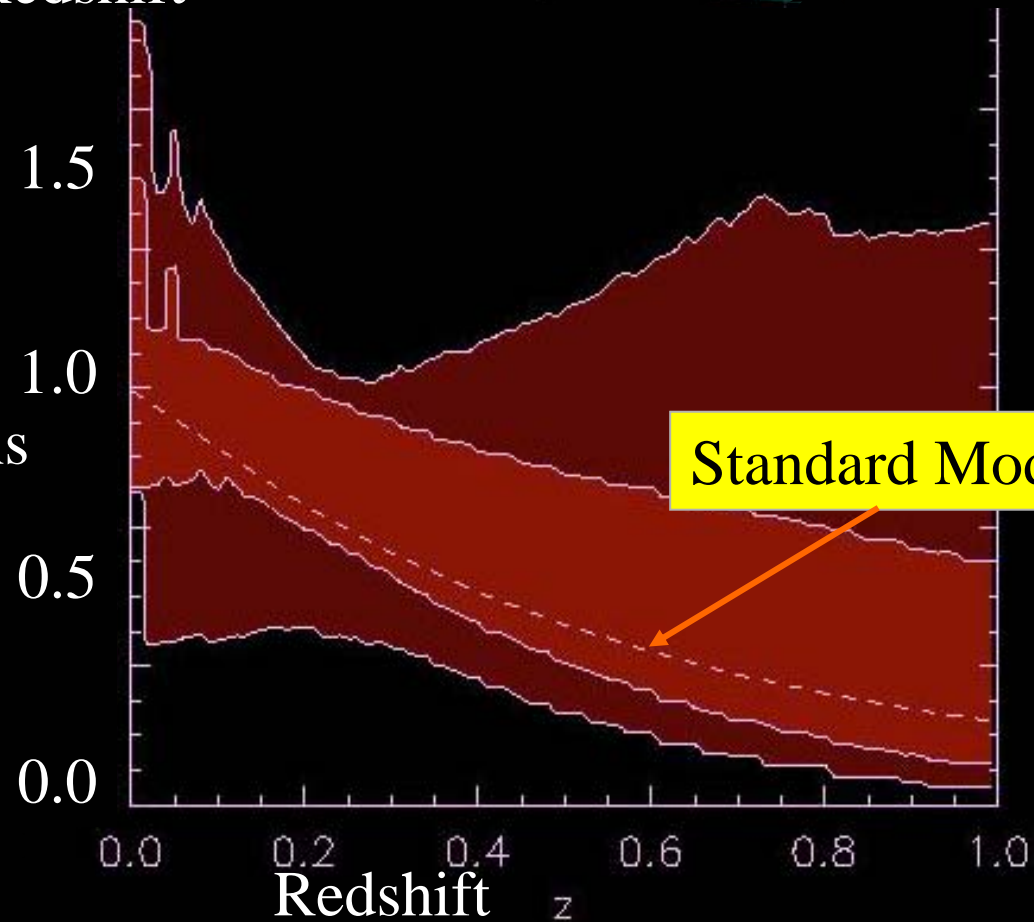
Massey et al 07

2 sq deg COSMOS
3-D Analysis

Growth of Density Perturbations from Lensing



Amplitude of
Density Perturbations



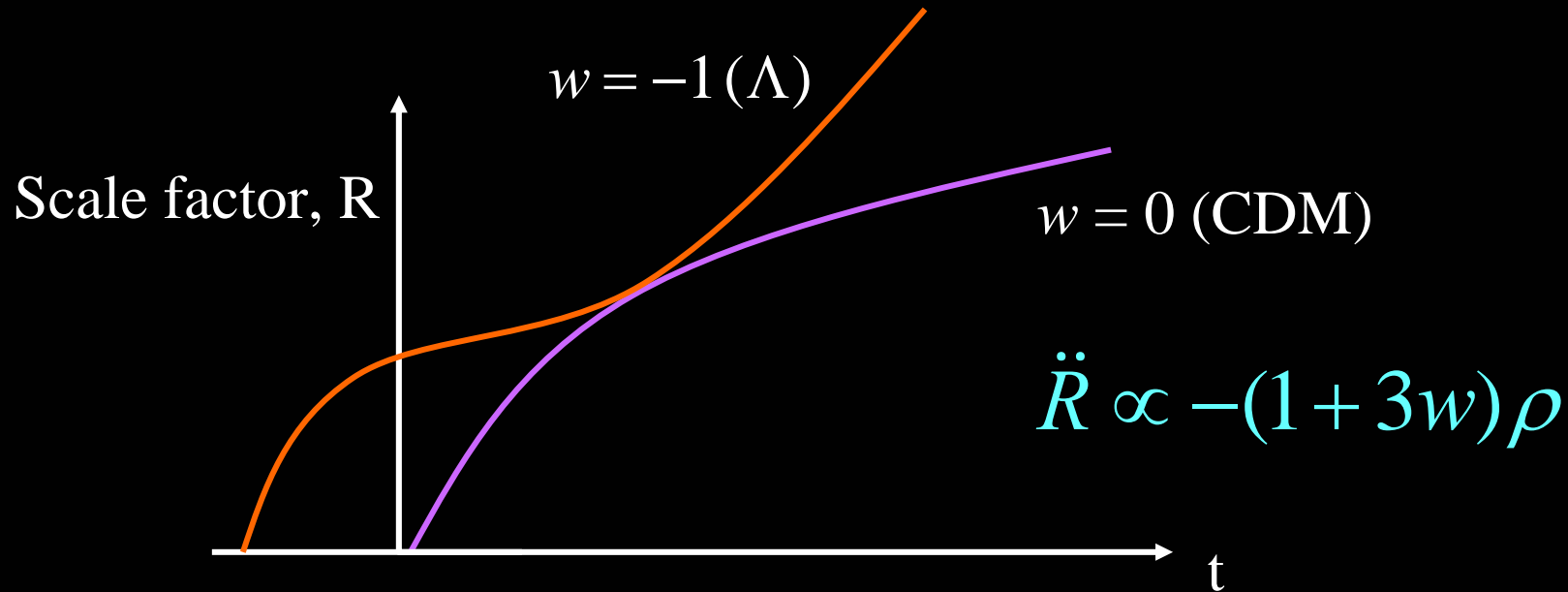
COMBO-17

Bacon, Taylor, et al 2005

Cosmic Acceleration & Dark Energy

Dark Energy characterized by an Equation of State:

