Disks in Young Stellar Objects

• IR excess due to disk emission

lack of correlation $A_V \leftrightarrow \text{IR}$ excess near-IR excess correlation with accretion indicator: veiling HST images: proplyds and silhouettes in Orion scattered light images HST images: flared disks mm images, dust mm images, molecules, Keplerian velocity \Rightarrow disk in central potential of star

Millimeter observations and models

• Disk masses from mm observations and parametric models

Assumptions

absorption and emission due to dust particles (same dust/gas ratio as ISM, \approx 1 %) optically thin vertically isothermal

 $T = T_0 (R/R_0)^{-q}$ $\Sigma = \Sigma (R/R_0)^{-p}$, p =3/2 (Hayashi)

Millimeter observations

Flux from annulus at R inclined by i to the line of sight at distance d

$$dF_{
u} = I_{
u} d\Omega = I_{
u} \left(\frac{2\pi R dR}{d^2} \right) \cos i$$

where the specific intensity is

$$I_{
u} = B_{
u}(1 - e^{- au_{
u}/\cos i}) \sim B_{
u} au_{
u}/\cos i$$

and the optical depth

 $\tau_{\nu} = \kappa_{\nu} \Sigma$



Millimeter observations

Total flux is

$$F_{\nu} = \frac{2\pi}{d^2} \int_{R_1}^{R_2} B_{\nu}(T(R)) \Sigma(R) \kappa_{\nu} R \mathrm{d}R$$

• Dependence on frequency: B_{ν} and \rightarrow dust opacity κ_{ν}

• With the disk mass,

$$M_d = \int_{R_1}^{R_2} 2\pi \Sigma R dR$$
$$\nu F_\nu = \frac{4k\nu^3}{c^2} \kappa_\nu M_d T(R_d) \left(\frac{2-p}{2-p-q}\right)$$

 $c^2 = R_d$ and $R_1 << R_2$.

Millimeter observations

$$\nu F_{\nu} = \frac{4k\nu^3}{c^2} \kappa_{\nu} M_d T(R_d) \left(\frac{2-p}{2-p-q}\right)$$

- $F_{\nu}, \kappa_{\nu}, p, q \rightarrow M_d$
- If $\kappa_{\nu} = \kappa_0 (\nu/\nu_0)^{\beta} = \kappa_0 (\lambda_0/\lambda)^{\beta}$,

$$\nu F_{\nu} \propto \nu^{3+\beta}$$

 \Rightarrow slope of the SED in the mm \rightarrow frequency dependence of dust opacity

Millimeter observations and models

- Most used (Beckwith et al 1990) dust opacity $\kappa_0=0.1 {\rm cm}^2 {\rm gr}^{-1}$ at $\lambda_0=250 \mu {\rm m}$
- $M_d \sim 0.01 0.1 {
 m M}_{\odot}$
- Surface density (for p = 3/2)

 $\Sigma = 3.5 (M_d/0.05 M_{\odot}) (R_d/100 AU)^{-2}$

• How valid are assumptions?

Accretion disks

- \bullet Disks in YSO are accreting \rightarrow use theories of accretion disks
- If steady accretion (constant \dot{M}), T(R)

 $T_{vis} = \left(\frac{3GM_*\dot{M}}{8\pi\sigma R^3} \left[1 - \left(\frac{R_*}{R}\right)^{1/2}\right]\right)^{1/4}$ $T_{vis} \propto R^{-3/4}, R >> R_*$

• If disk is optically thick, SED is

 $\lambda F_\lambda \propto \lambda^{-4/3}$

• SEDs of CTTS are flatter than expected from accretion disks



Irradiated accretion disks

with $\dot{M} \sim 10^{-8} M_{\odot} yr^{-1}$, $L_{acc} < 0.1 L_{\odot}$

 $\Rightarrow L_{acc} << L_{*}$

 \rightarrow stellar irradiation important heating agent

 \rightarrow irradiated accretion disks

• For flat disk, irradiation flux

 $F_{i\tau\tau} \sim I_*\Omega_*\coslpha \sim rac{I_*\pi R_*^2}{R^2}rac{h}{R} \propto I_*\left(rac{R_*}{R}
ight)^3$

