



**Data Analysis
for
Space Exploration of the Cosmic Microwave Background
in satellite missions
COBE, WMAP, and Planck**

Krzysztof M. Górski

Jet Propulsion Laboratory/Caltech

Pasadena, CA

&

Astronomical Observatory, Warsaw University, Poland



CMB data analysis lectures

Saturday: General Introduction

Sunday: Modeling Effective Beams, Component Separation

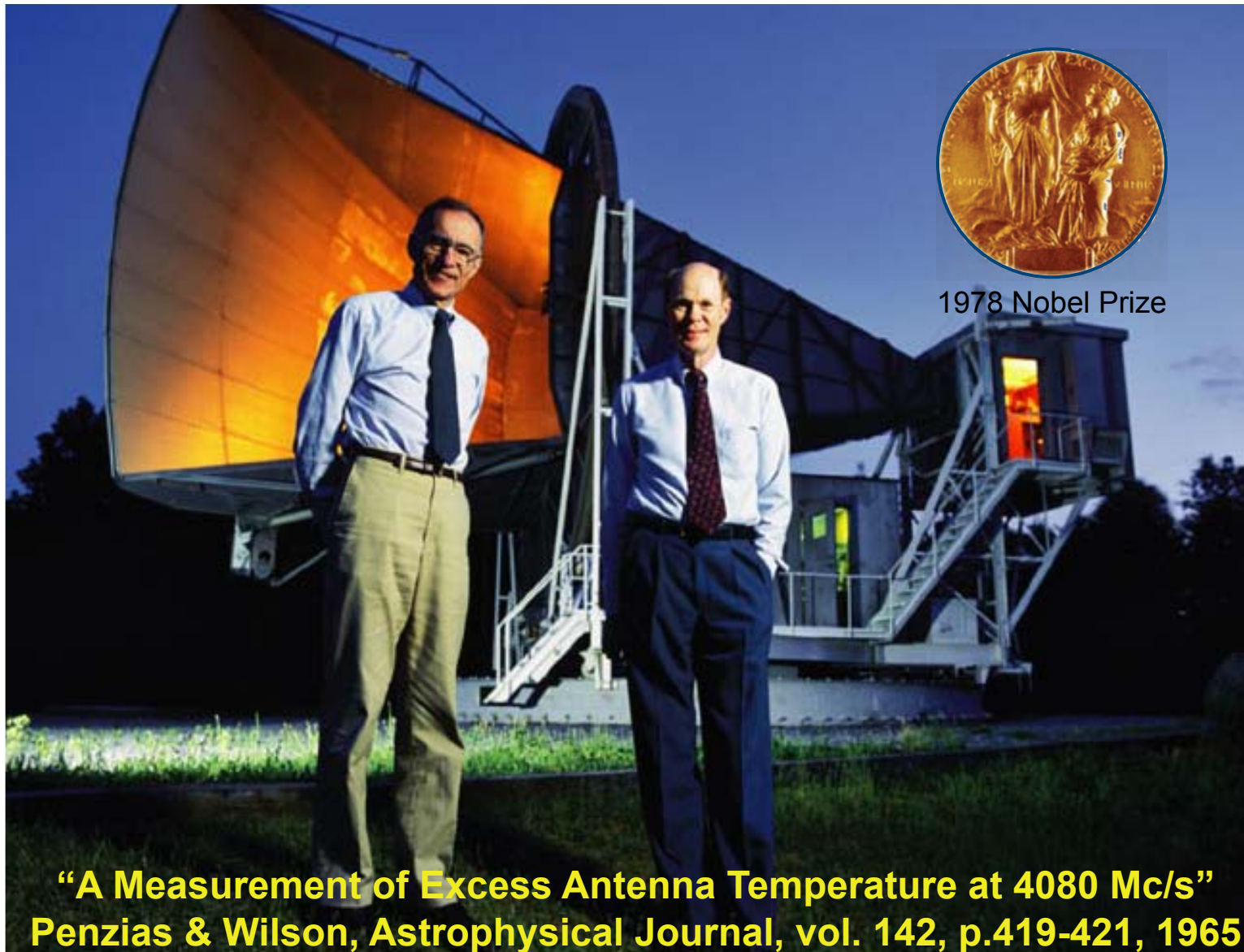
Monday: Likelihood, Power Spectrum Estimation, Point Source Extraction, Summary



CMB



1965: Discovery of the CMB



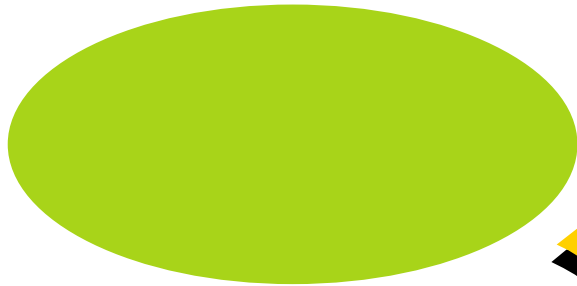


Emerging Structure in the Universe



Smooth Gas at $t \sim 400,000$ yrs

$$T_0 = 2.725 \pm 0.001 \text{ K}$$



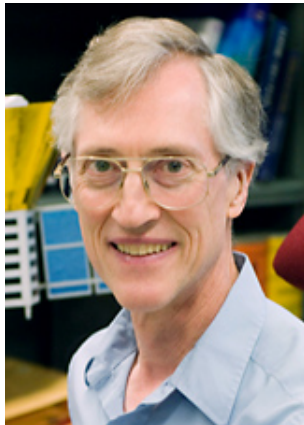
Galaxies & Clusters since $t \sim 1\text{-}2$ Byrs



HOW COME?

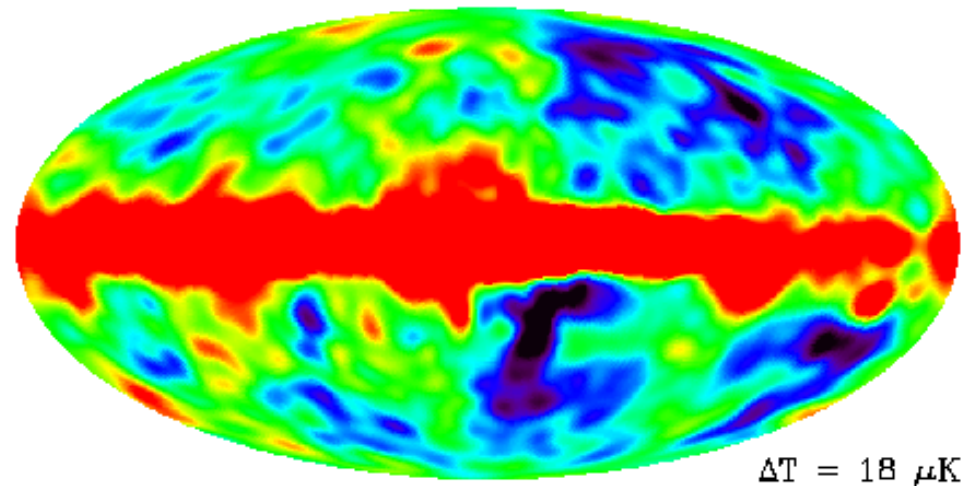
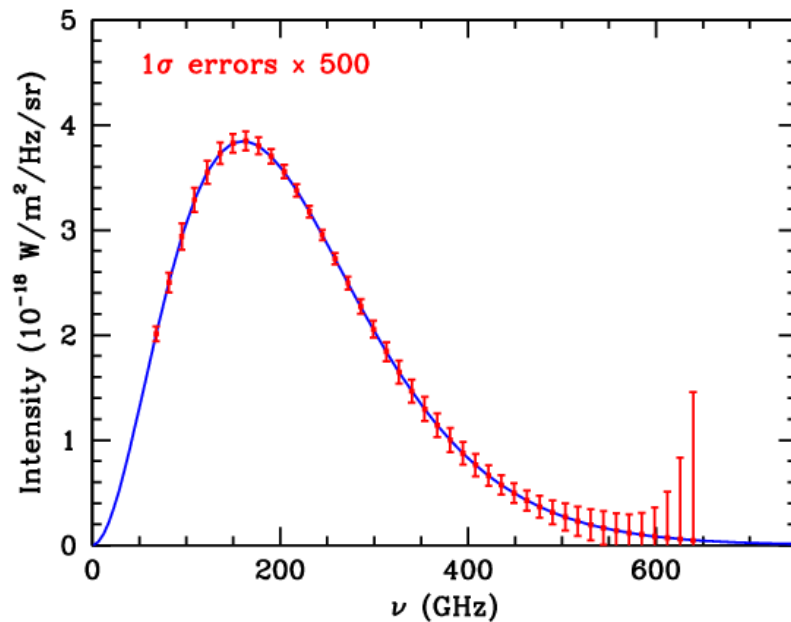
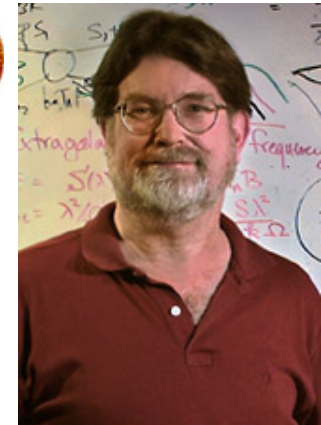


... and then there was COBE ...



Nobel prize in Physics, 2006, awarded to
John Mather and George Smoot

“for their discovery of the blackbody form
and anisotropy of the cosmic microwave
background radiation”





CMB drives a revolution in our understanding of the Universe



- **Existence of CMB**
 - One of the pillars of the hot big-bang model (expansion, origin of light elements, &CMB)
 - A snap-shot of the universe at the earliest epoch accessible to direct astronomical observation
- **Measurement of the black-body spectrum**
 - $T = 2.725 \pm 0.001$ K, deviations $< 10^{-4}$
 - Sets the temperature scale of the Universe
 - Only cosmological parameter known to better than 1%!
 - Rules out significant energy injection below $z \sim 10^7$.
- **Measurement of the anisotropy**
 - Shrunk substantially the range of viable cosmological models.
 - Gravitational instability in a dark matter dominated Universe formed large-scale structure seen by e.g. 2dF or SDSS.
 - The fluctuations are of the form predicted by inflation. (?)
 - The large-scale structure of space-time is “simple”. (?)
- **Precise normalization of large-scale structure in the universe**

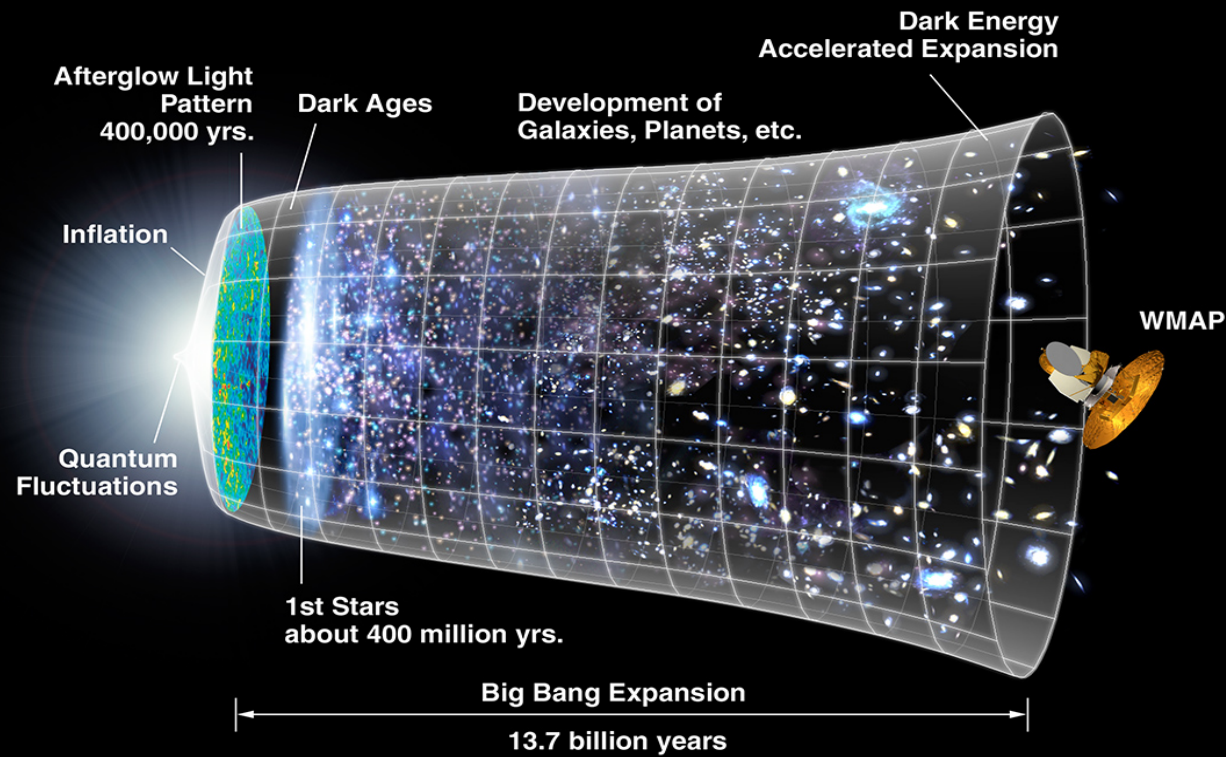
All right. But apart from the sanitation, the medicine, education, wine, public order, irrigation, roads, the fresh water system, and public health . . .

What have the Romans ever done for us?

Reg, spokesman for the People's Front of Judea



CMB Timeline for the Universe



NASA/WMAP Science Team



The angular power spectrum of the CMB anisotropy



- Current measurements are quite consistent with the primary fluctuations in the CMB being a Gaussian random field.
- The primary fluctuations in the CMB are thus well described by their angular power spectrum.

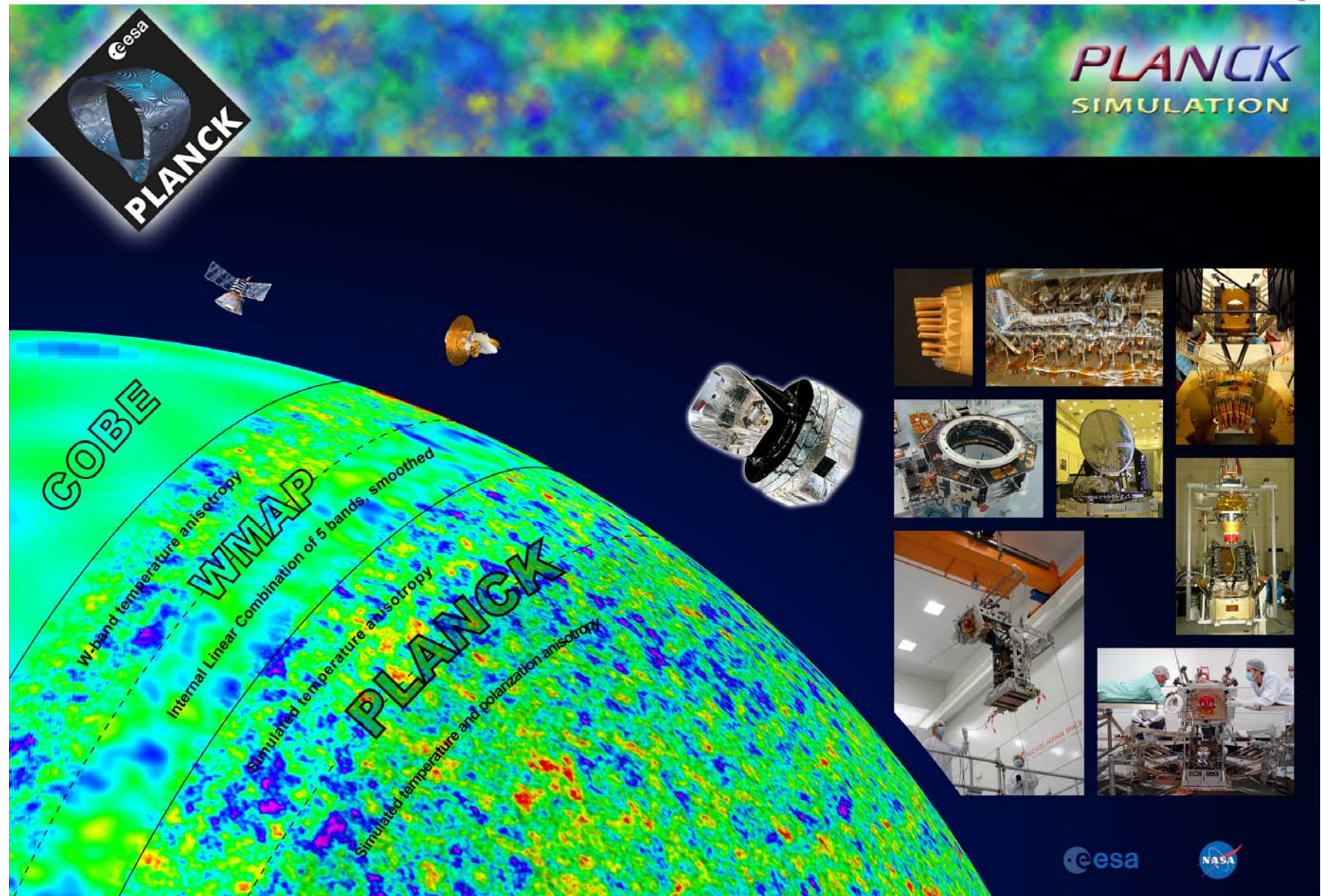
$$\frac{\Delta T}{T} \equiv \sum_{\ell m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

Curved sky analogue of FT

$$\langle a_{\ell m} a_{\ell' m'} \rangle = C_{\ell} \delta_{\ell \ell'} \delta_{m m'}$$