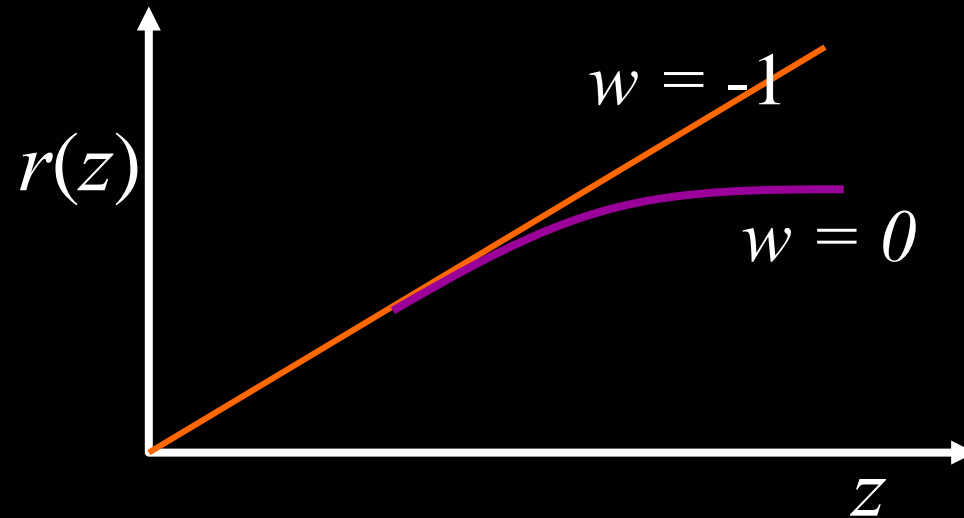
$$P = w\rho c^2$$



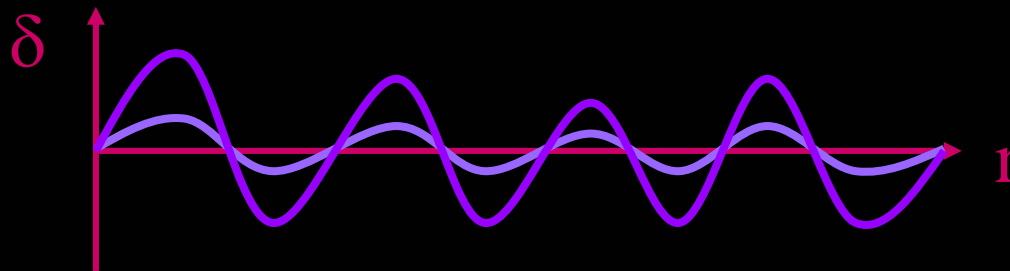
If $w = -1$ energy-density is Einstein's
Cosmological Constant, Λ .

Observable Effects of Dark Energy

- Geometry: DE changes the photon distance-redshift relation: $r(z)$



- Clustering: Alters the growth of density perturbations, $\delta(t)$.