 α = angle from surface to Rh = height

with $I_* \sim \sigma T^4 \Rightarrow T \propto \frac{R^{-3/4}}{R}$

Disks are flared

• But disks of CTTS are flared (Kenyon & Hartmann 1997) \Rightarrow can capture more stellar radiation than flat disks





Density in the isothermal approximation

Hydrostatic equilibrium in vertical direction

$$\frac{1}{\rho} \frac{\mathrm{d}p}{\mathrm{d}z} = -\frac{GM_*z}{R^3}$$

where $\rho(z,R)$ and p(z,R) are the density and pressure at height z and radius R

if isothermal disk

$$p=
ho c_s^2=
ho (2kT/m)^{1/2}$$

 c_s = isothermal sound speed, m = mass of the particle. In this approximation

$$ho(z,R)=
ho_c e^{-rac{z^2}{2H^2}}$$

where *H* is the scale height:

$$H = \frac{c_s}{(GM_*/R^3)^{1/2}} = \frac{c_s}{\Omega_K} \propto T^{1/2}$$

Flatter SED with irradiation

$$H = \frac{c_s}{(GM_*/R^3)^{1/2}} = \frac{c_s}{\Omega_K} \propto T^{1/2}$$

• if $T \uparrow \rightarrow$ cross section to capture of stellar photons $\uparrow \rightarrow$ disk gets heated

stable solution for the disk surface \rightarrow flared surface

 $T(R) \rightarrow R^{-1/2} \Rightarrow$ flatter SEDs

Irradiated disks are hotter



Kenyon & Hartmann 1987

Vertical structure

• Disks are not vertically isothermal

Stellar radiation enters the disk at an angle θ_0 to the local normal, \rightarrow energy captured

$$F_{i\tau\tau}\sim (\sigma T_*^4/\pi)(R_*/R)^2\mu_0$$

with

$$\mu_0 = \cos\theta_0$$



• a fraction $d\tau_*/\mu_0$ of the stellar flux absorbed at each z

 $\tau_* =$ vertical optical depth at the wavelength of the stellar radiation

Stellar energy deposited in upper layers

• a fraction $d\tau_*/\mu_0$ of the stellar flux absorbed at each z $\tau_* = \text{vertical optical depth at the wavelength}$ of the stellar radiation

• the larger the inclination $\leftrightarrow \mu_0 \downarrow$

 $d au_*/\mu_0\uparrow$ $z(au_*/\mu_0 \sim 1)$ \uparrow \Rightarrow stellar energy is deposited in higher layers



disk

λ

Malbet & Bertout 1991

Wavelength effects

 $\tau_* =$ vertical optical depth at the wavelength of the stellar radiation

- re-emerges at wavelength of local radiation
- $\kappa_*/\kappa_d >> 1$ (d = local radiation)

continuum from $z(\tau_d \sim 1)$ dust opacity increases as λ decreases Dust opacity $\lambda_* \sim 1 \mu m$ (CTTS), $\sim 0.3 \mu m$ (Herbig Ae/Be) $\lambda_d >> \lambda_*$ star + shock $\Rightarrow z(au_*/\mu_0 \sim 1) >> z(au_d \sim 1), \ (au_* = rac{\kappa_*}{\kappa_d} au_d)$ 1 \Rightarrow stellar energy is deposited κ in higher layers the hotter the star \Rightarrow Upper layers get heated $m_{d}^{\kappa_{d}}$

κ. abs

Temperature structure

• Conservation of energy $\rightarrow T(z)$

$$\int \kappa B_{\nu}(T) \mathrm{d}\nu = \int \kappa J_d \mathrm{d}\nu + \frac{\mathrm{d}F_d}{\mathrm{d}z}$$

 $J_d =$ mean intensity of the local radiation.

$$\frac{\mathrm{d}F_d}{\mathrm{d}z} = \Gamma_* = 4\pi\kappa^*\rho J_{*,0}e^{-\tau_*/\mu_0}$$

 Γ_{\ast} = stellar heating (no viscous heating)

- $\kappa^* =$ opacity at stellar wavelength
- $J_{*,0}$ = mean intensity entering the disk