Statistical isotropy

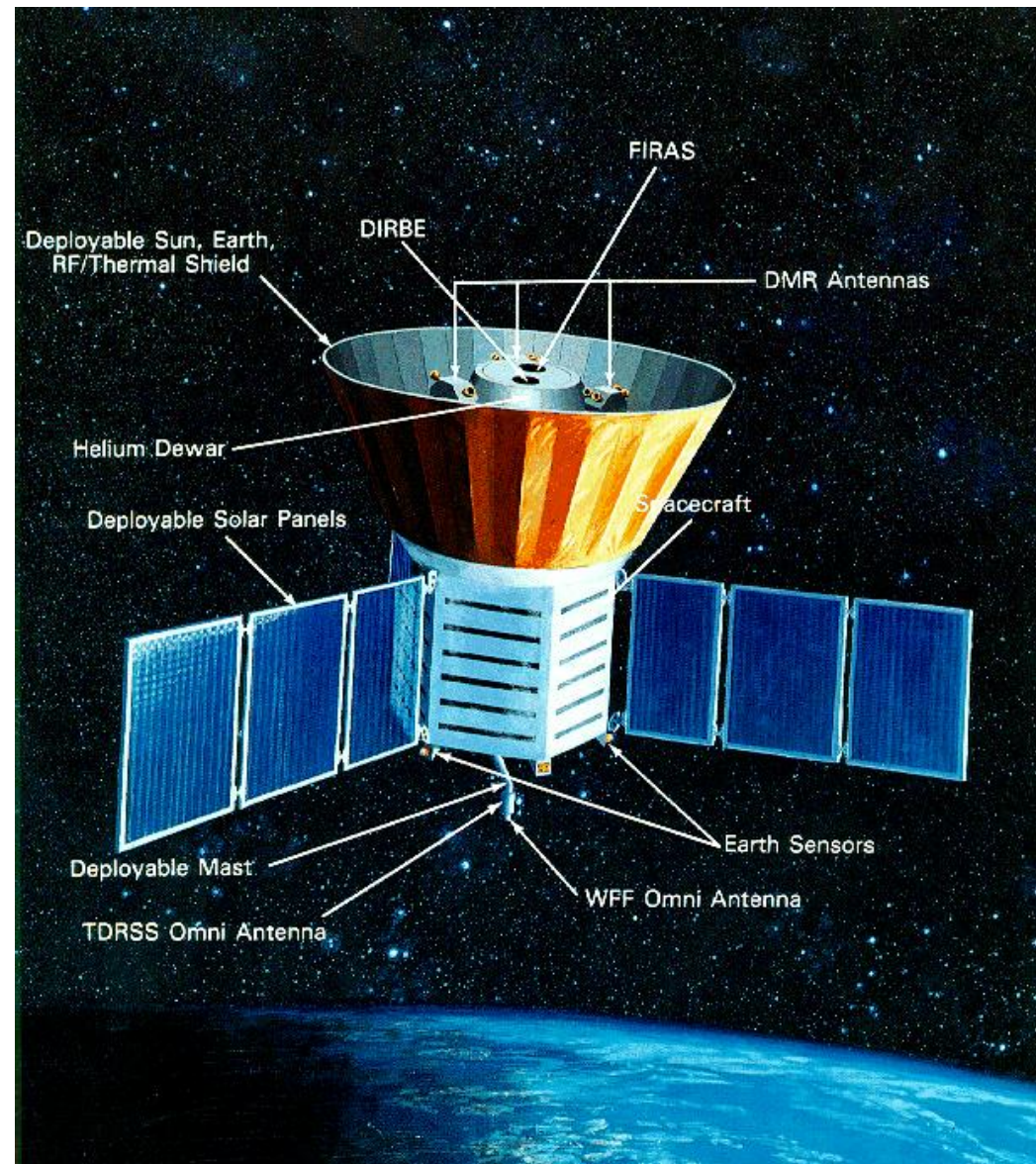
Rotational invariance





COBE

- COBE Satellite, 1989-1995
- FIRAS & DIRBE - < 1 year
- DMR - ~4 years
- COBE's motion -> scanning the sky with DMR
 - 'Bore' angle - 30 deg
 - Precession angle - 86 deg
 - Spin period - 73 sec
 - Precession period - 104 min

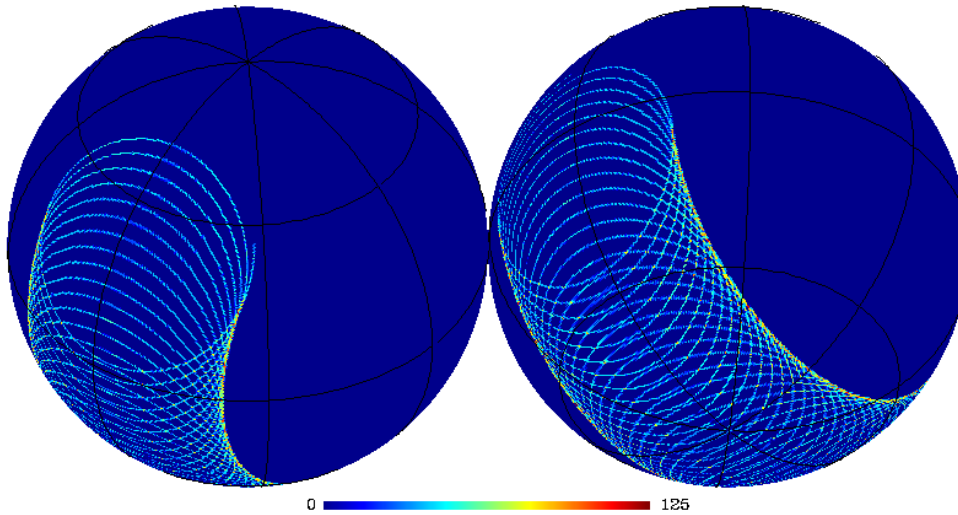




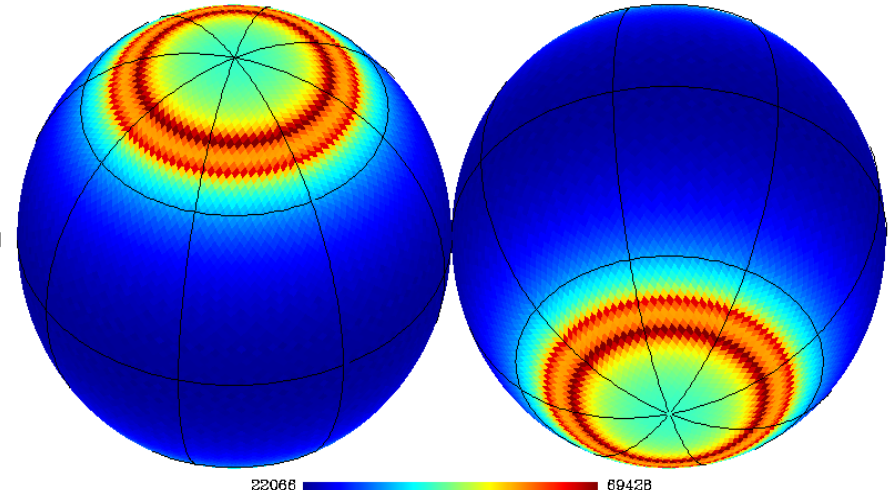
Scanning the sky with COBE



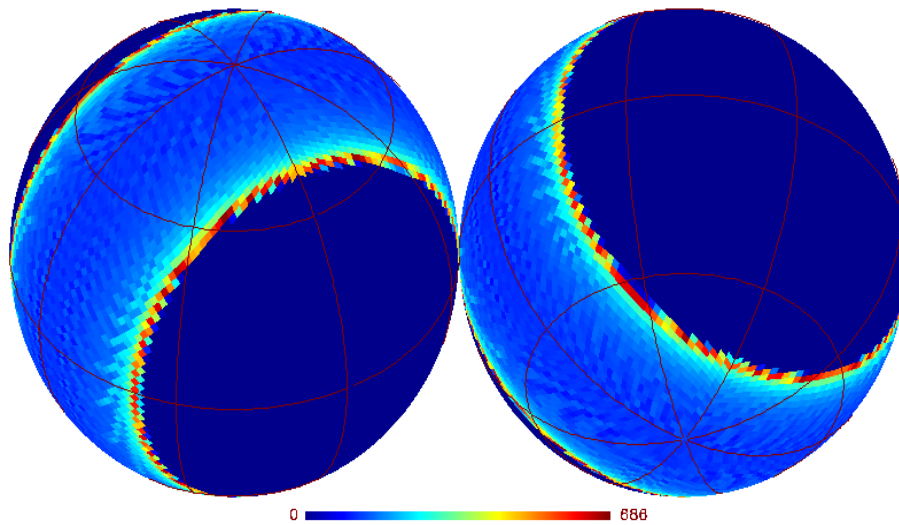
COBE-DMR 1 hr



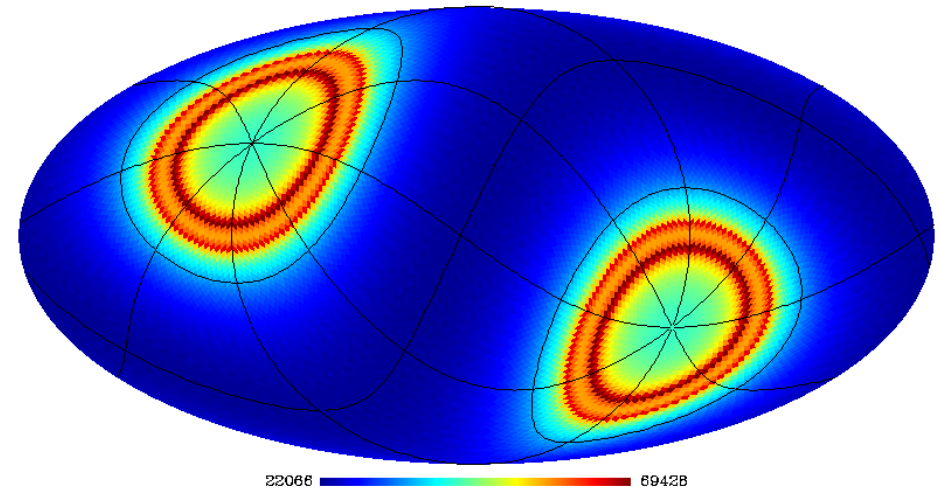
DMR 1yr

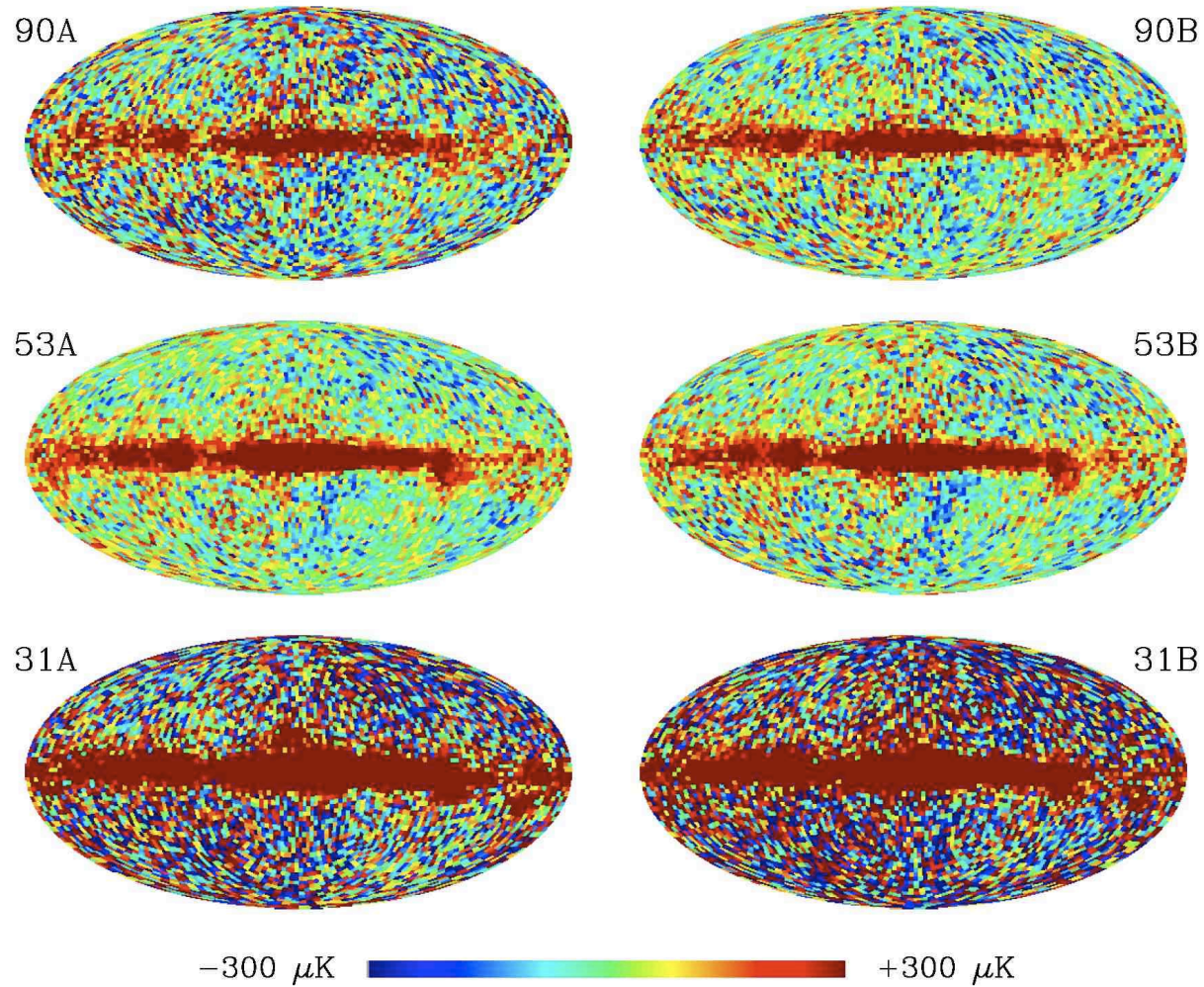


DMR 1day



DMR 1yr





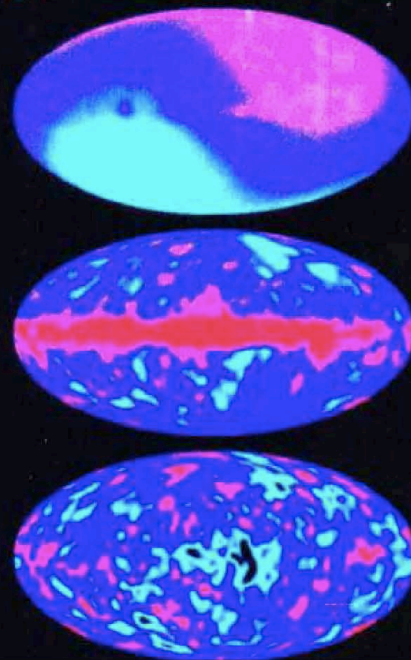


COBE-DMR Delivers ...



PHYSICS TODAY

JUNE 1992



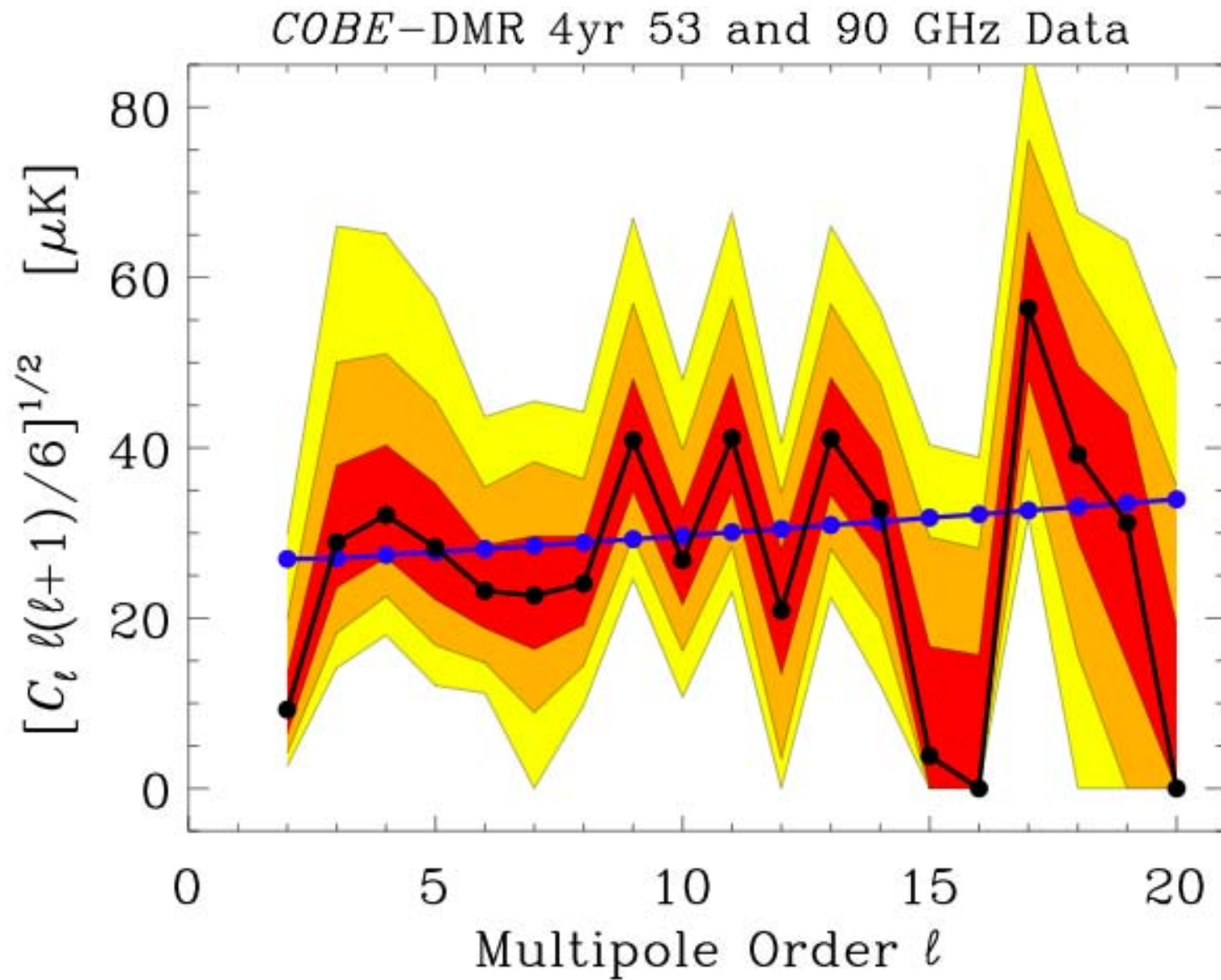
Sky map from DMR,
 $2.7 \text{ K} \pm 0.003 \text{ K}$

Doppler Effect of Earth's
motion removed ($v/c =$
 0.001)