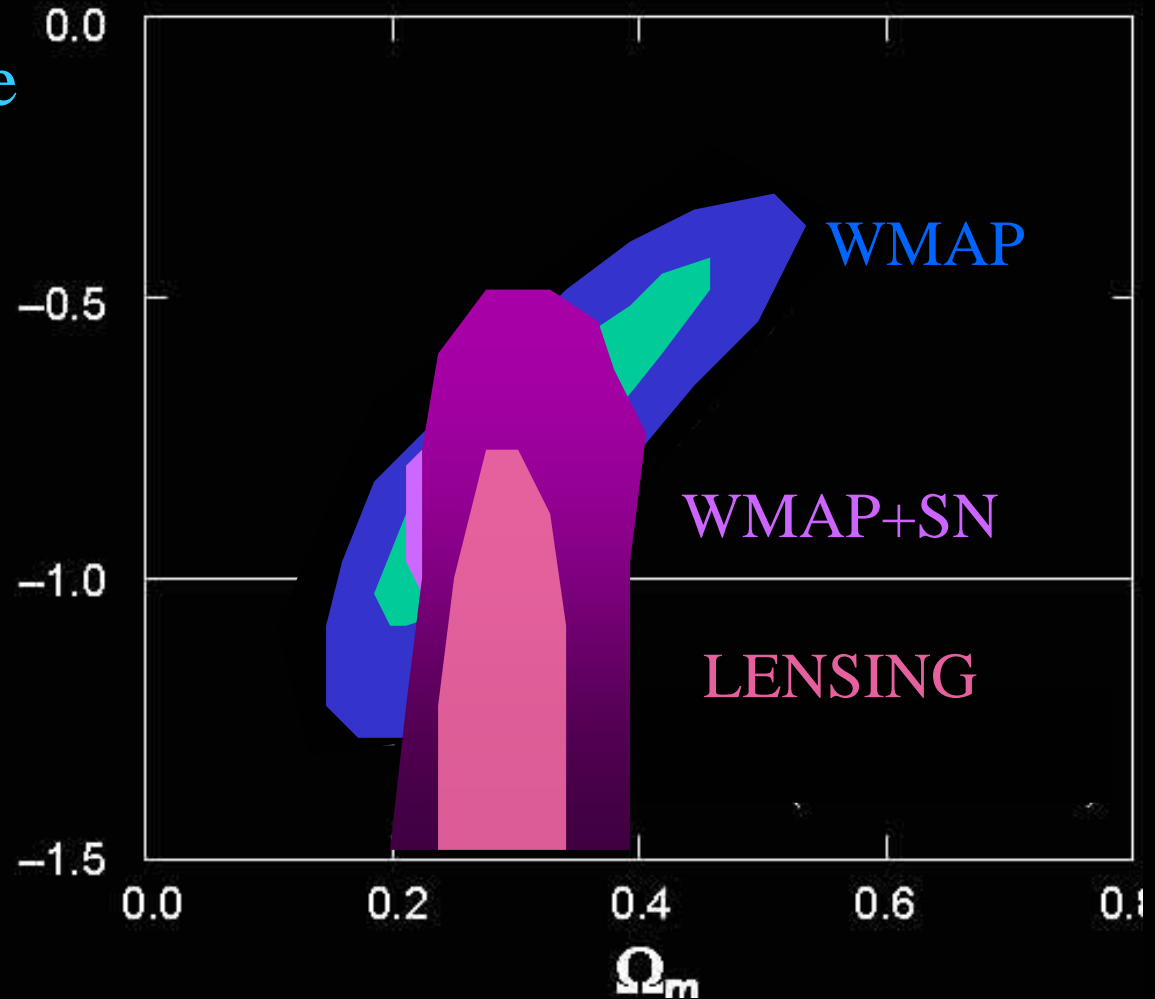
w from the CMB + Supernova + Lensing

Assume flat Universe

WMAP + SN

$$P_{DE} = w\rho_{DE}$$

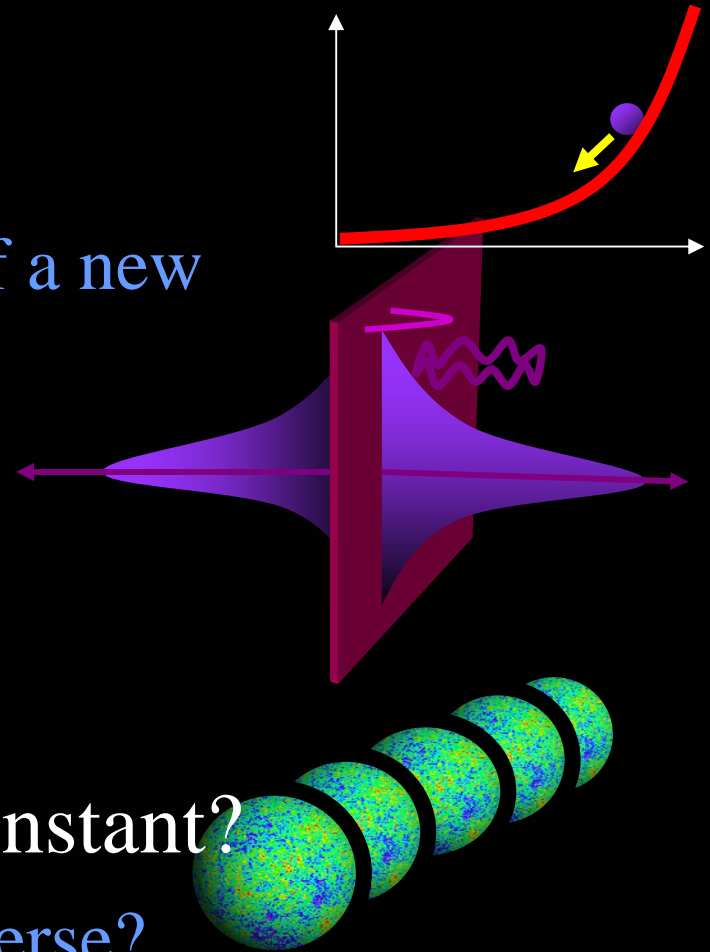
$$w = -0.93^{+0.05}_{-0.07}$$



Spergel et al ApJ 2006, Tereno et al 2006

Major Question: What is the Dark Energy?

- Particle physics?
 - Zero-point vacuum energy of a new scalar field.
- Gravitational physics?
 - Extra spatial dimensions.
- Einstein's Cosmological Constant?
 - Random variable in a Multiverse?

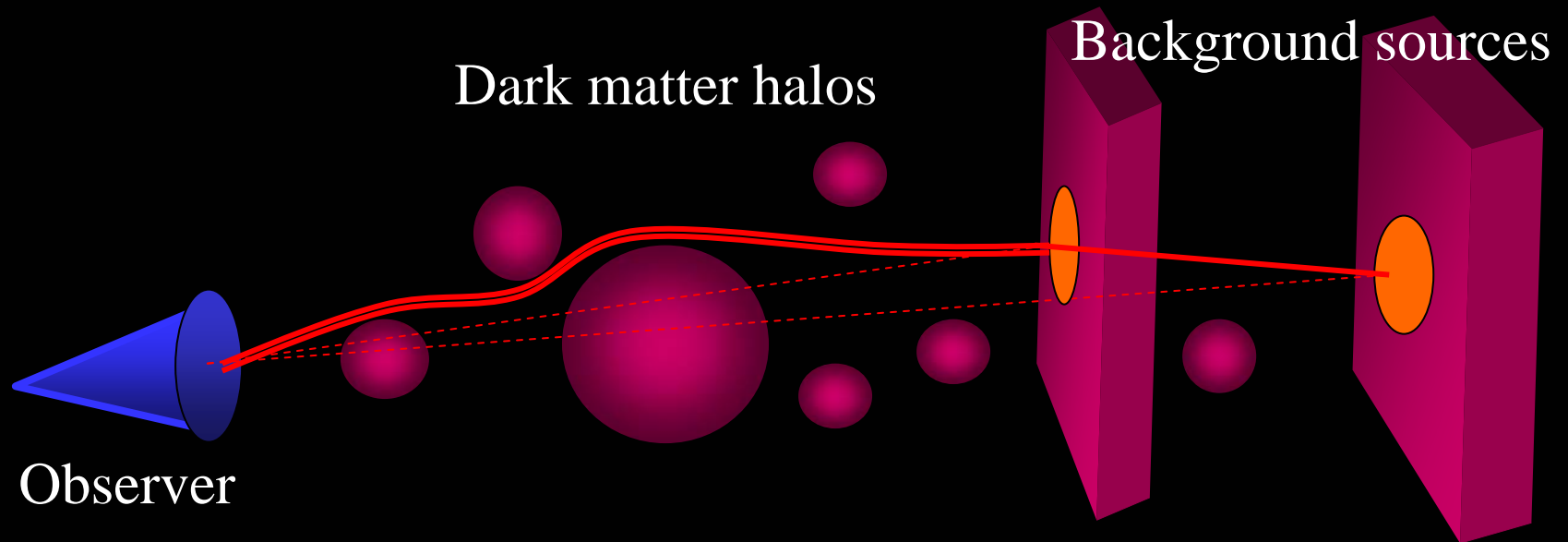


Dark Energy Equation of State

- The key to Dark Energy lies in its evolution:
 - If it doesn't it's Einstein's Cosmological Constant.
 - If it does it's dynamical field or non-Einstein gravity.
 - Differentiate between dynamical field and non-Einstein gravity by differences in geometry and clustering.