Temperature structure

With

$$J_{*,0} = 1/4\pi \int I d\Omega \sim I_* \Omega_*/4\pi$$

$$\kappa_P(T) \frac{\sigma T^4(z)}{\pi} = \kappa_P(T) J_d(z) + \kappa_P(T_*) \frac{\sigma T_*^4}{\pi} \left(\frac{R_*}{R}\right)^2 e^{-\tau_*/\mu_0}$$

 $\kappa_P = \mathsf{Planck}$ mean opacity $\kappa^* \sim \kappa_P(T_*)$

Calvet et al 1991, 1992

Upper layers

At surface, $J_d << J_{*,0}$, $\tau_*/\mu_0 << 1$,

 $\kappa_P(T)T^4(z) \sim \kappa_P(T_*)T_*^4\left(rac{R_*}{R}
ight)^2$

surface temperature \rightarrow optically thin limit

 \rightarrow the "hot layer" temperature in the 2-level approximation (Chiang & Goldreich 1997)

but T decreases as z decreases

Disk surface

• $T(z,R) \leftrightarrow \mu_0 \leftrightarrow$ surface of the disk $z_s(R)$

 \bullet where $\tau_*/\mu_0\sim 1$ and most of the stellar energy deposited

• size of upper optically thin region above the surface is given by

$\Delta z \sim \mu_0/\kappa_*$

the more inclined the surface \rightarrow the smaller the region



Isothermal approximation

• with more detailed calculation for stellar flux intersected by disk by surface $z_s(R)$

$$F_{irr}(R, z_s) \sim \frac{2\sigma T_*^4}{\pi} \left[\frac{1}{3} \left(\frac{R_*}{R} \right)^3 + \pi \left(\frac{R_*}{R} \right)^2 \frac{\mathrm{d} z_s}{\mathrm{d} R} \right]$$

for $R >> R_*$

for $z_s = nH \rightarrow z_s = z_s(T)$

$$\frac{\mathrm{d}z_{s}}{\mathrm{d}R} = \frac{1}{2} \frac{z_{s}}{T} \frac{\mathrm{d}T}{\mathrm{d}R} \frac{3}{2} \frac{z_{s}}{R}$$

With $F_{irr} = \sigma T^4 \rightarrow$ system for T(R) in the isothermal approximation

 $\rightarrow T(R) \propto R^{3/7}$

Solutions for the vertical structure

• But disks are not isothermal, and $z_s \neq nH$ \rightarrow solution of vertical structure equations for more accurate results

Several groups and approaches. Here, results from D'Alessio et al. Analytical solution of disk vertical structure equations, including irradiation and viscous heating. Iterative approach: find solution for given F_{irr} , i.e., $z_s(R)$, calculate new $z_s(R)$.

• Results for typical CTTS parameters: $M_* = 0.5 M_{\odot}, R_* = 2 R_{\odot}, \dot{M} = 10^{-8} M_{\odot} yr^{-1}$

Extent of the flared surface

* Since κ_* high \rightarrow surface is flared out to a few hundred AU

* although disk becomes optically thin to its own radiation ($\tau_{\rm R}$ < 1) at ~ few × 10 AU

 $\tau_{\rm R} = {\rm Rosseland}$ mean opacity





T (z,R) in optically thick annuli

* Three characteristic temperatures: T_0 (surface) T_{mid} (midplane) T_{phot} , at photoshere, $\tau_d \sim 1$, only defined if disk is optically thick at its own radiation

 $(\tau_{\mathsf{R}} > 1)$

* $T_{mid} >> T_{phot}$ if $\tau_{\rm R} >> 1$ (inner disks regions)

In the diffusion approximation

$$\frac{\mathrm{d}J_d}{\mathrm{d}z} = -\frac{3}{4\pi}\chi_R \rho F_d$$

or

$$\Delta(\sigma T^4)\sim {3\over 4\pi} au_R F_c$$

so, $\tau_R >> 1 \rightarrow T_c > T_{phot}$. T gradient allows viscous flux to escape



T(z,R) in optically thin annuli



When $\tau_R <<$ 1, inner disk \sim isothermal

- $T \propto 1/R^{1/2}$, $R >> R_*$
- but still hot upper layers





D'Alessio et al 1999

Implications of hot upper layers

*Strong features (CO,Silicate) in emission even if disk optically thick *Molecules can exist in upper layers, even if they are adsorbed on grain surface near midplane