Cosmic temperature/density
variations at 389,000 years,
 $\pm 0.00003 \text{ K}$

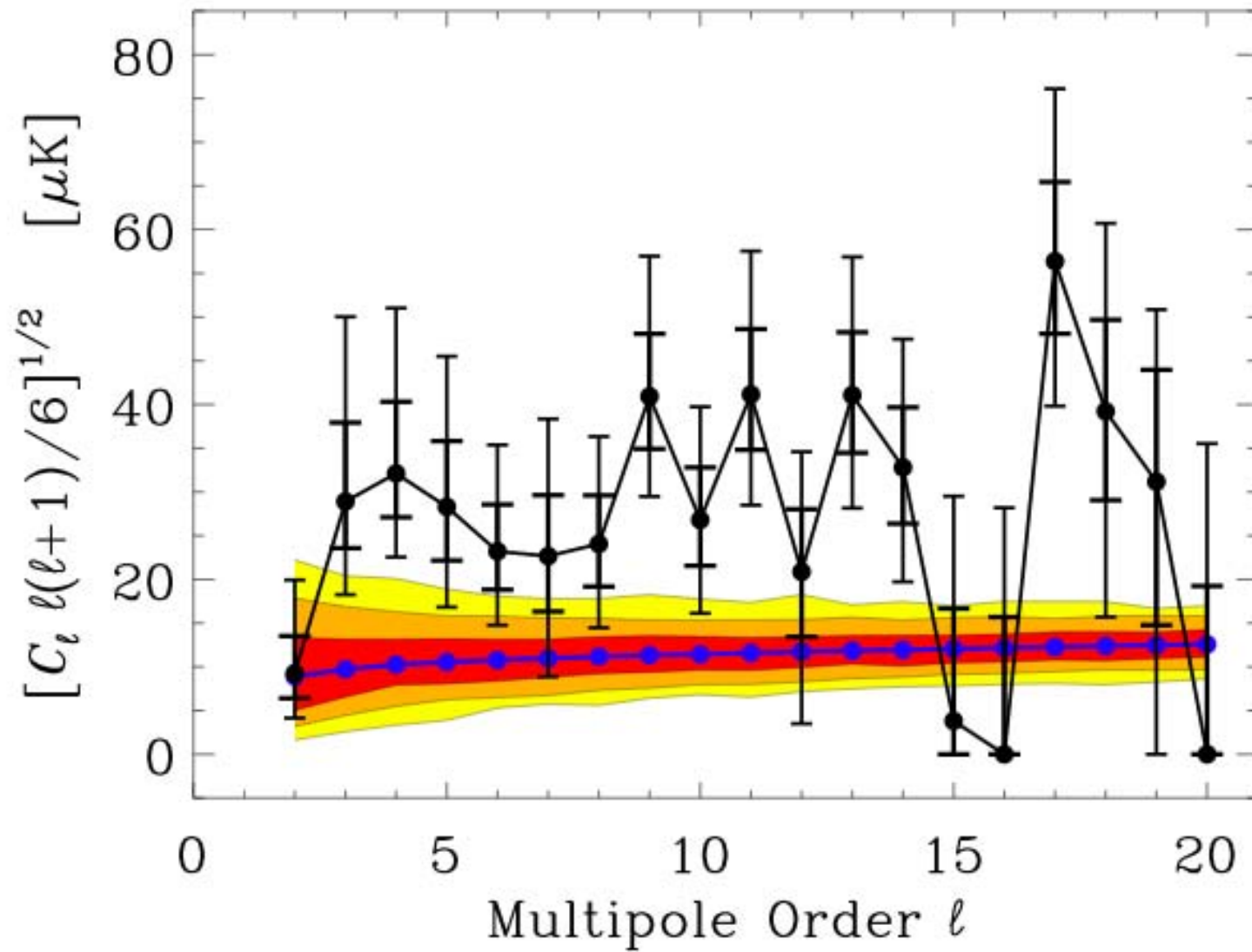
Lecture 2006

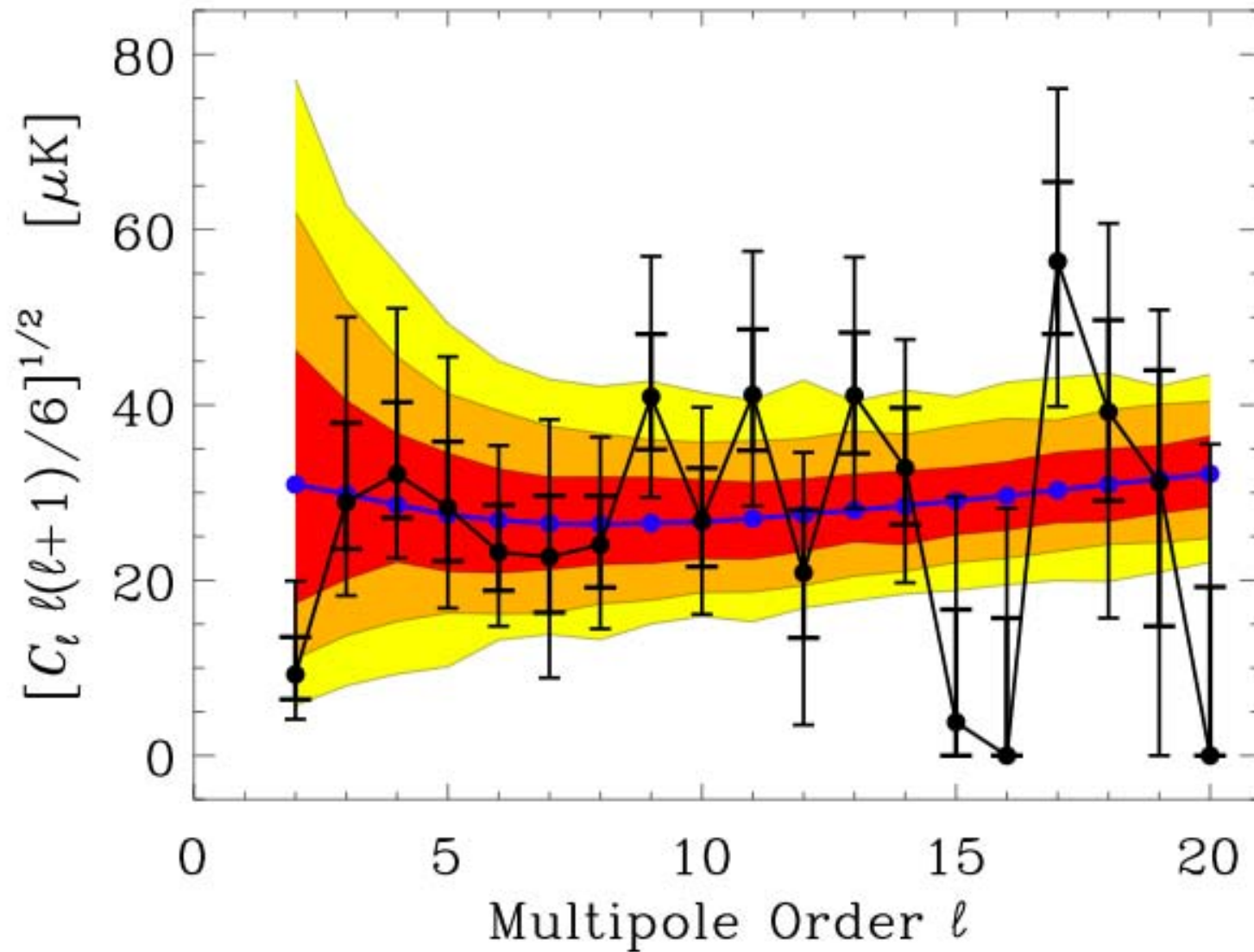
52





... comparison to biased-CDM theory



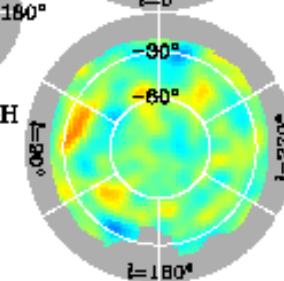
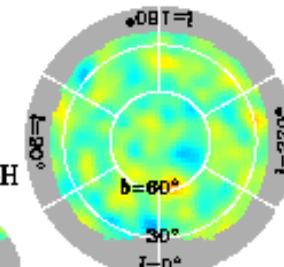
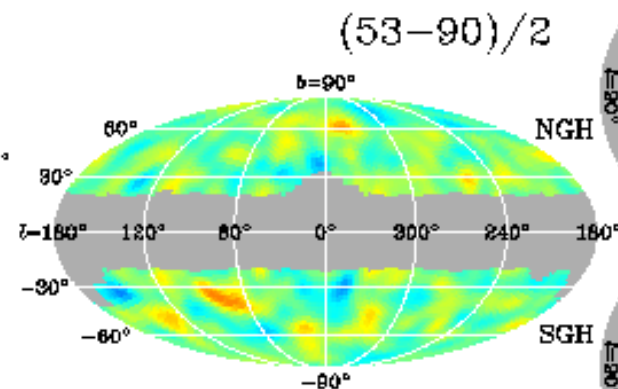
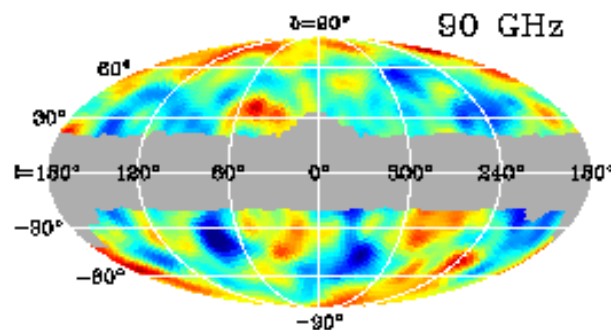
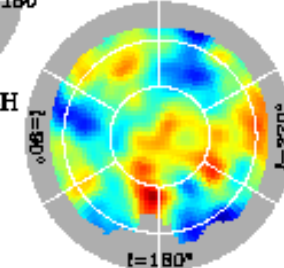
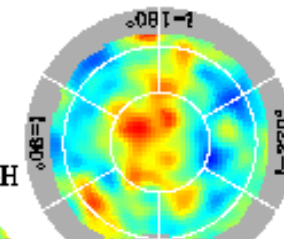
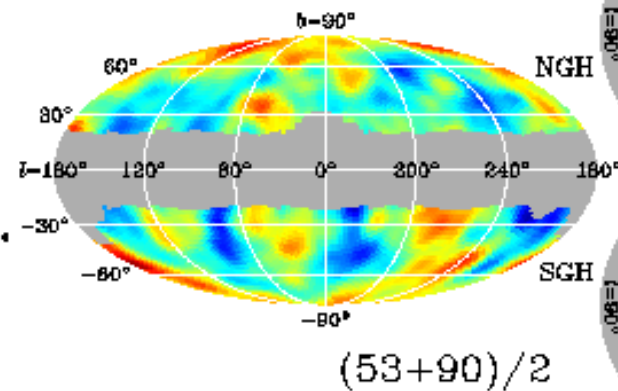
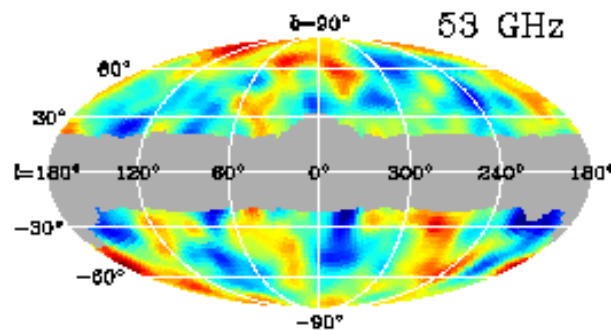




Last scattering surface according to COBE-DMR



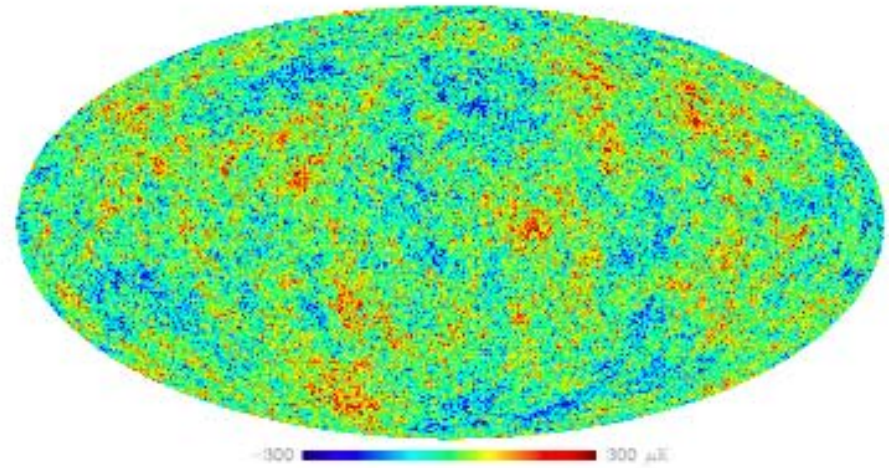
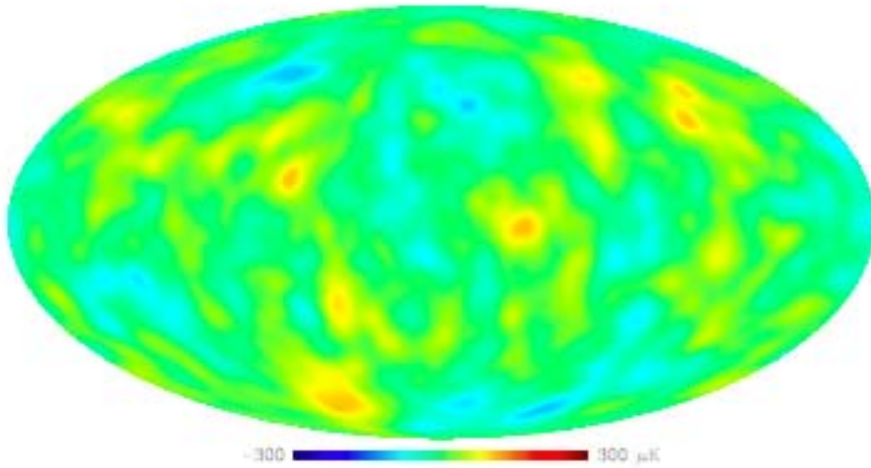
COBE-DMR 4-Year PE-Filtered Sky Maps



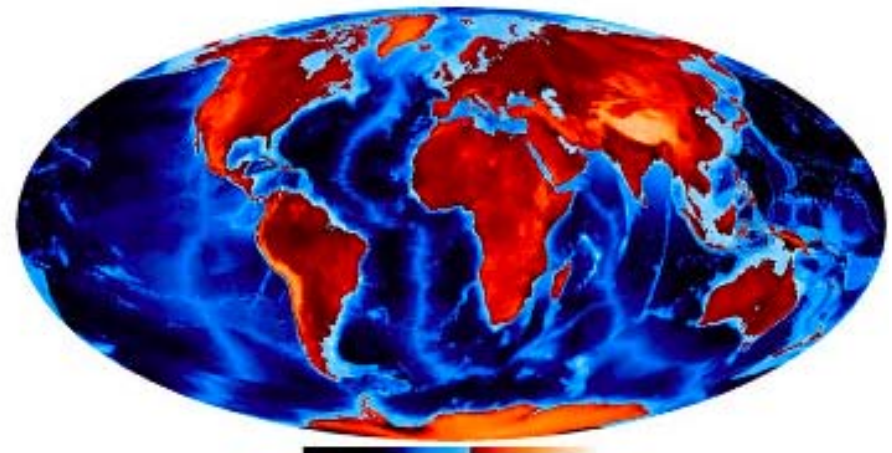
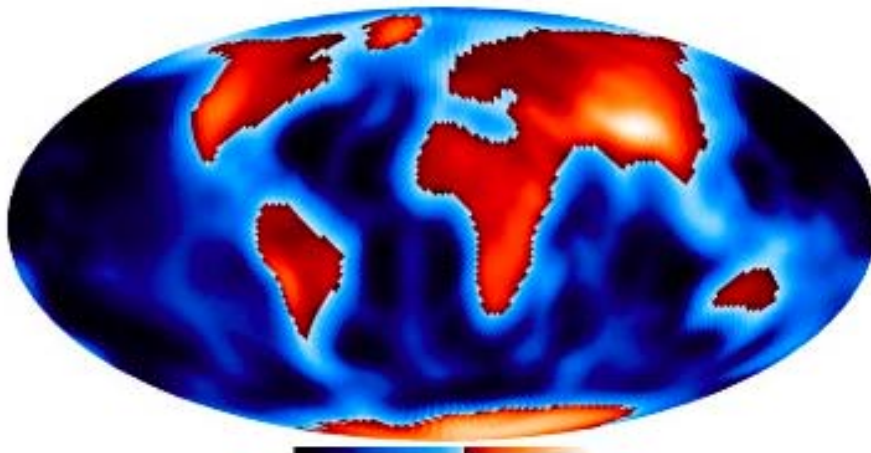
K.M. Gorski 1996

-100 μK 100 μK

Proceedings of the XXXIst Recontres de Moriond



After COBE - We wanted more ...