Geometric Test: 3-D Shear Ratios

(Jain & Taylor 2003, Taylor, Kitching, Bacon, Heavens 2005)



$$R_{ij} = \frac{\gamma(z_i)}{\gamma(z_j)} = \frac{S_k[r_j]S_k[r_i - r_L]}{S_k[r_i]S_k[r_j - r_L]} \approx w^{-0.02} \Omega_V^{0.01}$$

- Signal depends on $(\Omega_m, \Omega_v, w_0, w_a)$ and is insensitive to clustering.

Testing Gravity

- Dark energy opens up possibility gravity sector is wrong.
- A number of ways to test gravity with lensing:
 1. Generalize Einstein gravity:
 - $2\Phi \rightarrow \Phi + \Psi = (1 + \eta)\Phi$.
 - Add vector, tensor perturbations V, E .
 2. Parameterize non-Einstein gravity:
 - Growth index, γ , in DGP, braneworlds.
 3. Compare full non-Einstein gravity models:
 - Scalar/tensor models
 - Braneworld/DGP-like
 - $F(R)$ models
 - TeVeS, vector/tensor
 4. Consistency in w from structure and geometry.

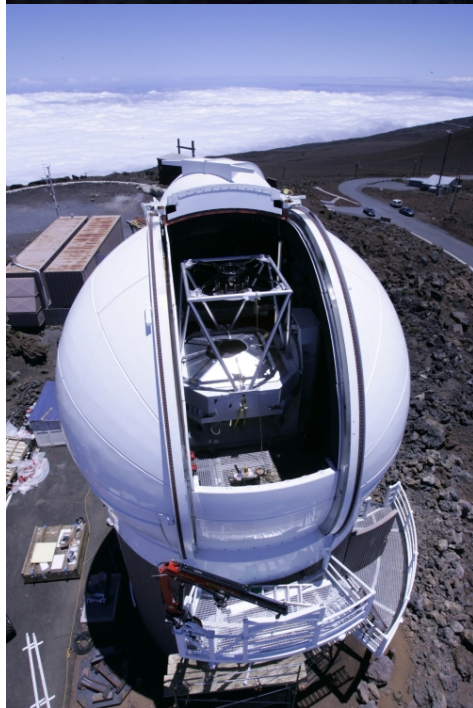
Neutrino dark matter

- Neutrino oscillation experiments show $m < 2.2\text{eV}$.
- Limit sum of neutrino masses to $> 0.06\text{eV}$.
- Future experiments (eg KATRIN) will reach $> 0.2\text{eV}$.
- Planck expects 0.5eV .
- Weak lensing with DUNE (+Planck) from space can measure the damping tail in the matter power spectrum:

$$m > 0.04\text{eV}$$



Pan-STARRS 1



- US led.
- 1.8 meter primary
- 1.4 Gpixel camera.
- 7 square degree field-of-view.
- 3π Survey
- g, r, i, z, y (r=24.5)
- PS-1 2008-2011 \mapsto PS-4

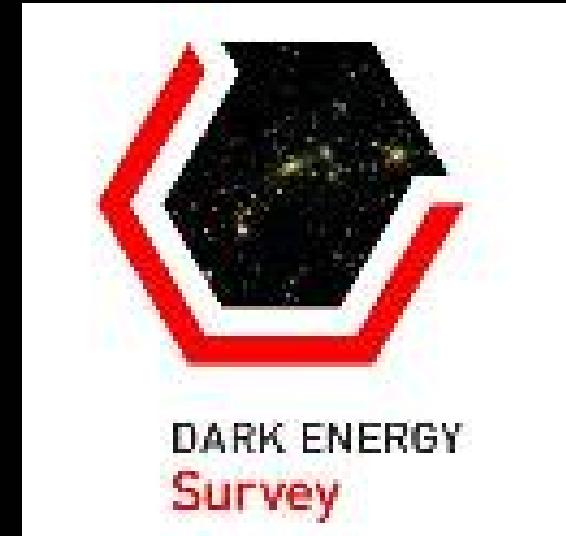
2008-2013: VST-KIDS

- EU led.
- ESO's Kilo-Degree Survey
- 2m primary
- 184Mpixels
- 1 square degree field-of-view
- 1,500 sq deg
- u'g'r'i'z'