Implications of hot midplane in inner disk

 $T_c \sim T_{dust}$, T_{dust} = dust destruction temperature "thermostat effect"

 $H \sim H(T_{dust})$ in inner disk ~ H("rim")

Rim is not significantly "puffed up" => inner disks are not shadowed



confirmed by observations

Disk Mass

Assuming this dependence,





SED @ IR similar for low dM/dt – dominated by irradiation F_{mm} increases with $\Sigma \sim$ dM/dt / α

Log R (AU)

D'Alessio et al 1999

Disk self-absorption

• Expression for disk flux

$$F_{\nu} = \frac{2\pi}{d^2} \int_{R_1}^{R_2} B_{\nu}(T(R)) \Sigma(R) \kappa_{\nu} R \mathrm{d}R$$

 \rightarrow simplification

Assumes disk isothermal Ignores self-absorption of disk emission by outer regions



• Effects of inclination. Edge-on disks selfabsorbed. Stellar scattered light





Dark lane: optically thick disk layers near mid-plane

D'Alessio et al 1999



Dust opacity: mixture of sizes

x(cm⁻² gr⁻¹)

optical

β(λ)

mm λ

Dust: mixture of grain sizes

 $n(a)da = a^{-p}da$

between a_{min} and a_{max}

p = 3.5 (ISM), p = 2.5 (coagulation)





Effect of dust opacity on heating

• Location of disk surface depends on dust opacity at stellar wavelengths

• For dust uniformly distributed in the disk and with a given mixture of grain sizes, the location of the disk surface depends on a_{max} (with fixed a_{min})







 $\kappa(mm) \uparrow$ \Rightarrow higher mm fluxes





Dust growth and settling

Gas in disk subject to radial pressure gradient $dp/dR \Rightarrow V_{orb} < V_K$ Dust tends to rotate at V_K

 \Rightarrow Small particles coupled to gas, large particles rotate at V_K

⇒Intermediate particles feel gas drag, loose J

 \Rightarrow Differences in orbital and radial velocities

 \Rightarrow Particules shock, stick together, grow in size

 \Rightarrow Gravity tends to settle particles to midplane

 \Rightarrow Faster at small radii (large Ω)

Weidenschilling 1997; Dullemond & Dominik 2004

Dust growth and settling



Weidenschilling 1997; Dullemond & Dominik 2004



Vertical optical depth



FIG. 5. Integrated optical thickness above height z, computed using Rosseland mean opacity for the mass loading and size distribution of particles at each level. Vertical distribution changes because of settling; total optical thickness decreases due to particle growth.

Settling – dust evolution in solar nebula Decrease of dust/gas in Lower surface even with small upper layers grains in upper layers 1 Increasing r=30 AU $\zeta_{\rm upp}/\zeta_{\rm st} = 1,0.1,$ 0.01,0.001 $\alpha = 0$ 5 0.8 depletion 0.6 $\rm z_s/R$ Z(AU) 0.4 3 0.2 2 0 Well mixed -2 0 1 2 -1a_{max}=1mm 0 log R (AU) $10^{-5} \ 10^{-4} \ 10^{-3} \ 10^{-2} \ 10^{-1} \ 10^{0}$ 10^{-6} Solids/Gas Mass Ratio ζ D'Alessio et al. 2006 Weidenschilling 1997



D'Alessio et al. 2006

Settling of solids toward midplane



Furlan et al. 2005

Settling of solids towards the midplane: effects on SED

Model slopes for a range of ε and inclinations compared to measured slopes in IRS spectra of Taurus stars Depletion of upper layers: $\varepsilon = \zeta_{upp}/\zeta_{st}$





Furlan et al 2005

Settling of solids toward midplane

Median of Taurus from IRAC fluxes for 60 stars (Hartmann et al 2005) and IRS spectra of ~75 objects (Furlan et al 2005)