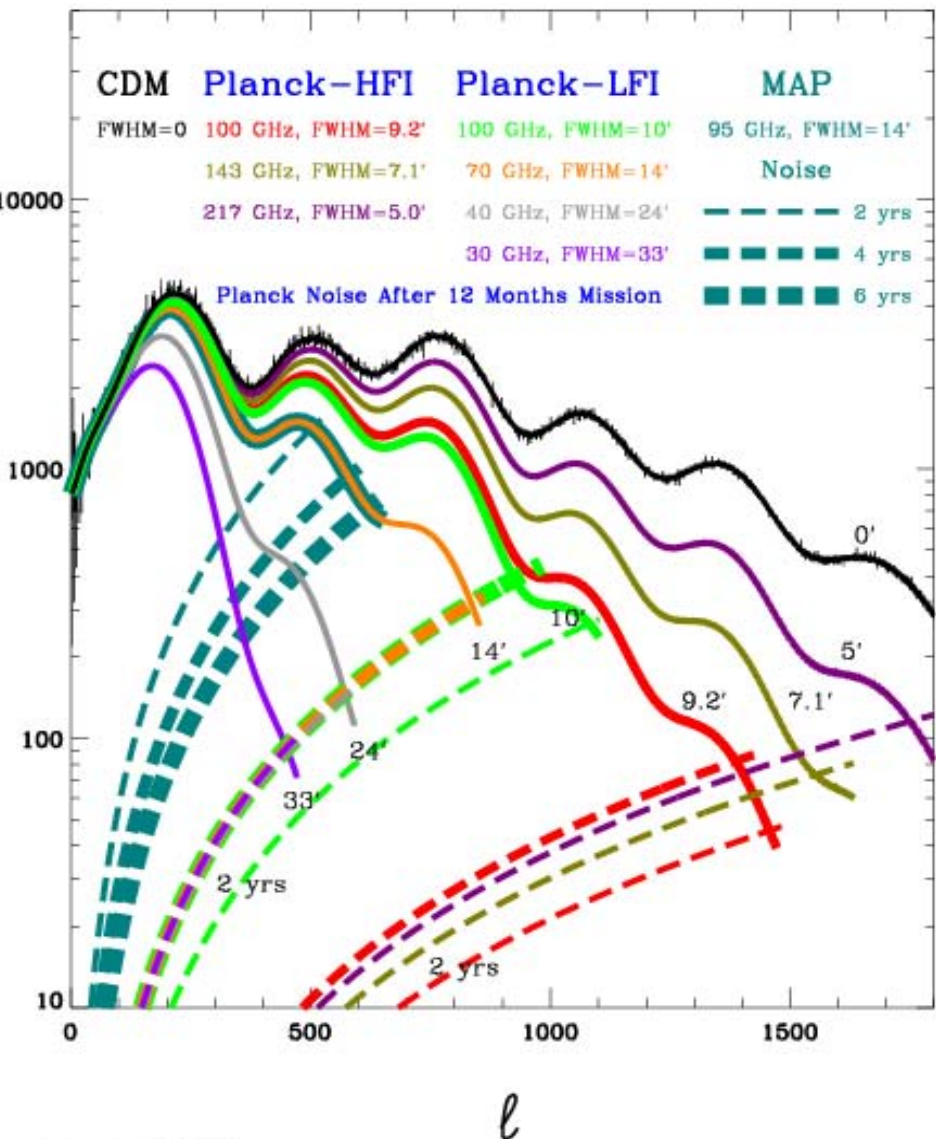
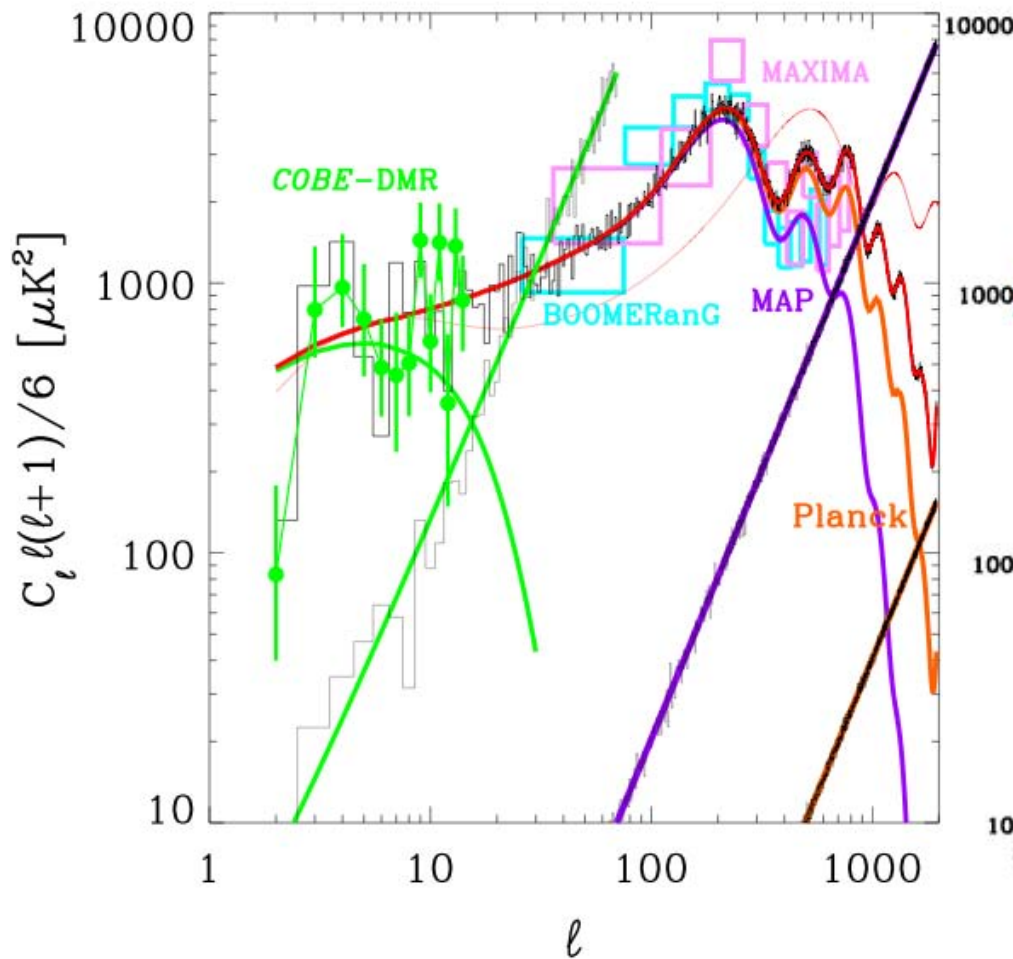


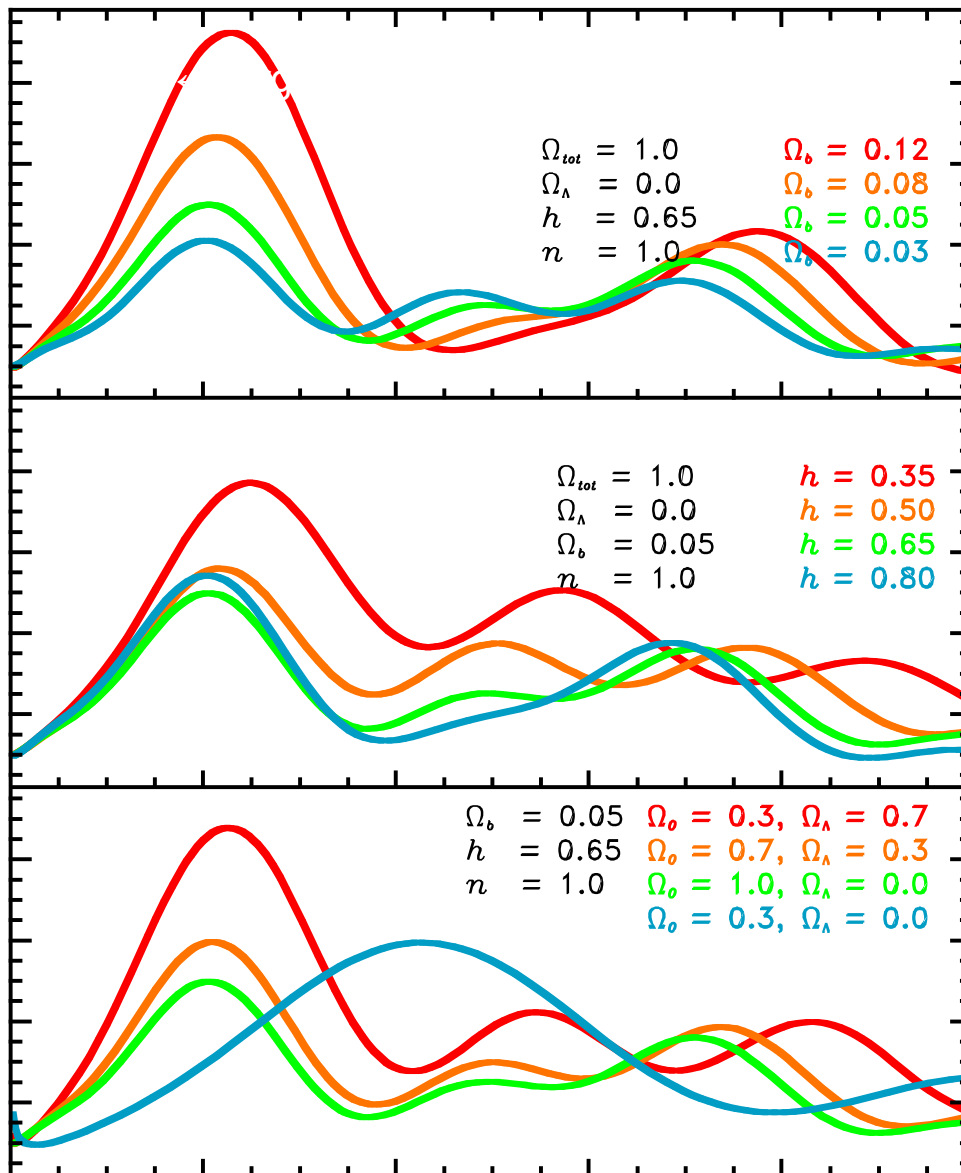


COBE made us want more ...

• What was required to make progress?

- Much more angular resolution
- Much less noise





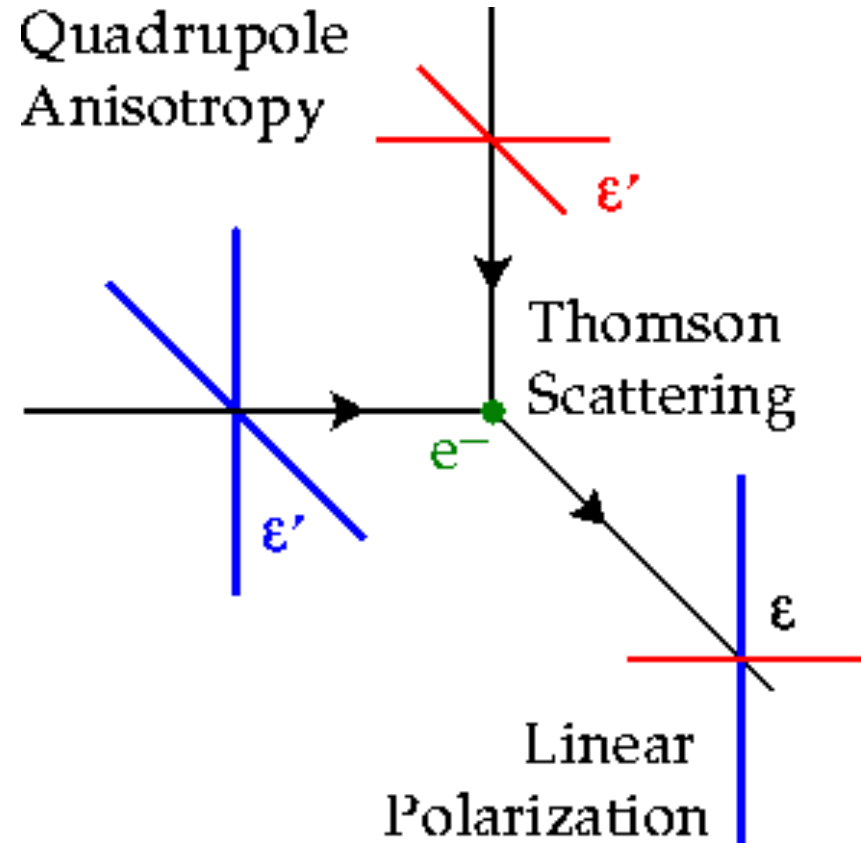
CMB temperature fluctuations on small angular scales (< 2 deg) depend strongly on cosmological parameters - hence, the anisotropy measurements can be used to determine the values of parameters that describe the observable universe.

In the presence of anisotropy we expect scattering to generate (linear) polarization.

Polarization provides a prediction, a cross-check and further information about conditions at last-scattering and reionization.

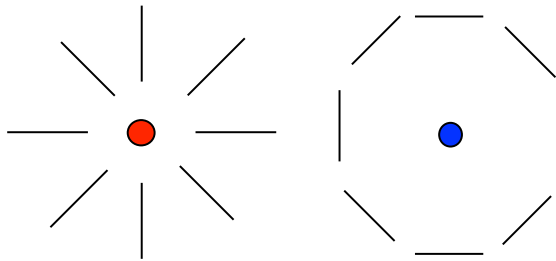
Rees (1968)

Kaiser (1983)

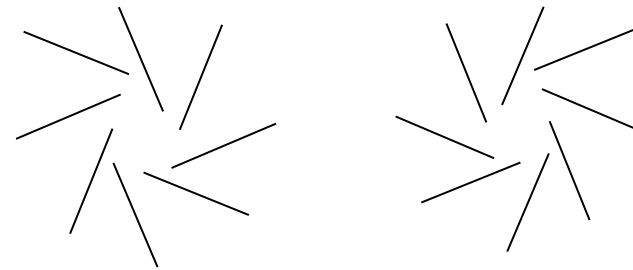


Hu & White (1997)

Polarization is made up of two “modes”, referred to as E- and B- modes because of their global parity properties.



E-modes



B-modes

Note that E-modes have no handedness, whereas B-modes do and thus cannot be generated by scalar (density) perturbations.

Hence, B-mode discovery would establish the new source for perturbations - tensor perturbations, i.e. primordial gravity waves.

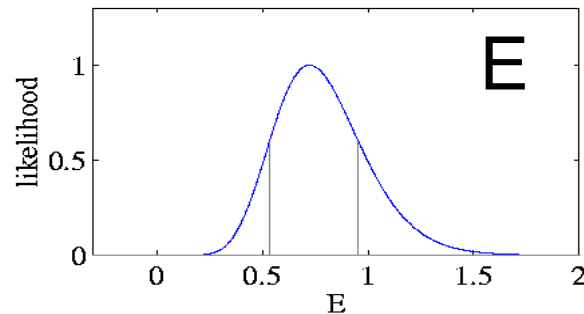
There are those who would call that “a smoking gun of inflation” ...



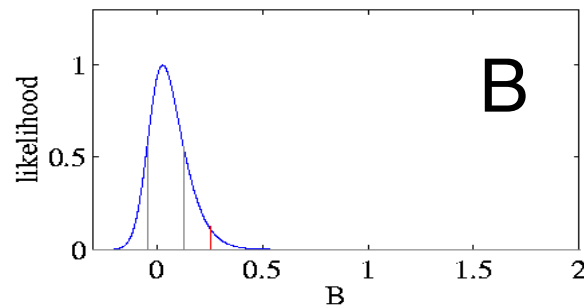
Polarization: first detection by DASI



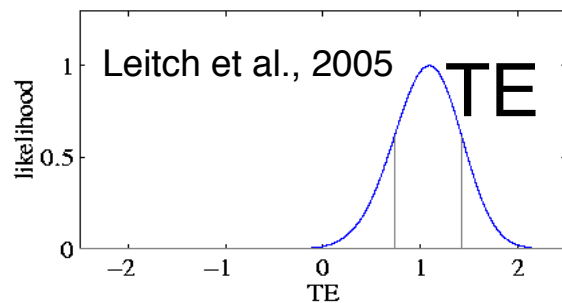
Single shaped 1-bin



6.3 σ
detection
consistent
with theory.

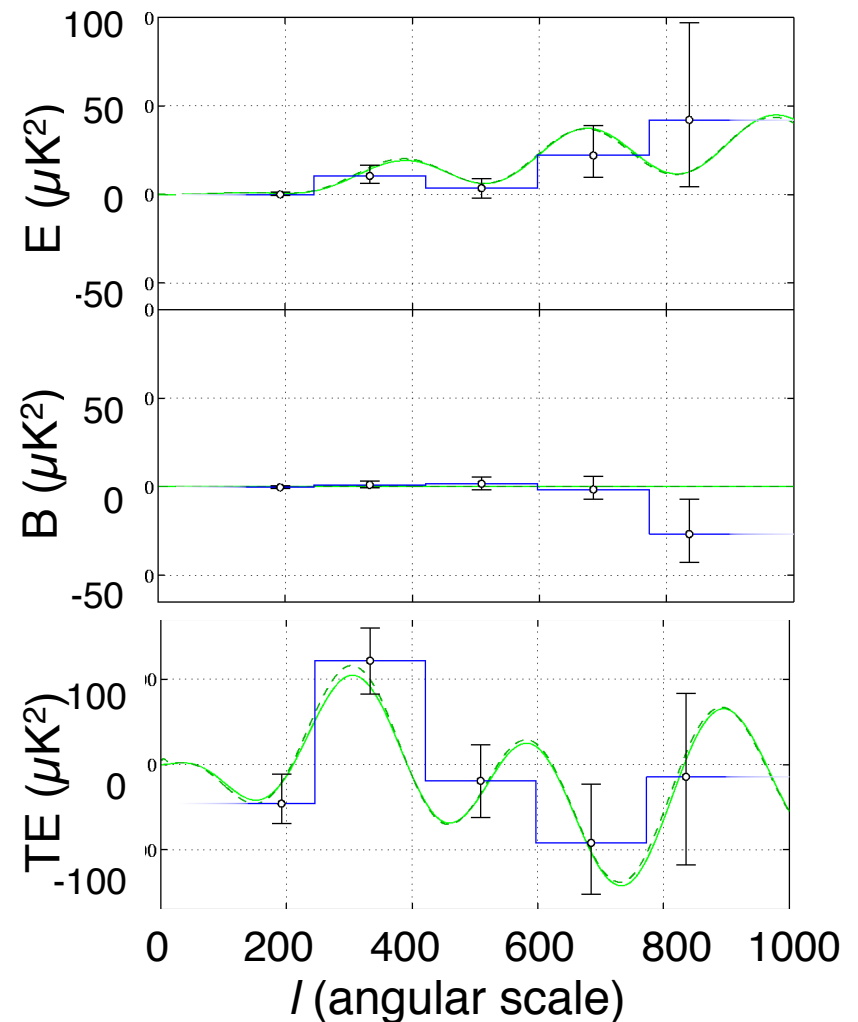


Consistent
with zero
(theory)