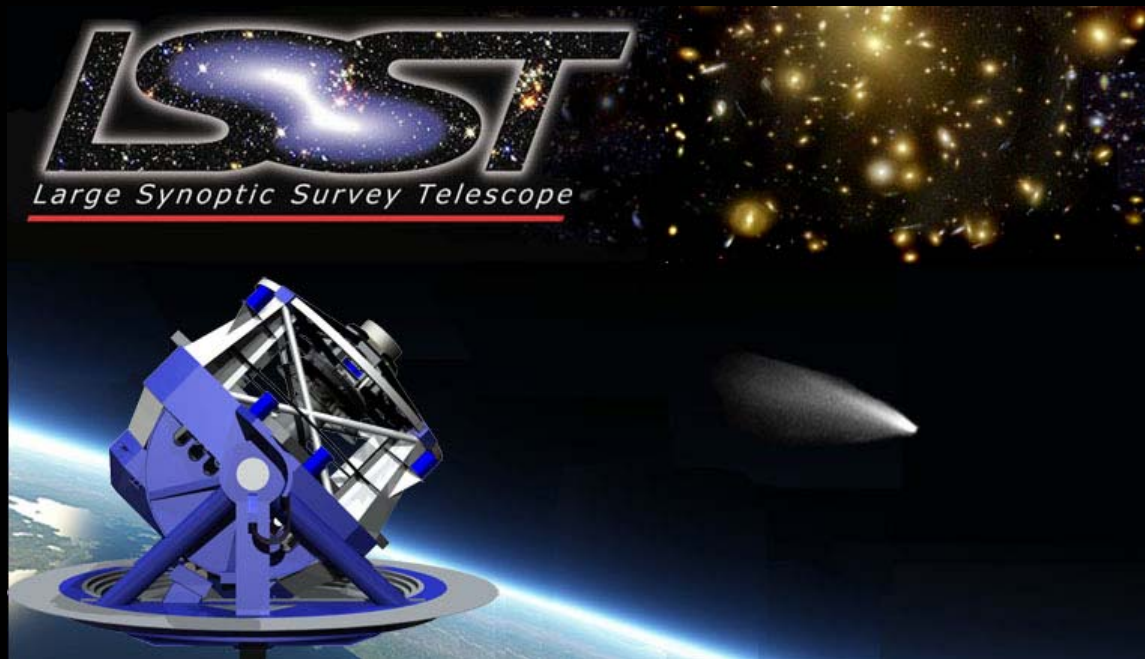


2010-2015: DES

- The Dark Energy Survey.
 - US led.
 - 4-metre primary
 - 500 Megapixel
 - 3 sqdeg fov
 - g,r,i,z
 - 5000 sq deg

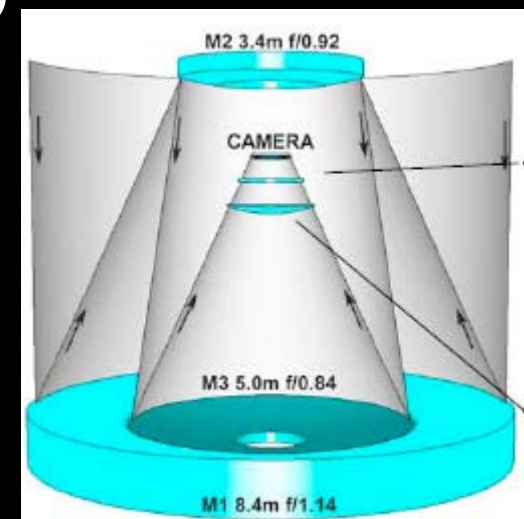


2014-2024: LSST



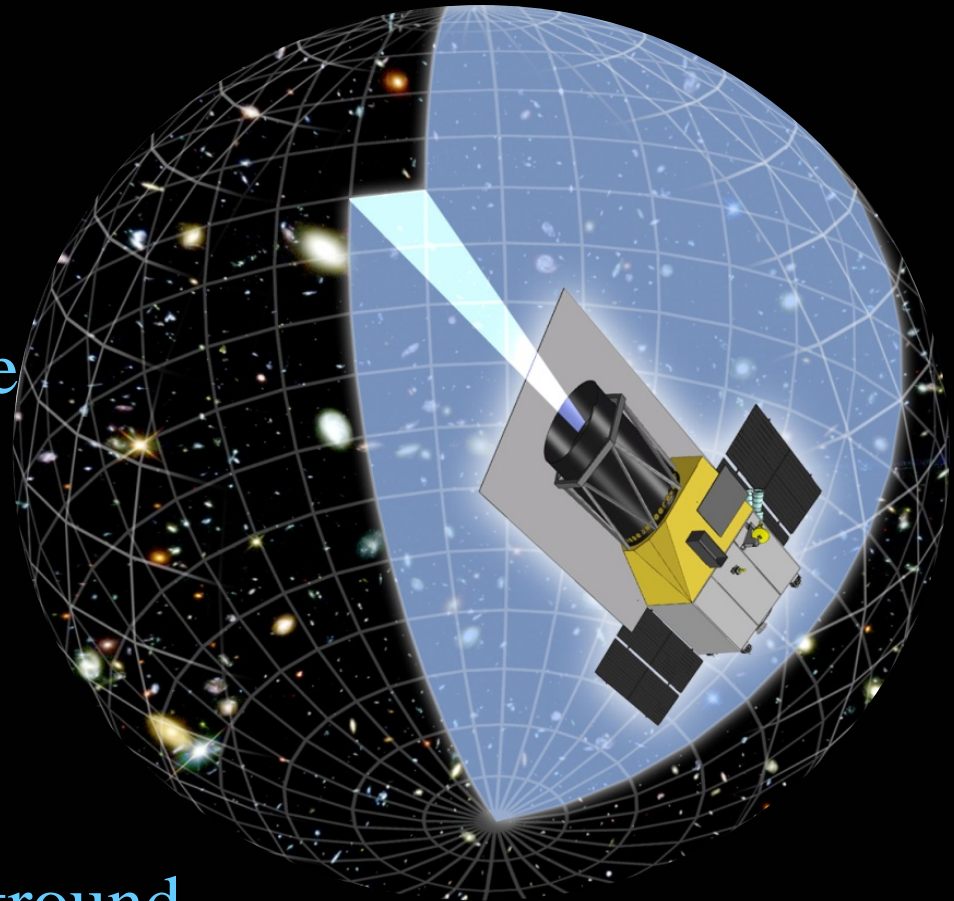
• Large Synoptic Survey Telescope (LSST)

- US led.
- 8.4m (effectively 6.5m) Primary
- 3.2 Gpixels
- 9.6 sq deg fov
- ugrizY