 $\epsilon \sim 0.1 - 0.01$ Olivines No settling in wall



Depletion of upper layers: $\varepsilon = \zeta_{upp}/\zeta_{st}$

Furlan et al 2006

Dust growth and settling



Weidenschilling 1997



Inclination effects in settled disks



D'Alessio et al. 2006

High accretors: DR Tau

Silicate **emission** and high far-IR flux because of irradiation by high energy radiation from accretion shock



Emitting region decreases with settling

•As degree of settling increases, disk flux comes from a smaller region of the disk







Wall at dust sublimation radius



Dust destruction radius: optically thin expression

$$R_{p} = [L_{*}/4 \pi \sigma \kappa_{i}/\kappa_{d}]^{1/2}/T_{sub}^{2}$$

Including accretion shock emission and local radiation field:

 $R_{p} = [(L^{*}+L_{acc})/4 \pi \sigma (2+\kappa_{i}/\kappa_{d})]^{1/2}/T_{sub}^{2}$

Muzerolle et al 2005



And shape of wall! Isella & Natta

Wall emission in near-IR



Dust evolution in inner disk



SED evolution:comparison at different ages



SED evolution: inner disk

Decrease of median slope with age: consistent with decrease of dM/dt and dust settling in inner disk

Hernandez et al 2006b



SED evolution



SED evolution

Present evidence:

As a given population ages, the fraction of remaining disks tend to have lower accretion rates and their dust more settled towards the midplane

But fraction of remaining disks decreases with time. What happened to the other disks?

Transition disks

Transition disks?

Lack of significant excess flux below 10 μm
But flux comparable to the median of Taurus at longer wavelengths

Model:

- •Clearing of the innermost, hotter disk regions
- •Truncated outer optically thick disk
- •Wall at truncation radius illuminated frontally by star

Transition disks





Spectra from IRS on board Spitzer



More disks in transition in Taurus

IRS spectra finely maps wall region



 $R_w \sim 24AU$ outer disk + inner disk with little dust + gap (~ 5-24AU)

Rw ~ 3 AU only external disk but accreting star

Calvet et al 2005

Detection of predicted hole on GM Aur with SMA



Search of transitional disks in large populations: IRAC-MIPS 24 observations of clusters in a range of ages



Filter transmissions

Photosphere

-10.5

-11.5

IRAC

8 10

 $\log \lambda(\mu m)$

6

MIPS

20

0

0.5

0.5 1 [5.8] - [8]

1.5

Search of transitional disks in large populations: IRAC-MIPS 24 observations of clusters in a range of ages



Inner disk clearing



Fraction of accreting transitional disks $\sim 1\%$

Briceno et al 2005

Observations of transition disks in populations of ages 1-10 Myr indicate

timescale ~ $N_{transition}/N_{total} x$ age ~ few 10⁵ yrs \Rightarrow Rapid phase

Accretion onto star is turned off quickly during transition phase (most objects not accreting)

Constraints for models

Inner disk clearing: planet(s)?

Giant planet forms in disk opening a gap

Wall of optically thick disk = outer edge of gap at a few AU



Bryden et al 1999

Inner gas disk with minute amount of small dust – silicate feature but little near IR excess, bigger bodies may be present

Inner disk clearing: planets?

•Tidal truncation by planet

•Hydrodynamical simulations+Montecarlo transfer – SED consistent with hole created and maintained by planet – GM Aur: $\sim 2M_1$ at ~ 2.5 AU – Rice et al. 2003



Inner disk clearing: planets

CoKu Tau 4, wall at ~ 10 AU No inner disk



D'Alessio et al. 2005



Planet-disk system with planet mass of 0.1 M_{jup} for CoKu Tau 4 Quillen et al. 2004

Inner disk clearing: planets?

Planet formation can explain:

- •SEDs of transition disks
- short timescale for transition phase ~ run-away gas accretion/gap opening
- •rapid disappearance of inner disk, viscous time scale at gap, increased efficiency of MRI in low opacity inner disk

Problems: outer disk may make planet migrate inwards in viscous timescale, small α ?

Inner disk clearing: photoevaporation of outer disk?



UV radiation photoevaporates outer disk When mass accretion rate (decreasing by viscous evolution) ~ mass loss rate, no mass reaches inner disk

 $R_g \sim G M_* / c_s^2 (10000K) \sim 10 AU (M_*/M_{sol})$



Inner disk clearing: photoevaporation of outer disk?