2.9 σ
detection
consistent
with theory

Five 1-bins

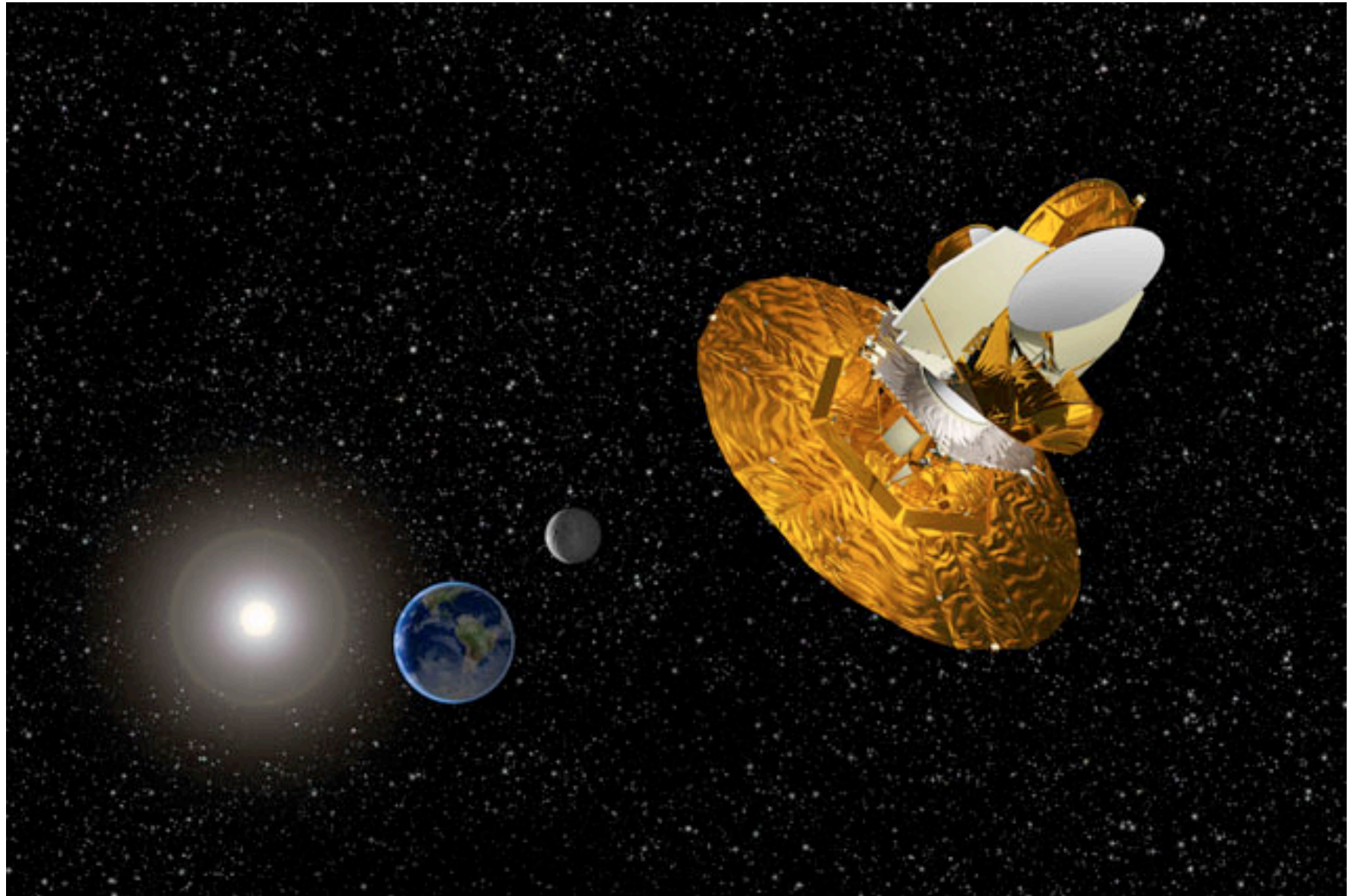




WMAP

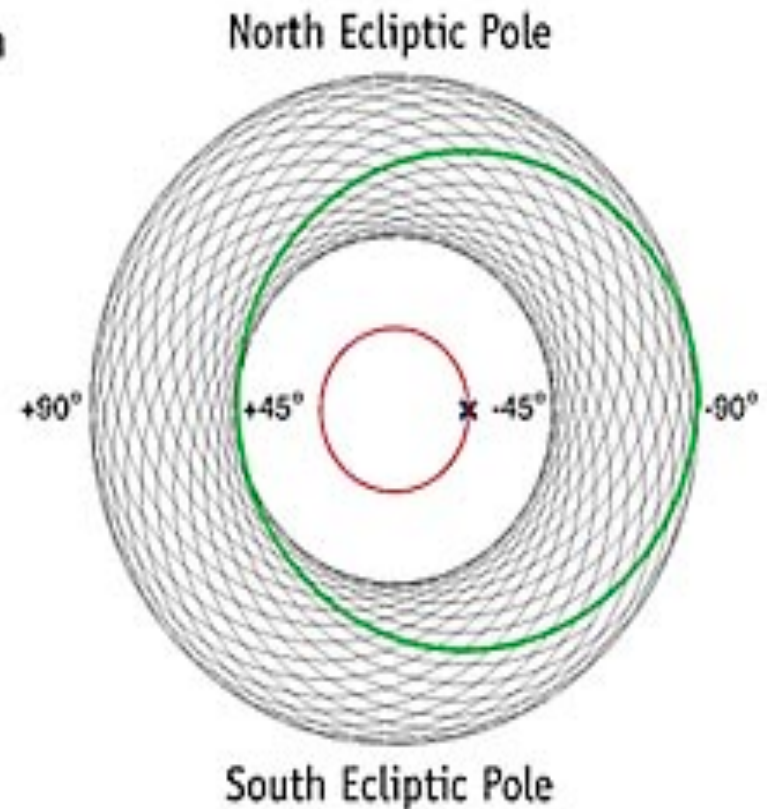
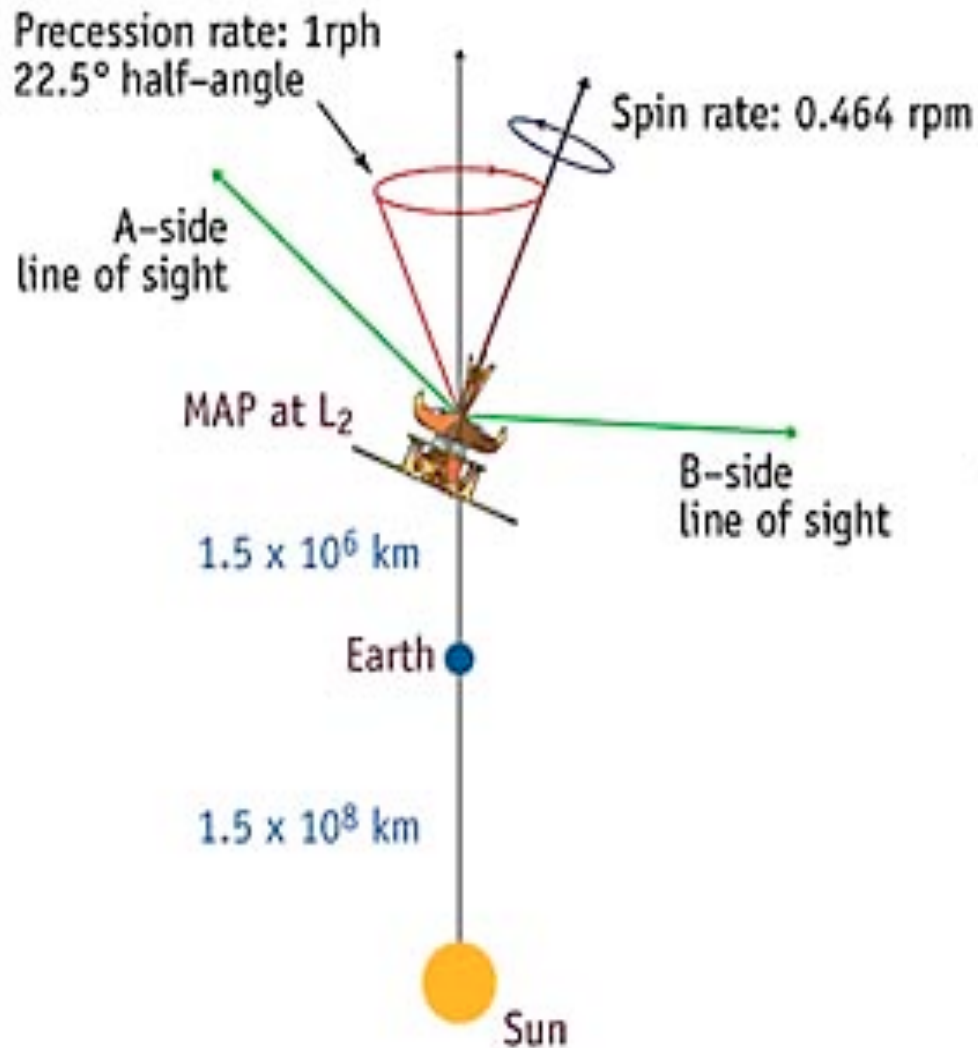