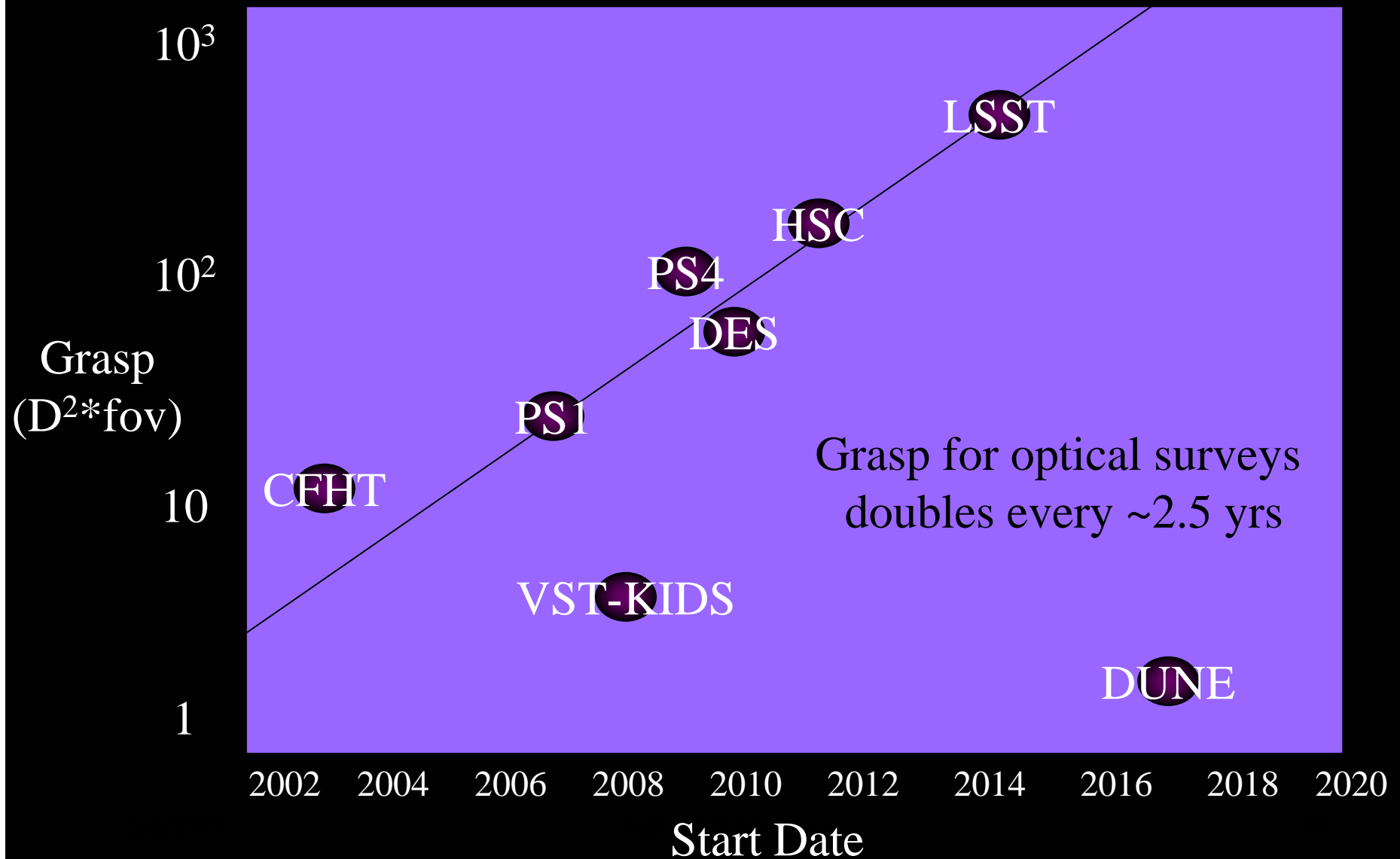


2017-2021: DUNE – Dark UNiverse Explorer

- Cosmic Visions proposal to European Space Agency
 - EU led.
 - 1.2m satellite telescope
 - 0.5 sq deg fov
 - 20,000 sq deg
 - r-i-z + Y,J,H
 - Optical photo-z from ground.
 - Merger with spectroscopic survey SPACE (BAO's).