Prediction: rapid decrease of mass accretion rate = > most transitional disks not accreting



Clarke et al 2001

Inner disk clearing:photoevaporation of outer disk?

Prediction: low mass accretion rate and mm flux in transitional disks





Clarke et al 2001



Summary

•Protoplanetary disks are irradiated emission disks

•For typical accretion rates, stellar (and accretion shock irradiation controls the heating)

•Accretion rates onto the star constrain the surface density

•Although a minor component of the material, dust controls absorption and emission, ie, heating of the disk

•Dust properties can be inferred from the SEDs

•As a given population ages, the fraction of remaining disks tend to have lower accretion rates and their dust more settled towards the midplane

•Fraction of remaining disks decreases with age •Can transition disks help understand how disks dissipate?

Summary

•Great progress in understanding disk evolution •Spitzer data crucial

•Disks evolve accreting mass onto star and dust growing and settling to midplane

•At some point, disk enters into transitional phase, rapidly turning off accretion and clearing up inner disk

•Alternative models for clearing are planet formation and photoevaporation of outer disks. Present evidence may favor planet formation.

•Characterization of properties of transitional disks in large samples of different ages may settle the issue



•More dust processing as dust in disk evolves

•Where is processing taking place?

exposure to high stellar high energy radiation? shocks?

processing inside planetesimals (Bouwman et al 2003)?

Processing in inner disk

•Silicate feature formed in innermost disk – also flux $\lambda < 10 \ \mu m$ •As degree of settling increases, disk flux comes from a smaller region of the disk



Upper layers are hotter than regions where the continuum form

Radiation enters at angle to local normal: deposits at $\tau_* / \mu_0 \sim 1$, $\mu_0 = \cos \theta_{0,,,}$, $\tau_* \sim \mu_0$, $\mu_0 << 1$

•Stellar energy is deposited in upper levels





Disk vertical structure equations

The disk energy balance equation is

$$\frac{dF}{dz} = \Gamma_{\rm vis} + \Gamma_{\rm ion} + \Gamma_{\rm irr} , \qquad (3)$$

where F is the total flux given by the sum of the radiative, convective, and turbulent energy fluxes (DCCL). Here, $\Gamma_{\rm vis}$ is the heating due to viscous dissipation (e.g., Frank, King, & Raine 1992), $\Gamma_{\rm ion}$ is the heating due to ionization by cosmic rays and radioactive decay (Nakano & Umebayashi 1986; Stepinski 1992), and $\Gamma_{\rm irr}$ is the heating by irradiation.

Disk vertical structure equations

$$\frac{dP}{dz} = -\rho g_z , \qquad (9)$$

where P is the gas pressure, g_z is the z component of the stellar gravity, i.e., $g_z = GM_* z/(R^2 + z^2)^{3/2}$, where M_* is the stellar mass, and we have neglected radiation pressure and the disk self-gravity.

Particle motions



FIG. 1. Particle velocities as functions of size in the model nebula at 30 AU. Particles are assumed to have a fractal structure at sizes 10^{-2} cm, and constant density 0.7 g cm^{-3} at d > 1 cm. Dotted line: thermal velocity at $T = 50^{\circ}$ K. Solid line: radial velocity, with peak value equal to $\Delta V = 54 \text{ m scc}^{-1}$ at $d \simeq 10^2$ cm. Changes in slope are due to variation of particle density ($d \le 1$ cm) and transition from Epstein to Stokes drag law ($d \sim 10^5$ cm). Dashed line: transverse velocity relative to pressure-supported gas. Short dashes: escape velocity from the particle's surface.



FIG. 4. Deviation of the gas velocity from the Kepler velocity in the central plane of the nebula. At t = 0, ΔV has the "free-stream" value of 54 m sec⁻¹. Formation of the dense particle layer drags the gas with it, decreasing ΔV to $\simeq 10$ m sec⁻¹. As their mean size increases with time, the particles decouple from the gas, allowing ΔV to increase. Dashed line: turbulent velocity induced by shear between the particle layer and surrounding gas.



•Many parameters involved – general idea of physical processes