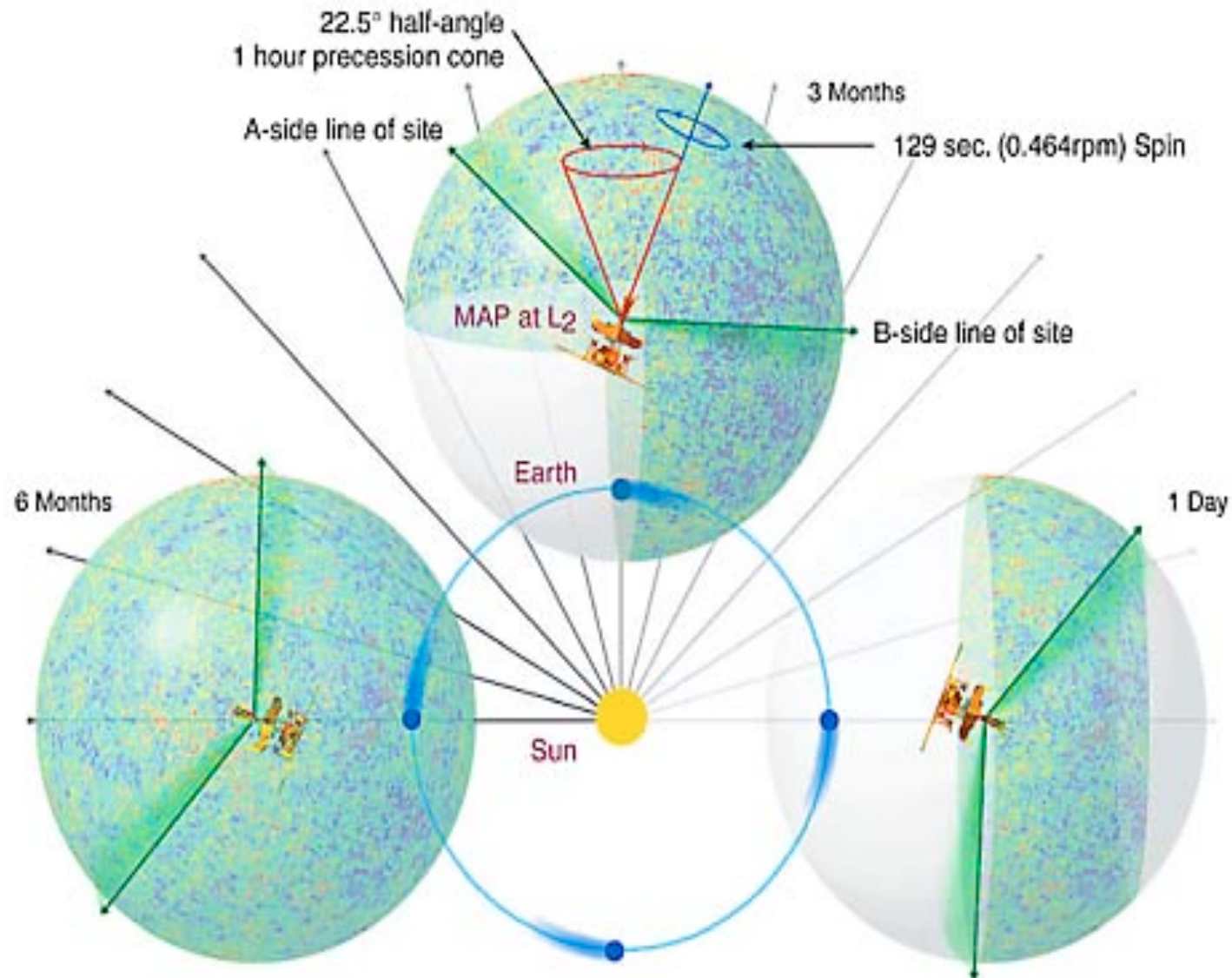
WMAP in orbit at L-2



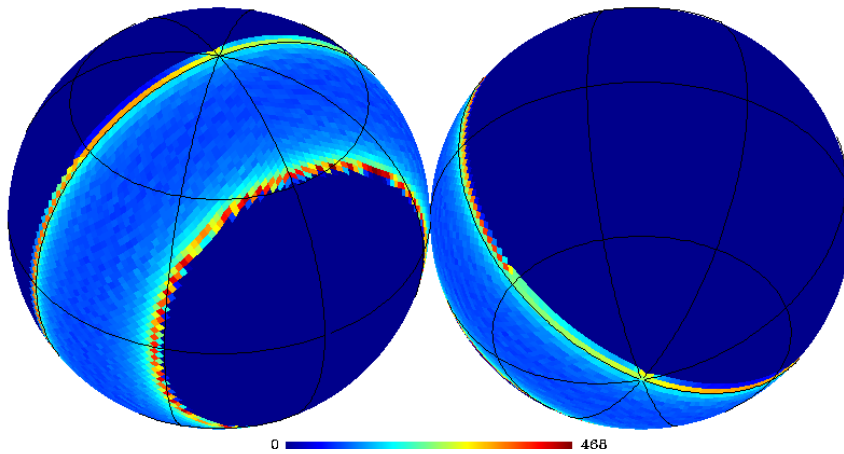


WMAP scanning specifications

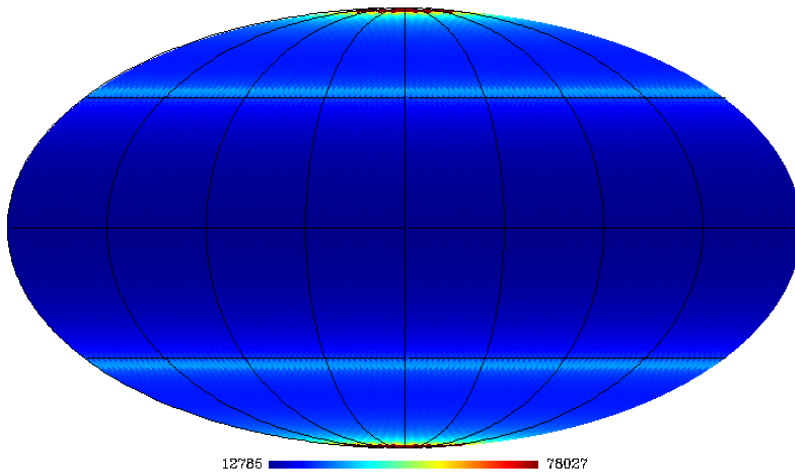




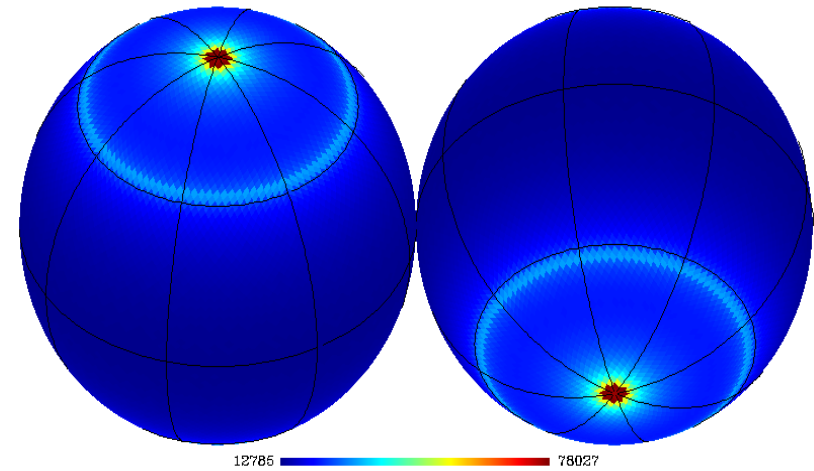
WMAP 1day



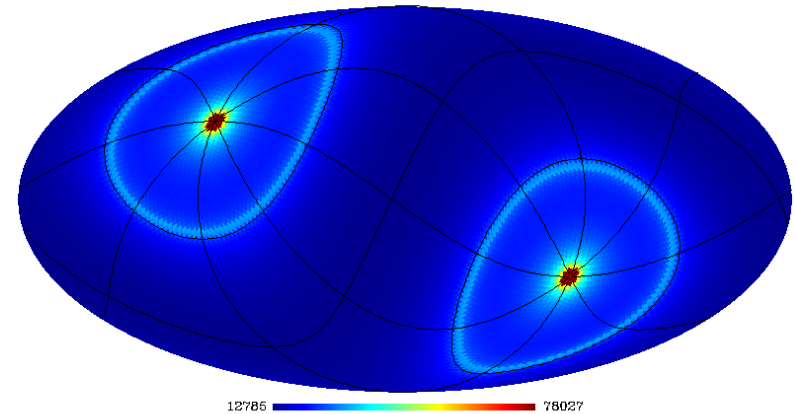
WMAP 1yr



WMAP 1yr

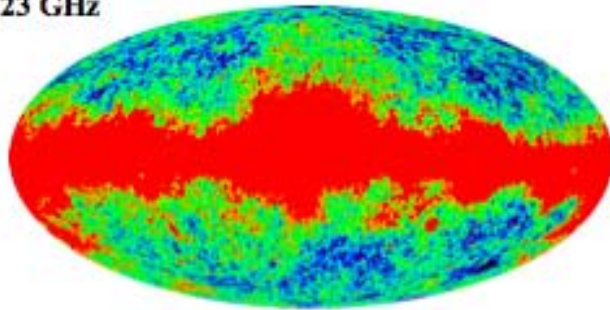


WMAP 1yr

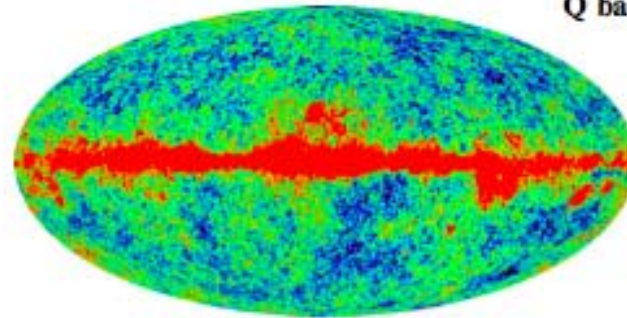


Courtesy of the WMAP Science Team

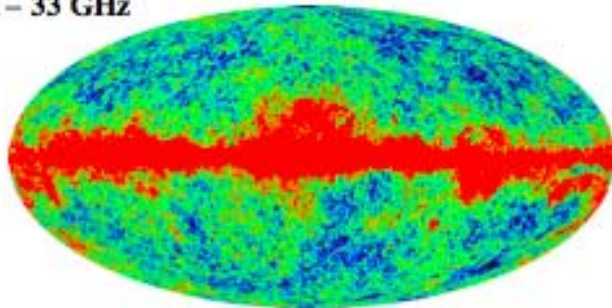
K band – 23 GHz



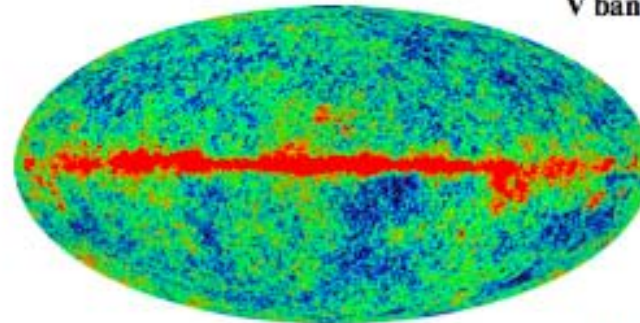
Q band – 41 GHz



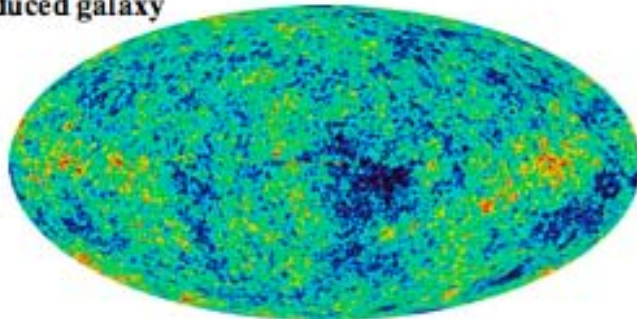
Ka band – 33 GHz



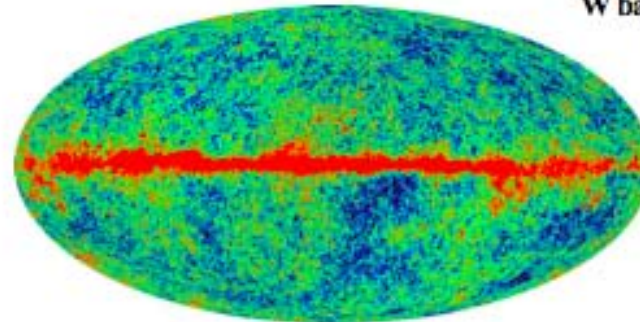
V band – 61 GHz



ILC reduced galaxy

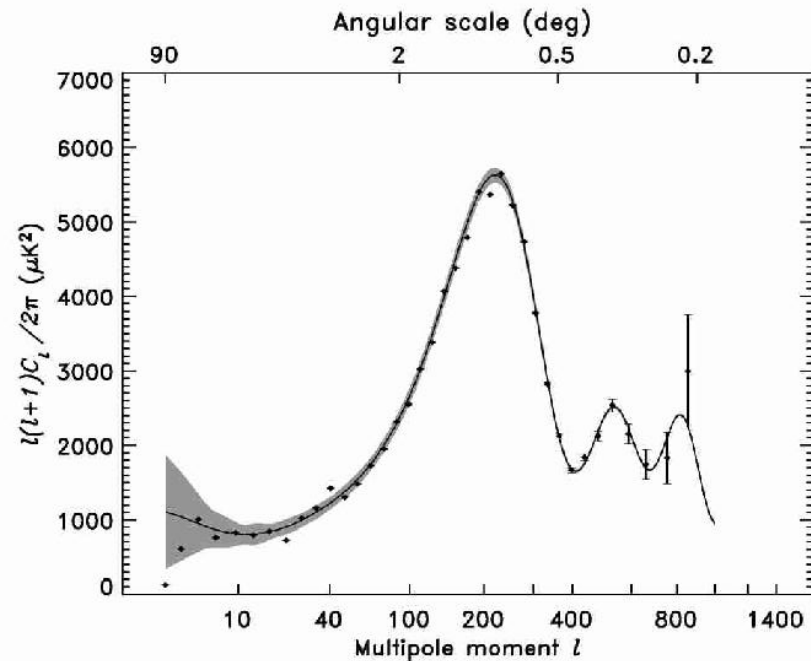
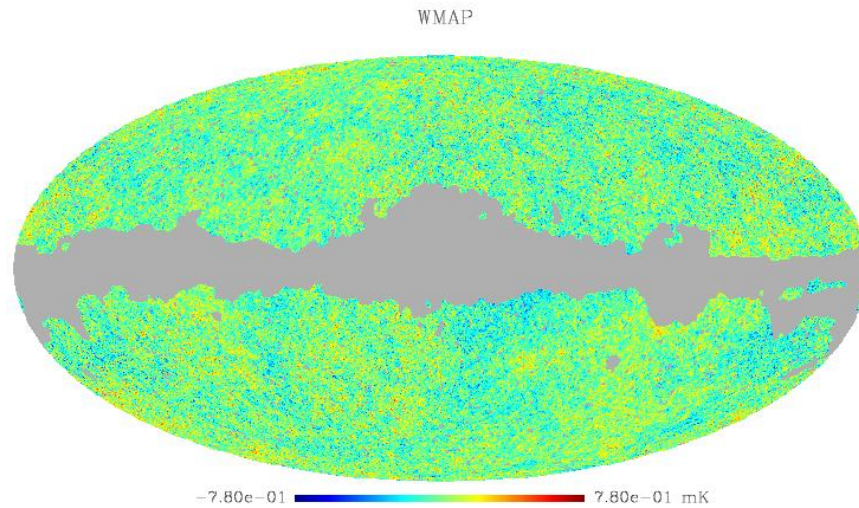


W band – 94 GHz

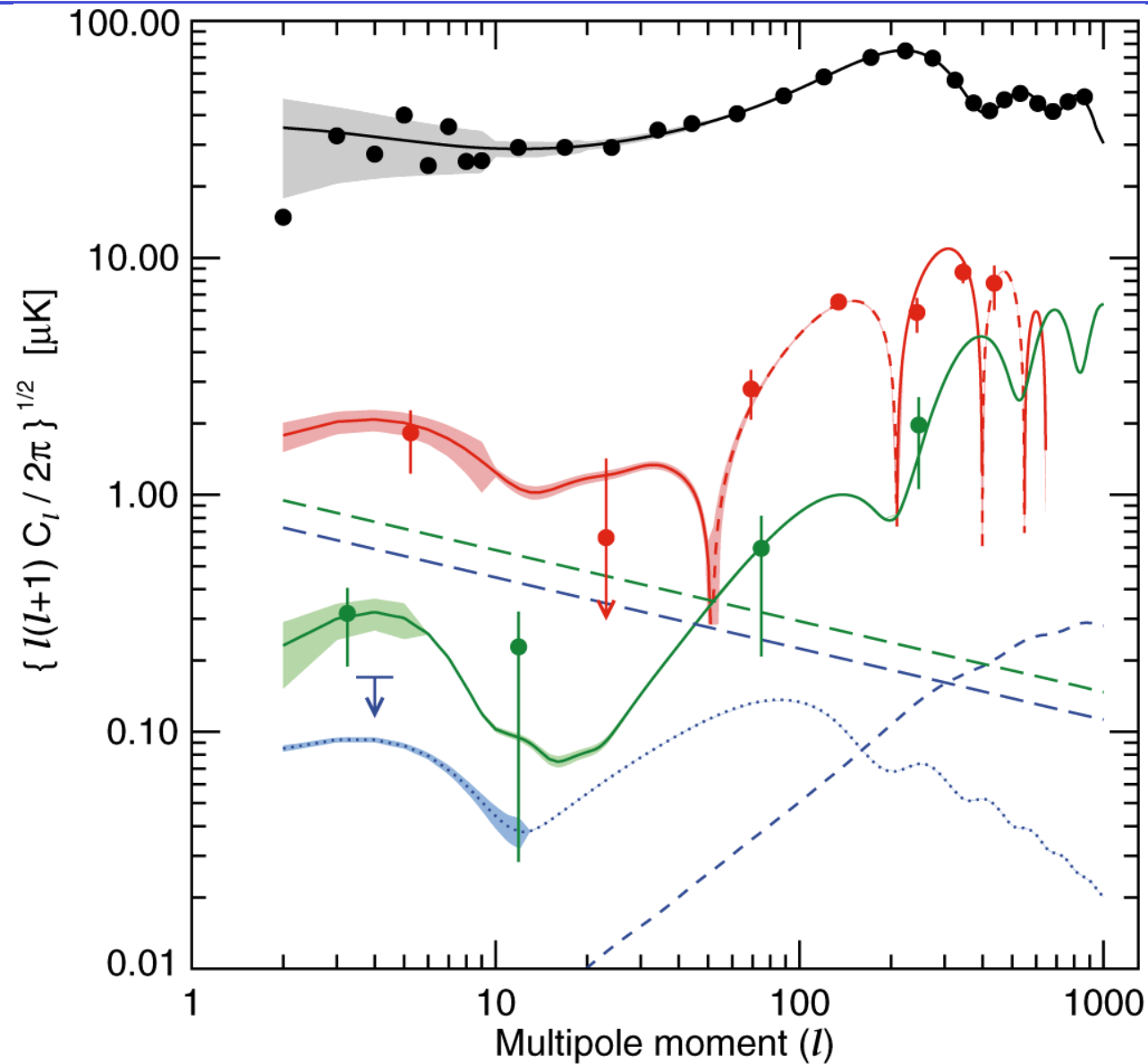




Post-COBE Dream that Came True



- It appears that the cosmological model has already been defined fairly tightly
- Is it, therefore, possible that what is left to be done is “just”
 - Refinement, refinement, refinement ???
 - For example, with Planck, and with polarization measurements, etc.



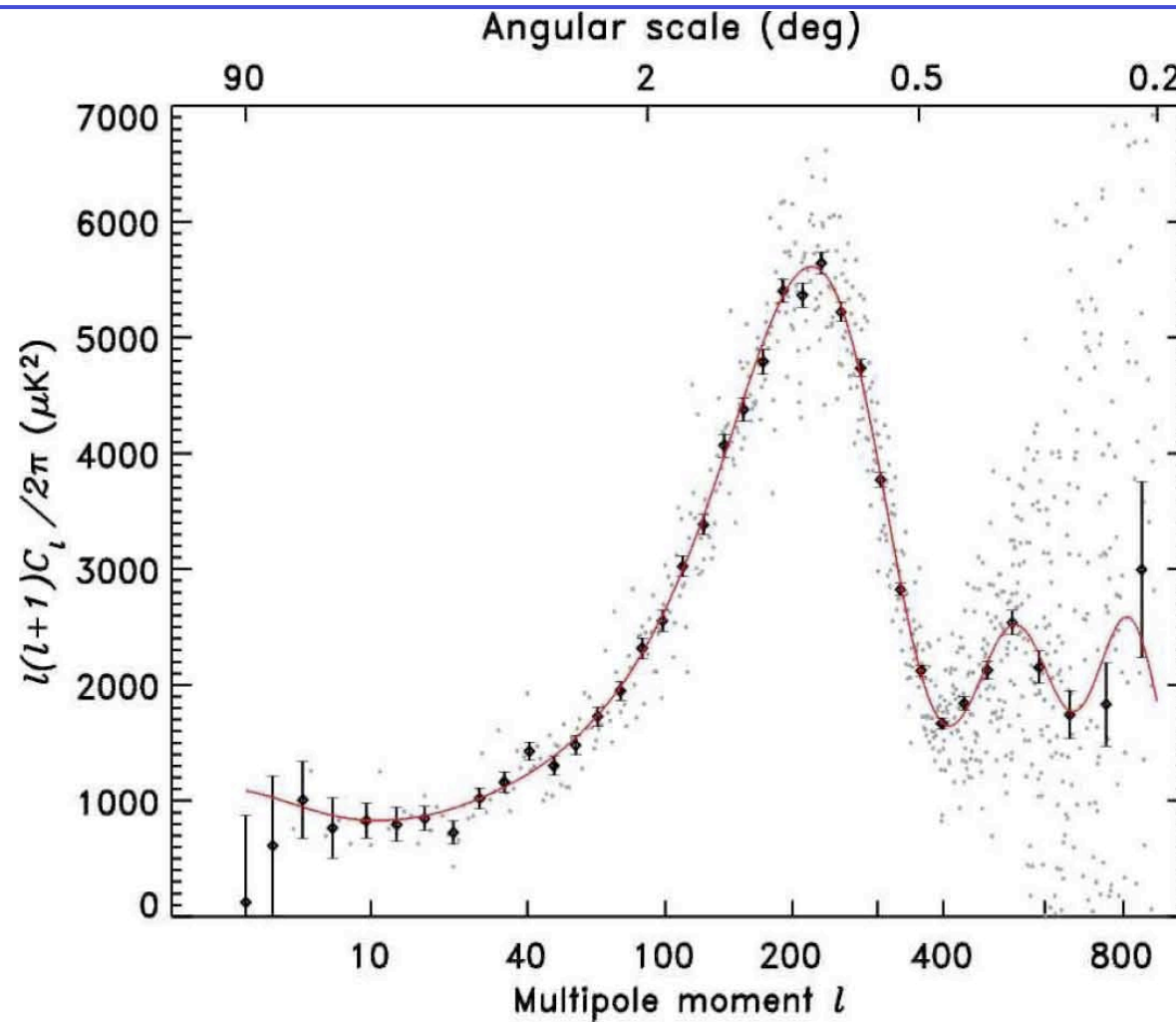


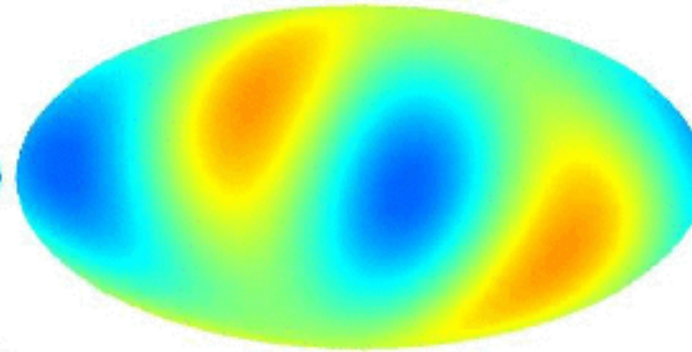
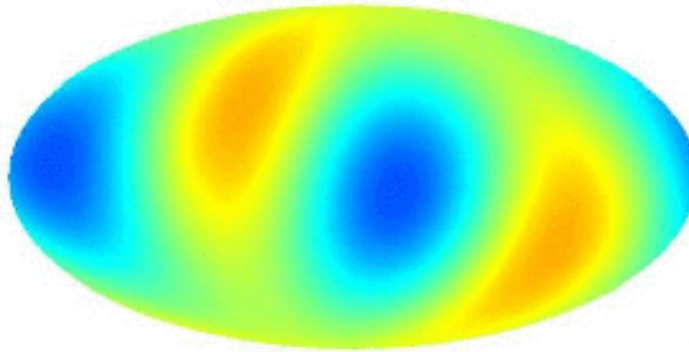
Fig. 1.— This figure compares the best fit power law Λ CDM model to the *WMAP* angular power spectrum. The gray dots are the unbinned data.



WMAP Anomalies - Mode alignment

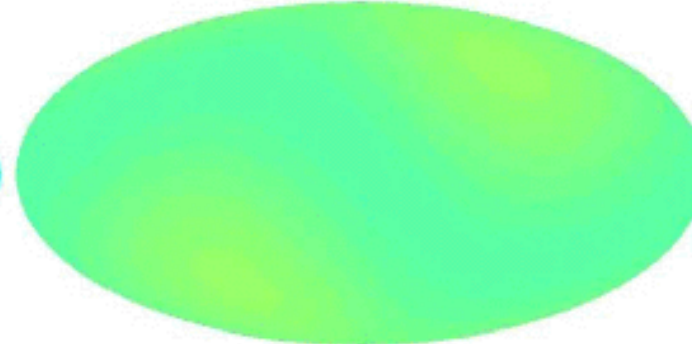
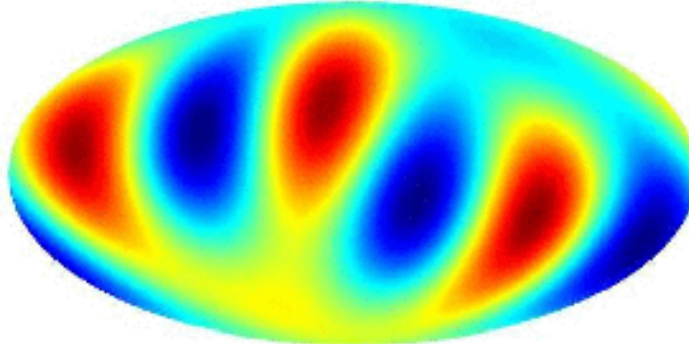


$l = 2$



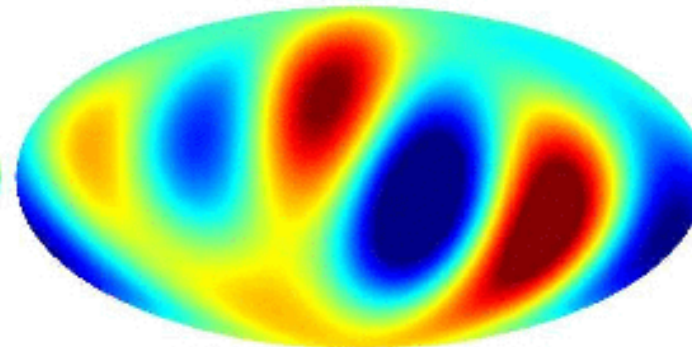
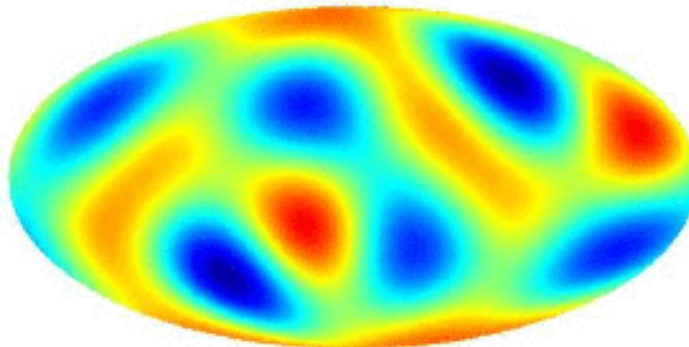
corrected