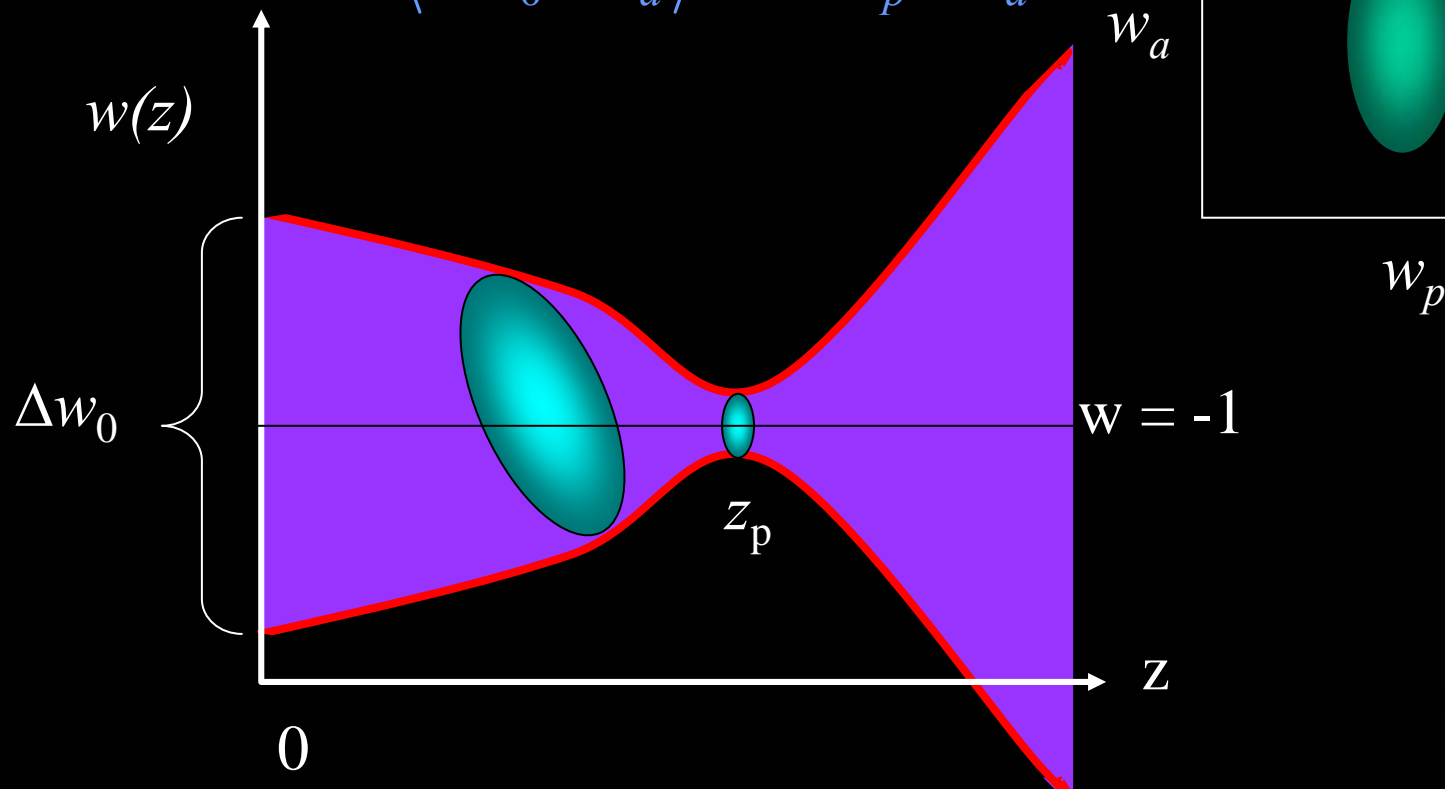
Grasp vs. Start Date



Dark Energy Figure of Merit (FoM)

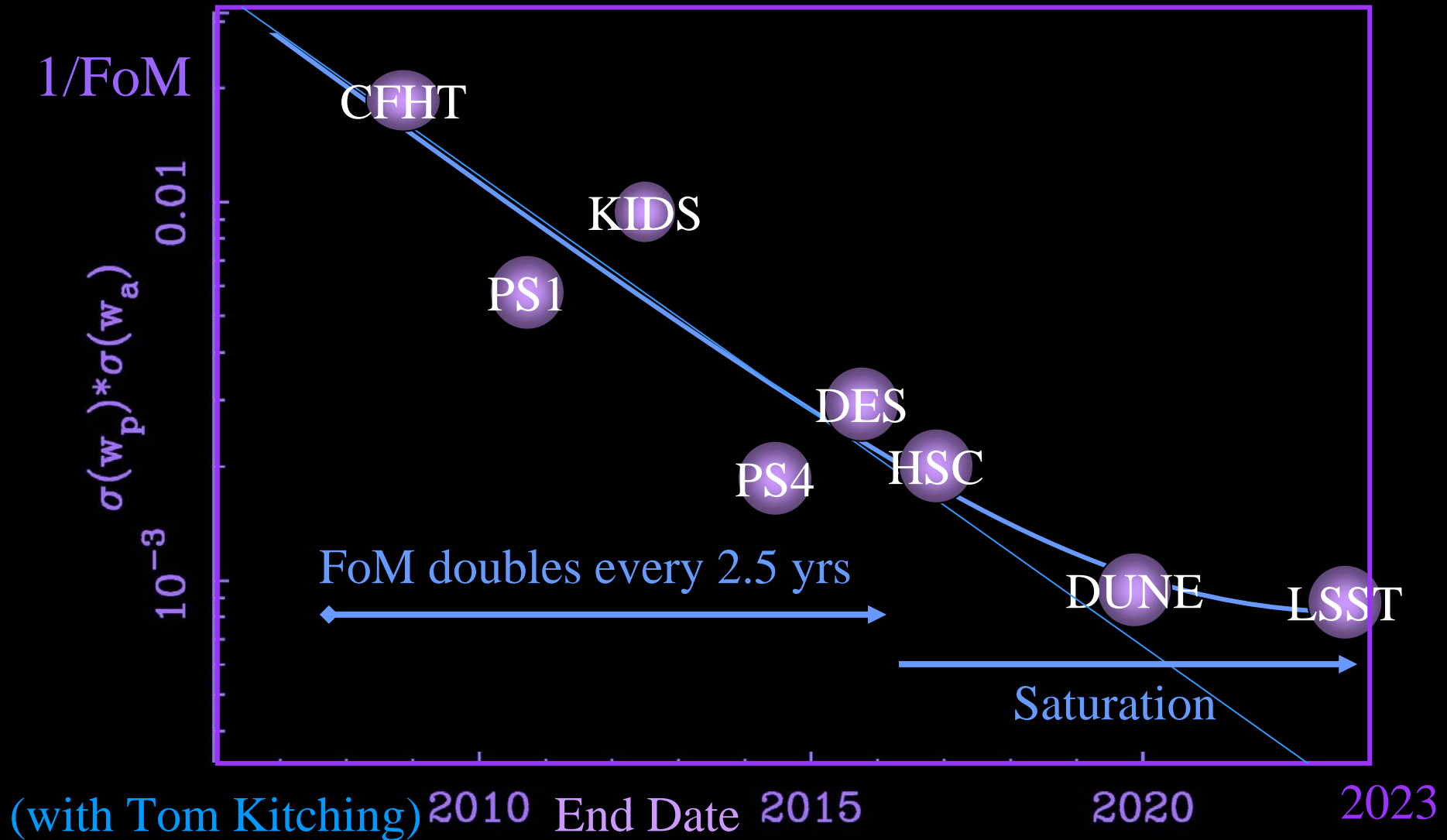
- Evolving equation of state: $w(z) = w_0 + w_a [1 - a(z)]$
- Define pivot redshift, z_p : $w_p = w_0 + w_a [1 - a_p]$

$$FoM = \frac{1}{\langle \Delta w_0 \Delta w_a \rangle} = \frac{1}{\Delta w_p \Delta w_a}$$



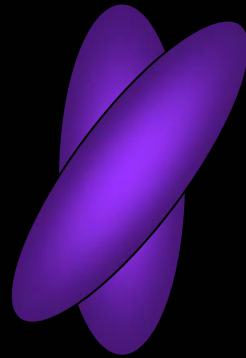
FoM for Dark Energy from Lensing

3-D shear power and shear-ratios combined
with Planck Explorer CMB survey (2008)



Challenges: Image Distortions

- Image distortions: (Kitching, Taylor & Heavens 2007)