$l = 3$



kinematic

$l = 4$



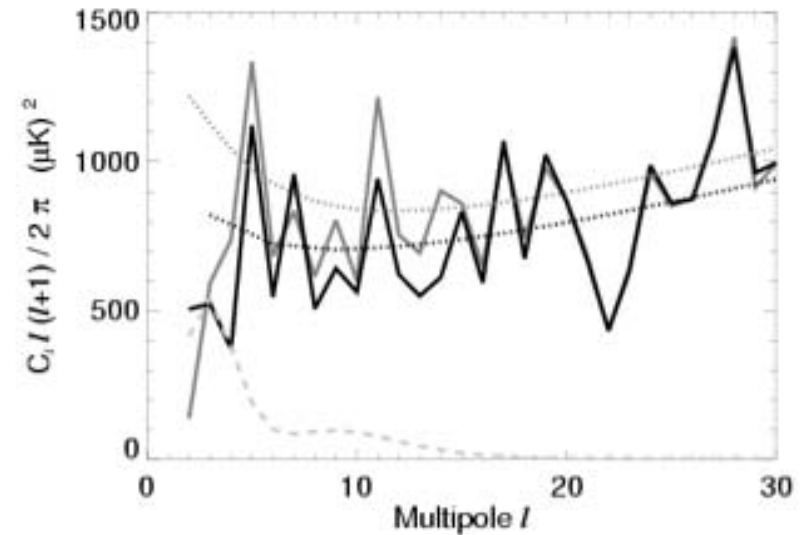
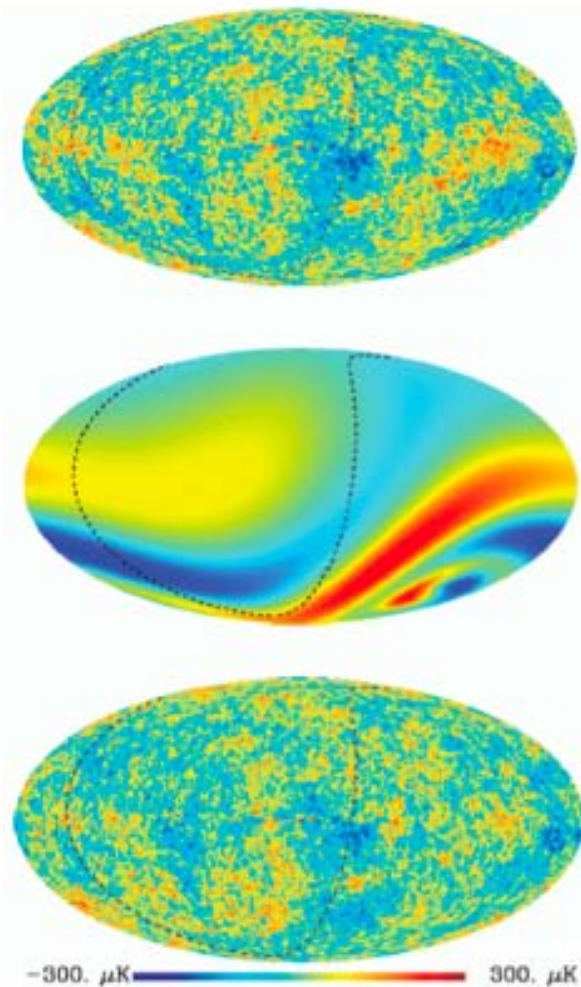
$l = 2+3+4$

$-34\mu\text{K}$  $34\mu\text{K}$

Tegmark et al. *PRD*, 68, 123523 (2003)



Violation of Global Isotropy?



Shear $(\sigma/H)_0 = 4.3 \times 10^{-10}$

Vorticity $(\omega/H)_0 = 9.5 \times 10^{-10}$

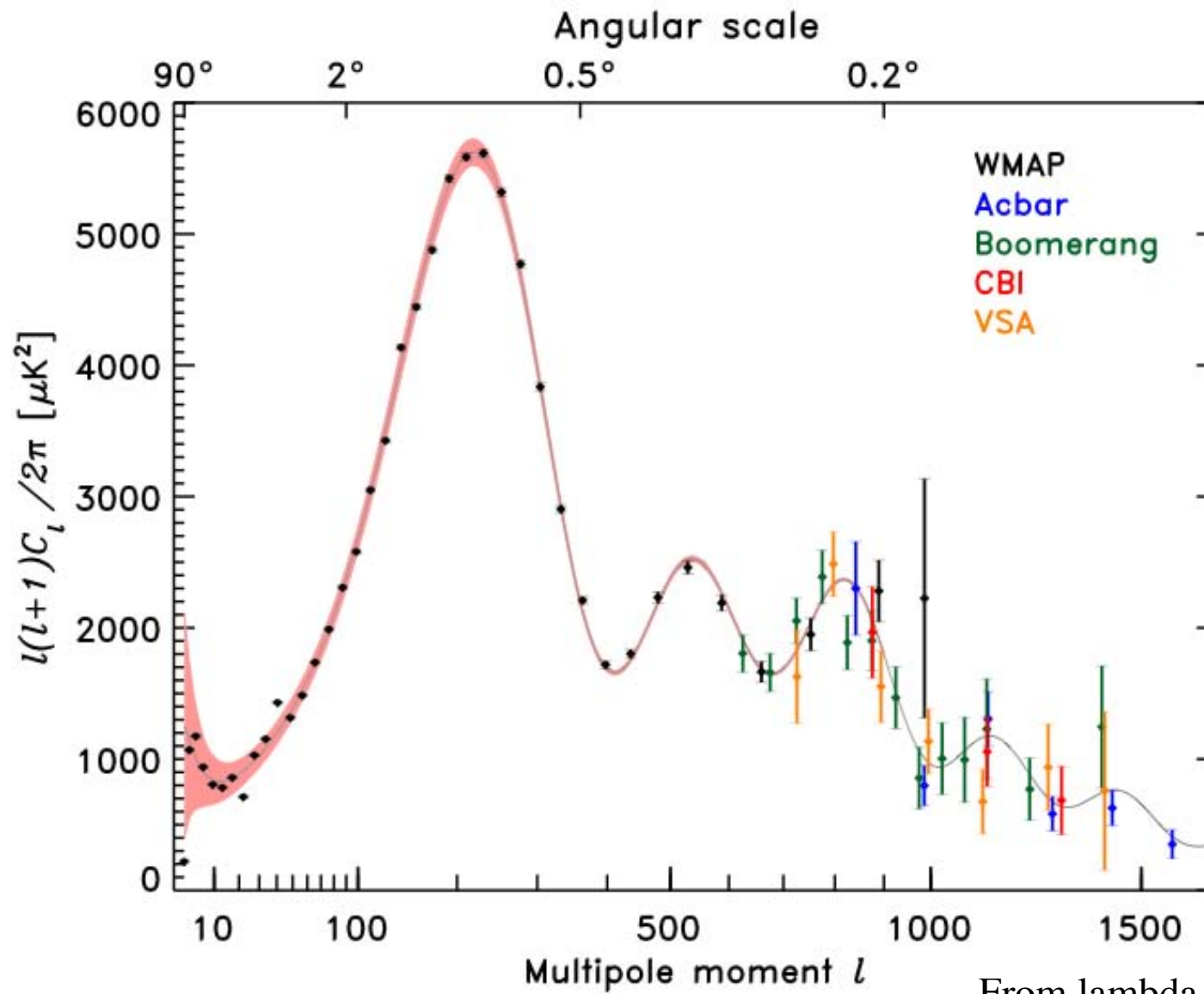
Spiral axis $\{l, b\} = \{222, -62\}$

BUT $\Omega_0 = 0.5$!

Jaffe, Banday, Eriksen, Gorski, Hansen, 2005. ApJL, 629, 1



Current state-of-the-art



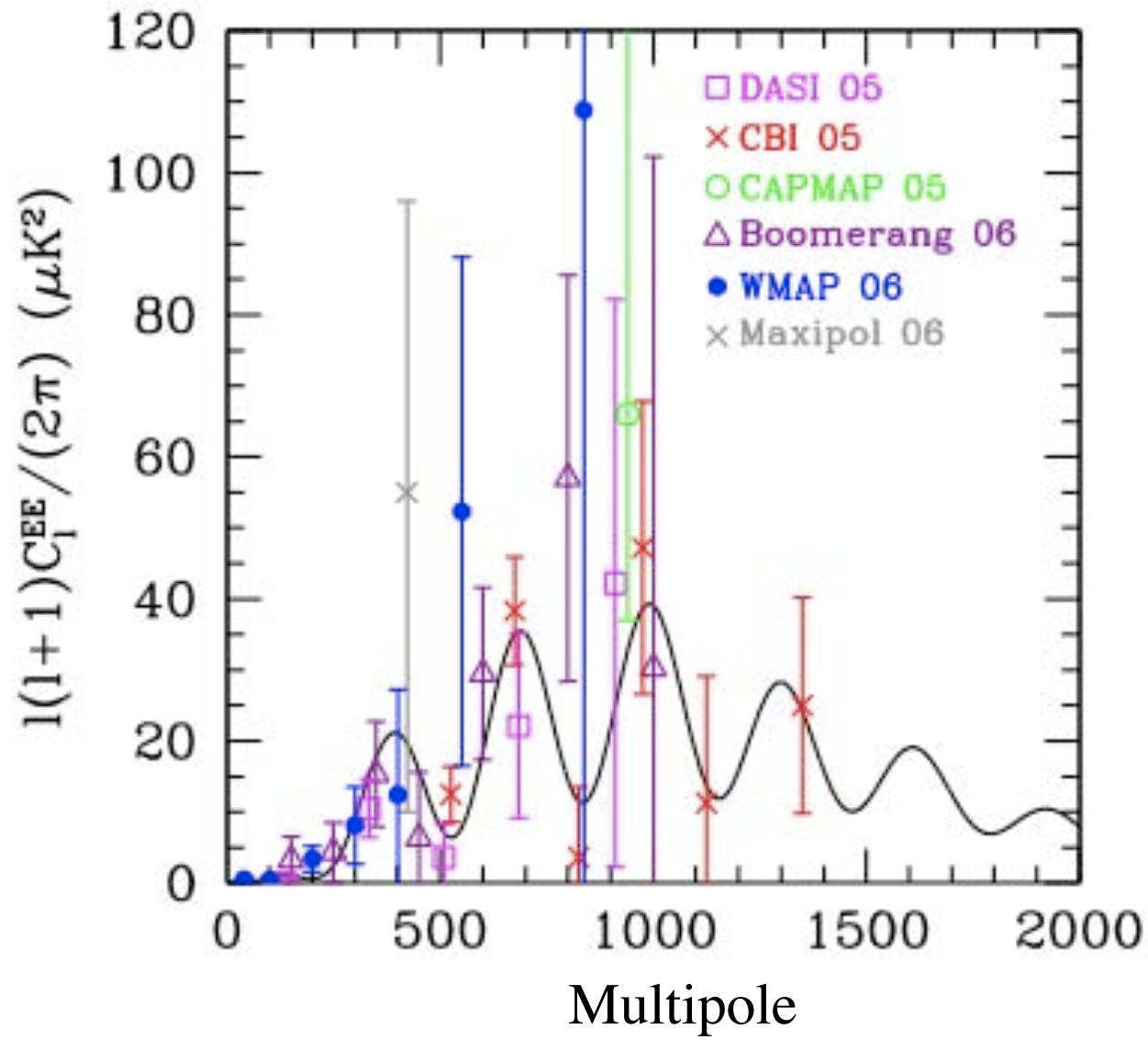
From lambda.gsfc.nasa.gov



The world compilation of CMB polarization measurements



Courtesy Lewis Hyatt





Intermission

HEALPix

5 Platonic Solids

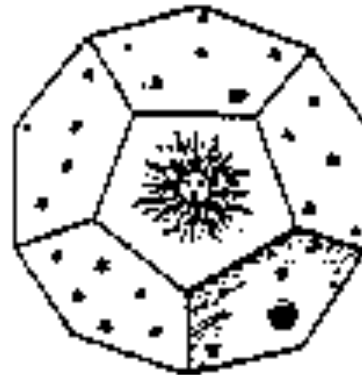
- Drawing from Kepler's *Mysterium Cosmographicum*



Cube
Earth



Tetrahedron
Fire



Dodecahedron
the Universe



Icosahedron
Water



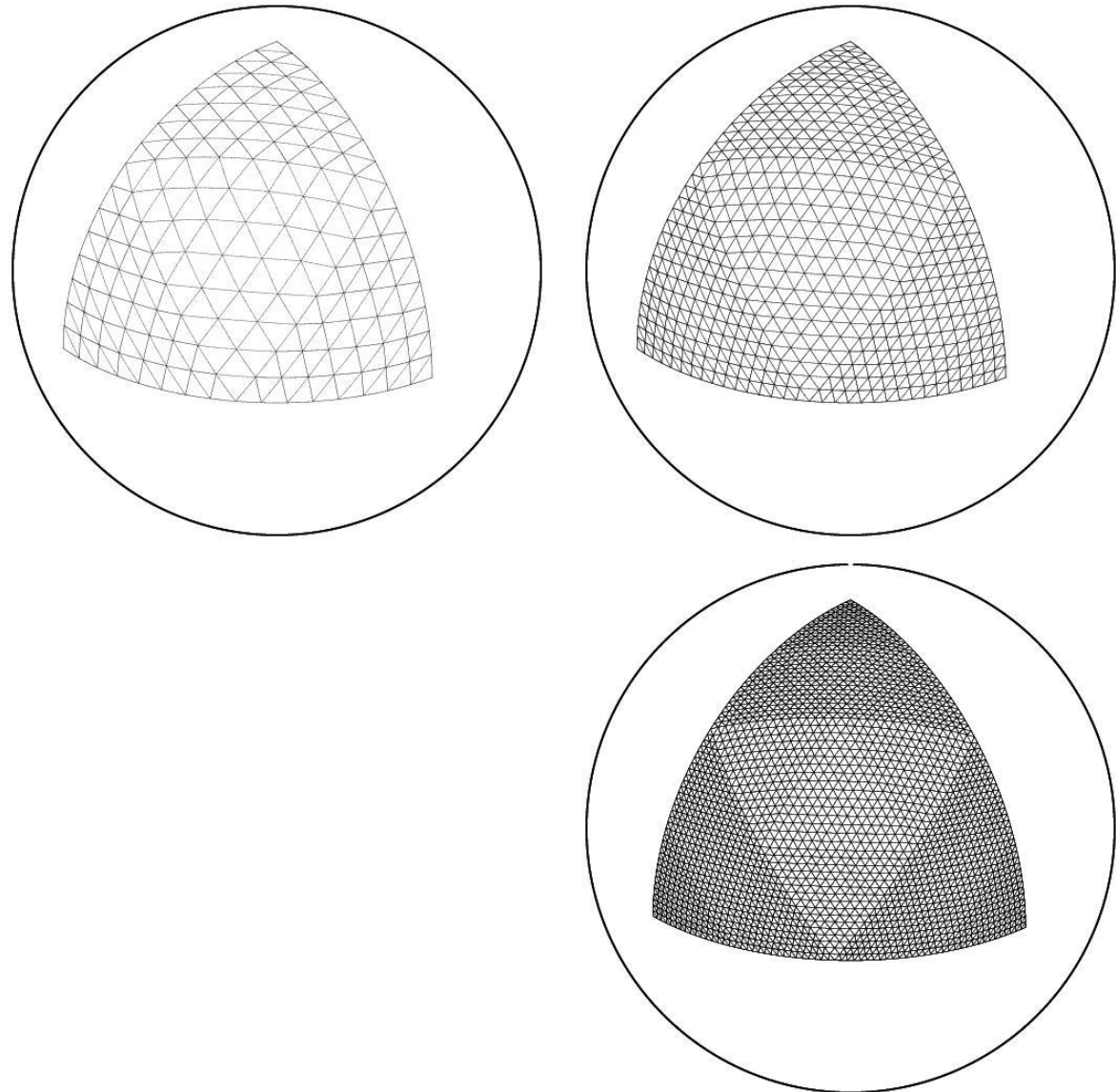
Octahedron
Air

Icosahedral Dome, Epcot Center, Disneyworld, Florida



HTM Hierarchical Triangular Mesh

Used
extensively
in
SDSS



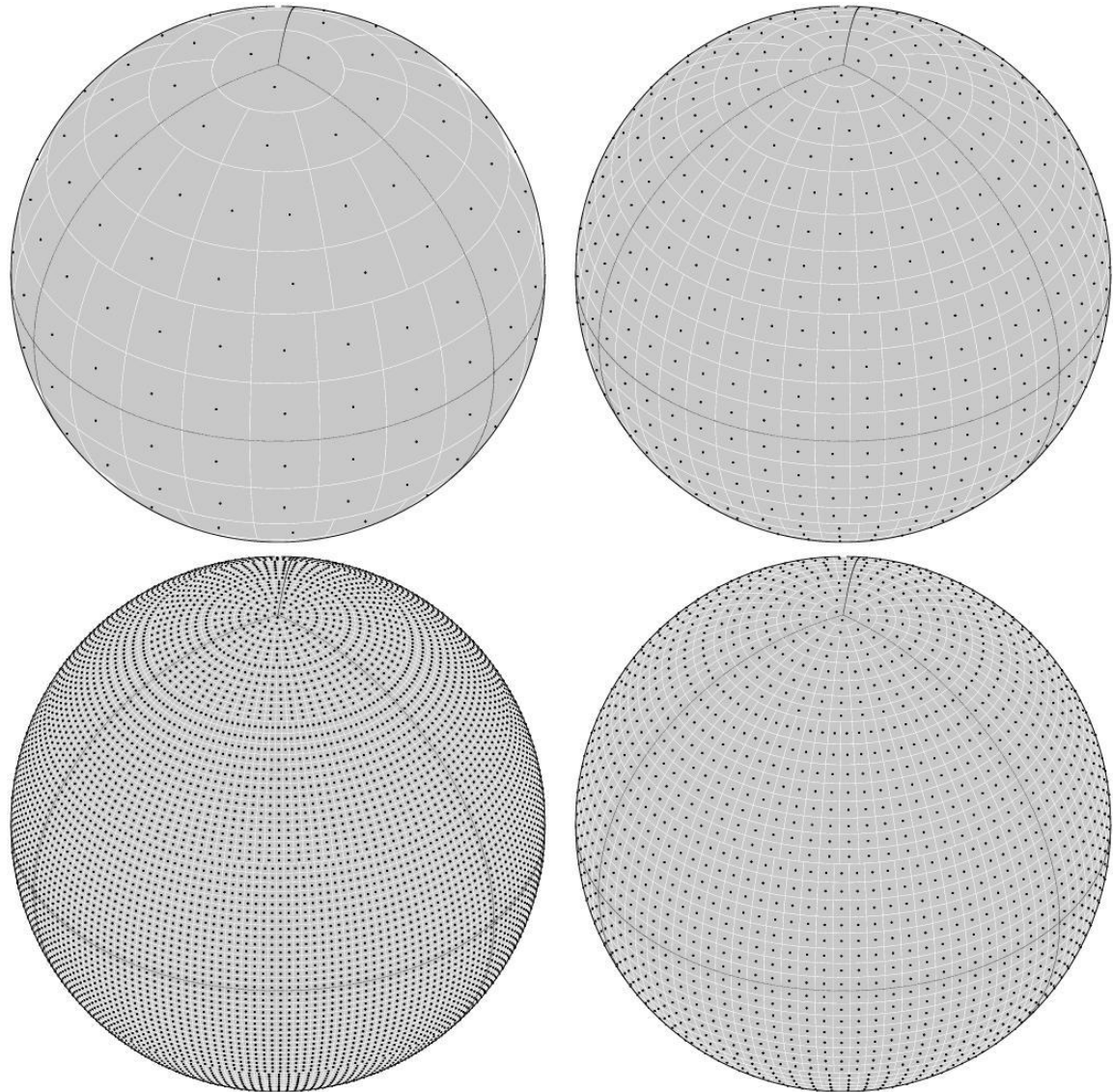
Discoball

- Used extensively in discos



IGLOO

**Crittenden
and
Turok**



Panteon, Rome

- Built in 124 AD!
- 43m dome
- The largest in the world until the XXth century!!!