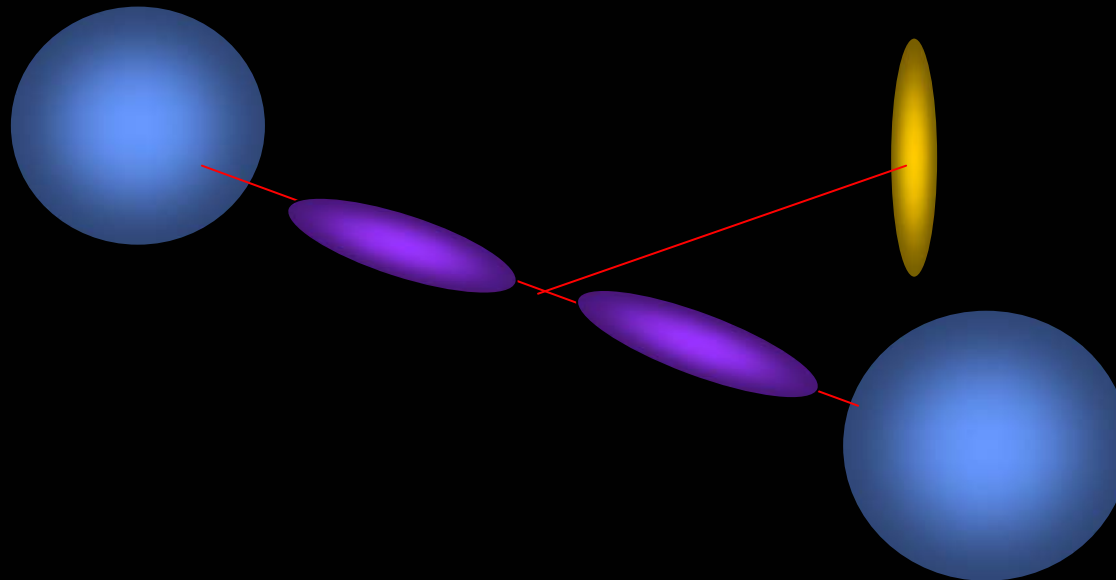


$$\gamma' = A e^{i2\omega} \gamma + \gamma_{bias}$$

calibration rotation bias.

Challenges: Intrinsic Alignment

- Two alignment effects:
 - Intrinsic-Intrinsic alignments
 - Galaxy-Intrinsic alignment

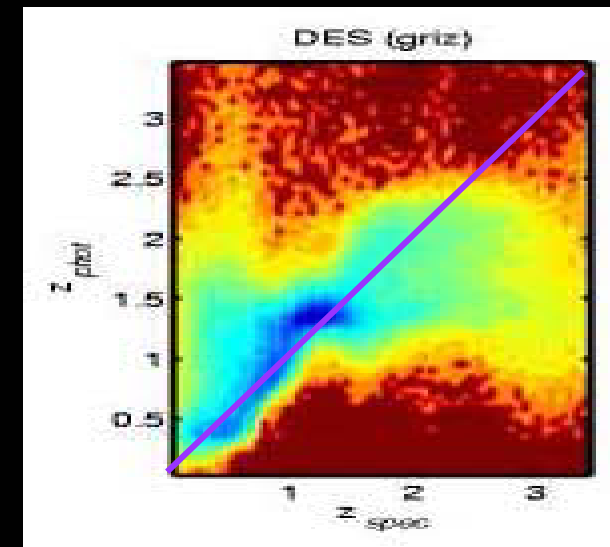
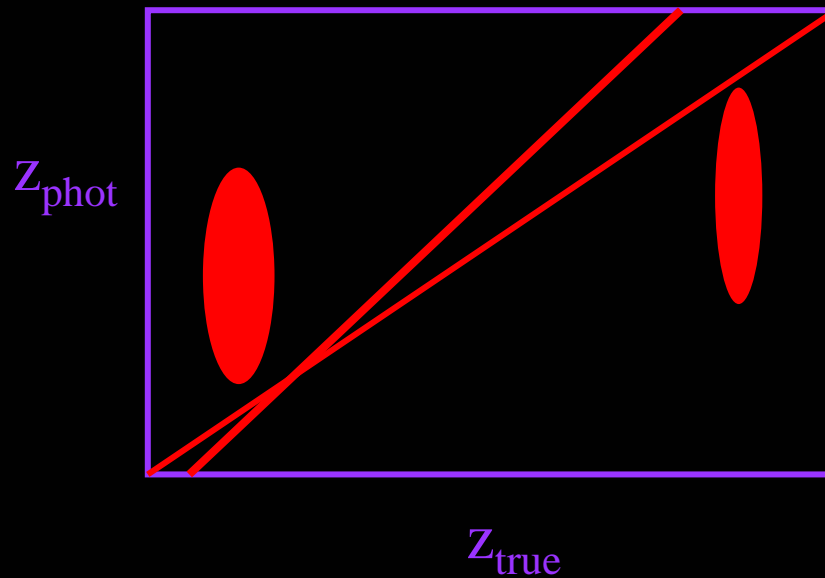


$$C^{\gamma\gamma} = C^{GG} + C^{II} + 2C^{GI}$$

(Bridle & King, 2007; Kitching, Taylor & Heavens 2007)

Challenges: Photometric Redshifts

- Photometric redshifts: calibration, bias, outliers



Abdalla et al (2007)

$$z_{phot} = Cz_{true} + z_{bias}$$

(Abdalla et al, 2007; Kitching, Taylor & Heavens 2007)

Organizational Challenges



- Coordinated effort.
- EU Research-Training Network.
- DUEL (Dark Universe with Extragalactic Lensing)
 - Exploit Cosmological Lensing from CFHTLS, Pan-STARRS, VST-KIDS
 - Plan for future surveys (DUNE...)
 - 8 Network Partners:
 - Edinburgh, Paris, Bonn, Heidelberg, Munich, Leiden, Naples, British Columbia
 - 14 Postdocs & PhD students across network.
 - Training & exchange of methods & data.

Summary

- **Currently:**
 - Accurate 2 & 3D mass maps
 - See growth of structure
 - Cosmological parameters
 - Scaling all of this up for new surveys (Pan-STARRS, VST-KIDS, DES) will be a major challenge.
 - European Network (DUEL) to help do this.
- **Future Aims (PS4, DUNE, LSST):**
 - Map Dark Matter over whole sky to $z \sim 1$.
 - Pin down dark energy to $\sim 1\%$.
 - Test gravitational physics.
 - Measure neutrino mass to $> 0.04 \text{eV}$.
 - Probe initial conditions (inflation).
 - Develop theory and methods.