The Next Four ...

**San Pietro
Rome
42m
1593 AD**



**Santa Maria
del Fiore
Florence
42m
1420 AD**

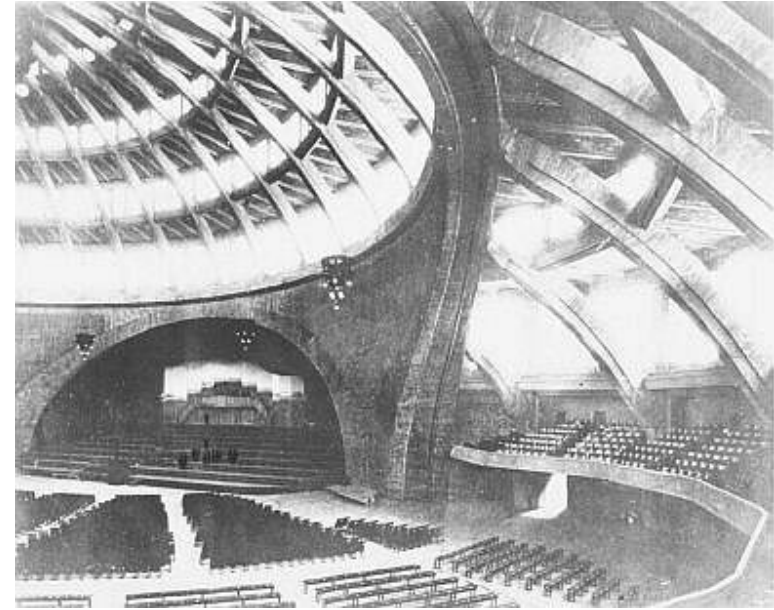
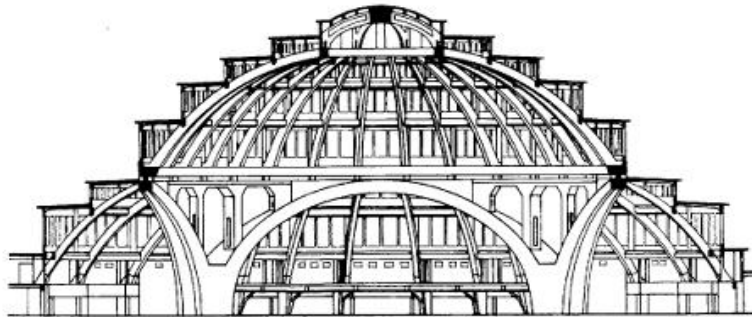
**Hagia Sophia
Istanbul
32m
537 AD**



**St. Paul's
London
33m
1710 AD**



Jahrhunderthalle by Max Weber, 1913, Breslau



Krzysztof M. Górski

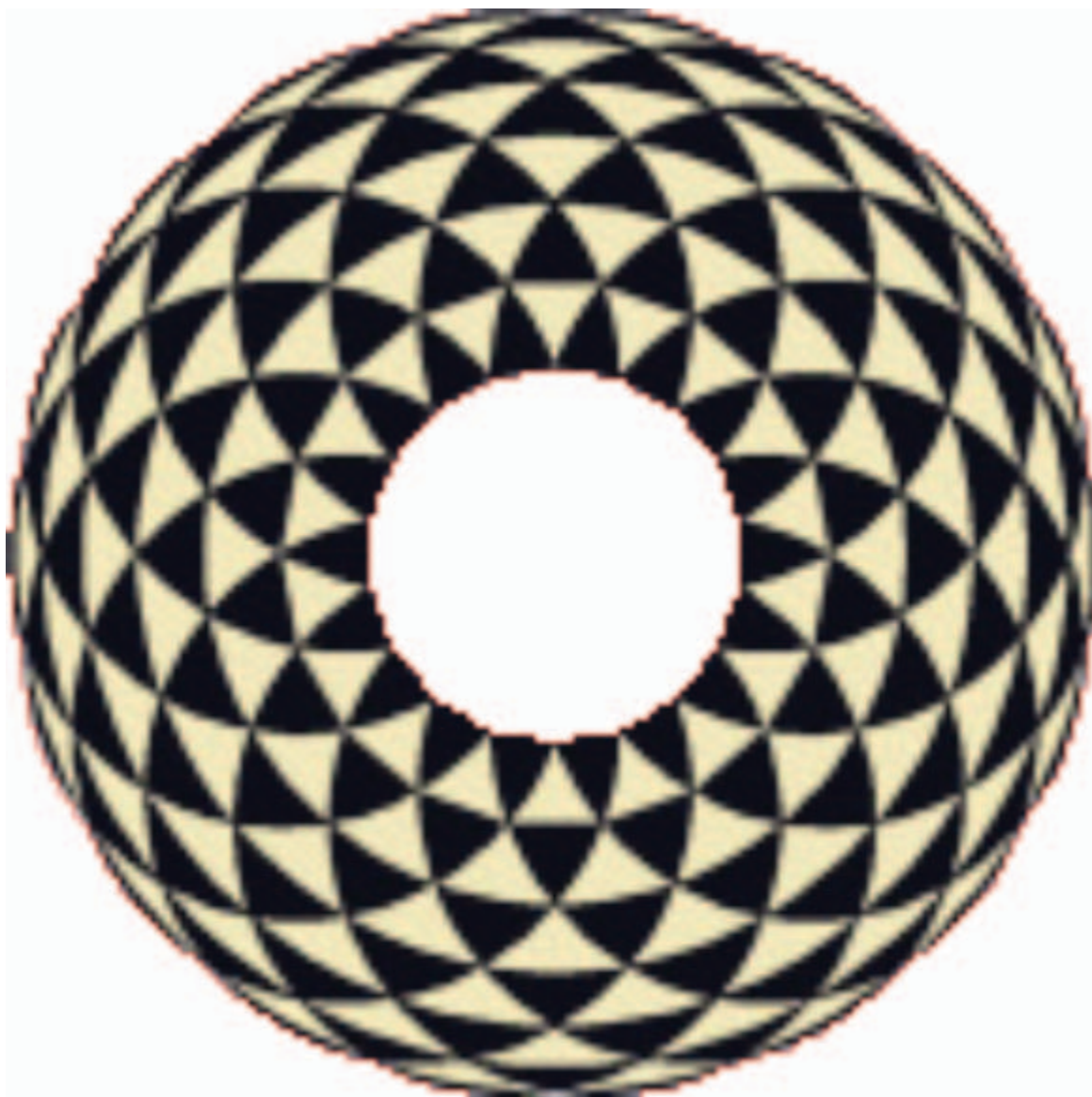
Azores School on Observational Cosmology, Angra do Heroismo,
Sept. 2011

Temple of Venus and Roma

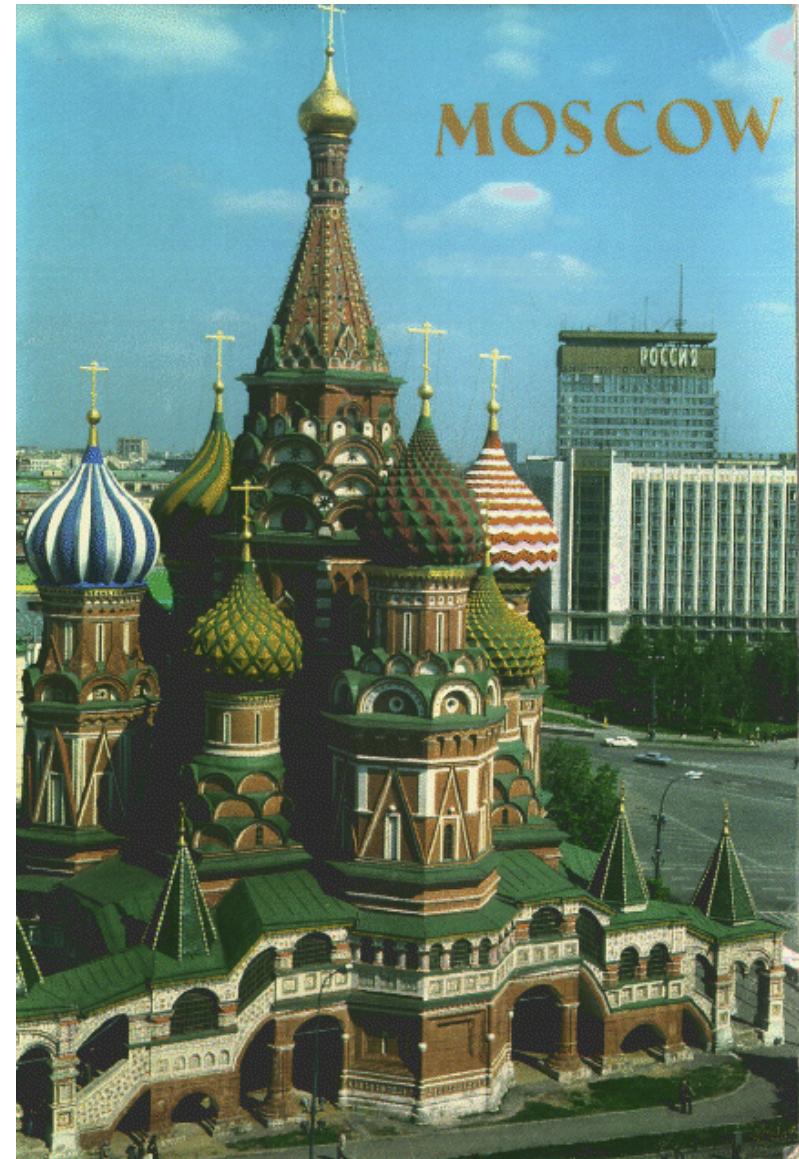
- On Forum Romanum, across the road from Colosseum



Roman Floor Mosaic



St. Basil, Moscow



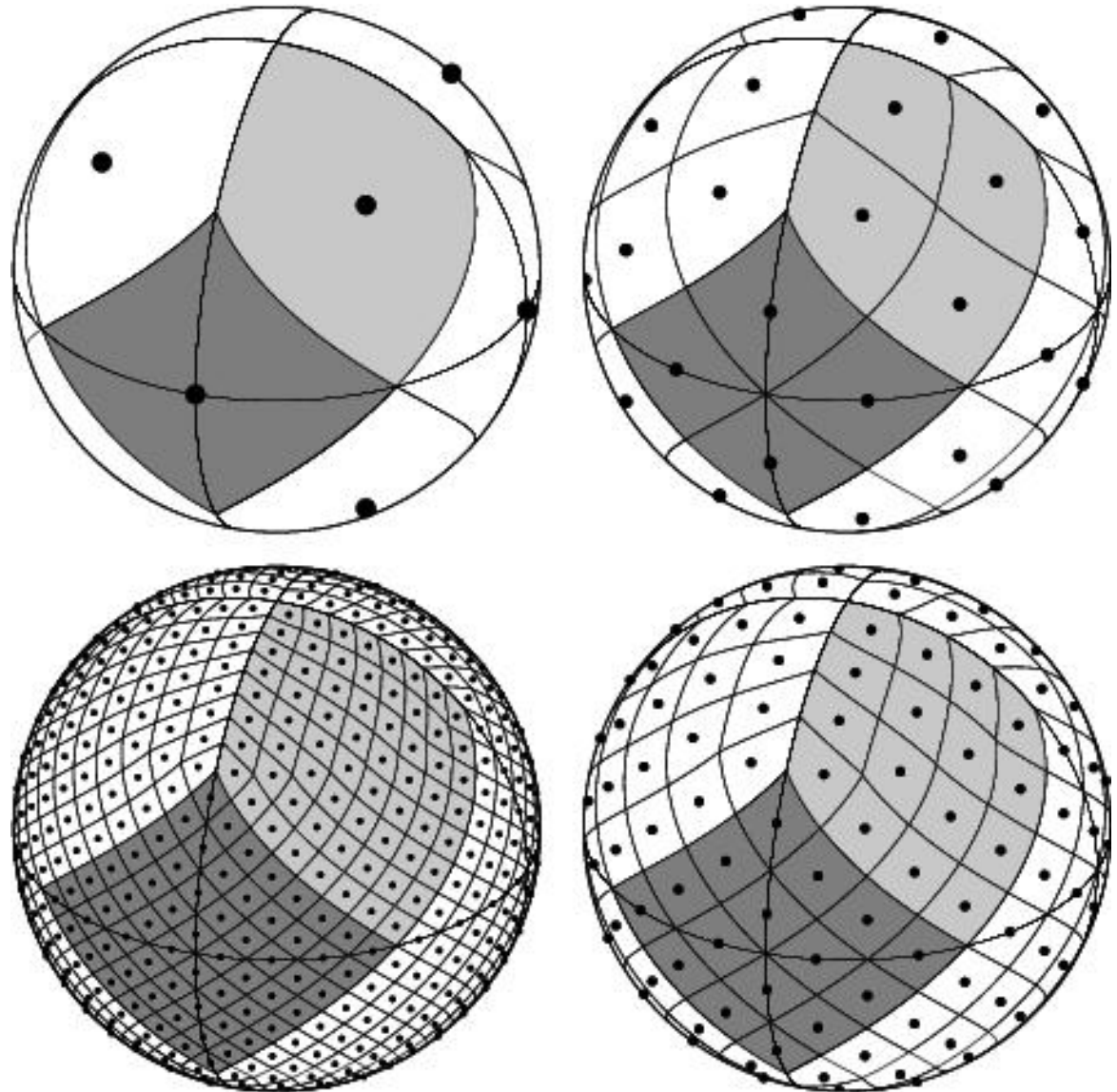
- Hierarchical
- Equal Area
- Iso-Latitude
- Pixelization

<http://healpix.jpl.nasa.gov>

Freely available, GNU-licensed software library (F90, C++, C, IDL) for discretization, synthesis, analysis, etc. of functions on the sphere;

Developed and supported since 1997; Used by WMAP and Planck; also Boomerang, Archeops, and other suborbital experiments;

Gorski, Hivon, Banday, Reinecke, Wandelt, Hansen, ...

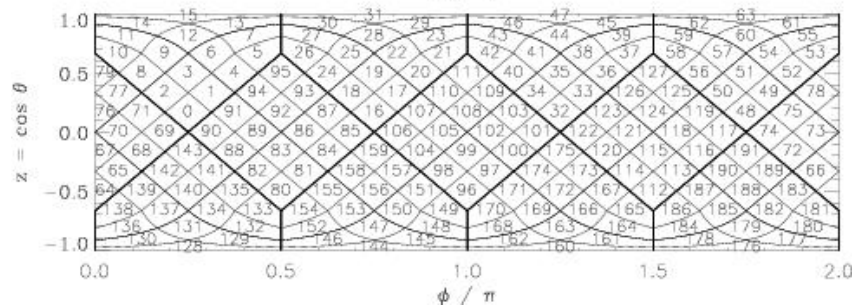
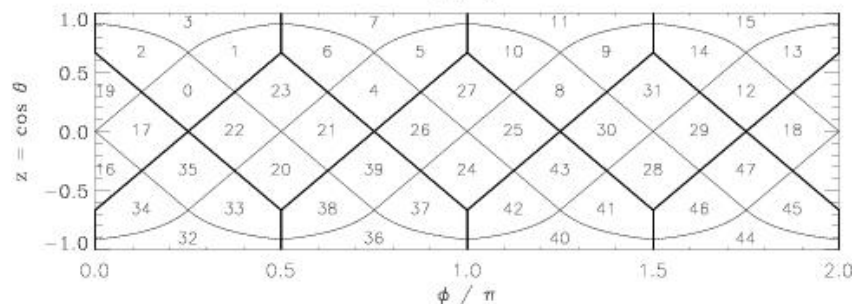
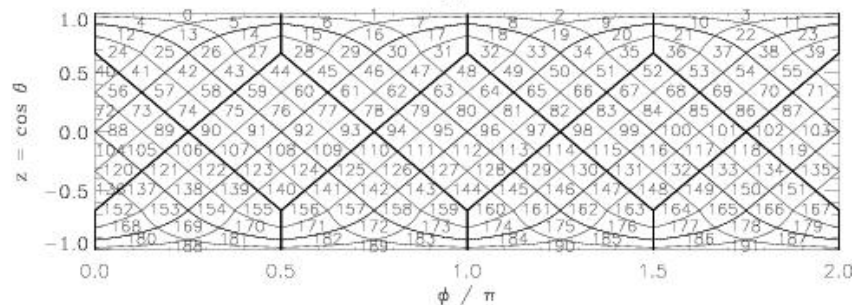
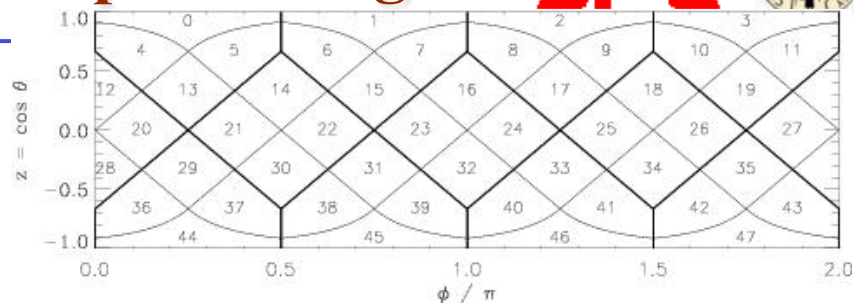




HEALPix - the Sky Map Indexing



Ring Scheme



Nested Scheme

3 11_2	1 01_2
2 10_2	0 00_2

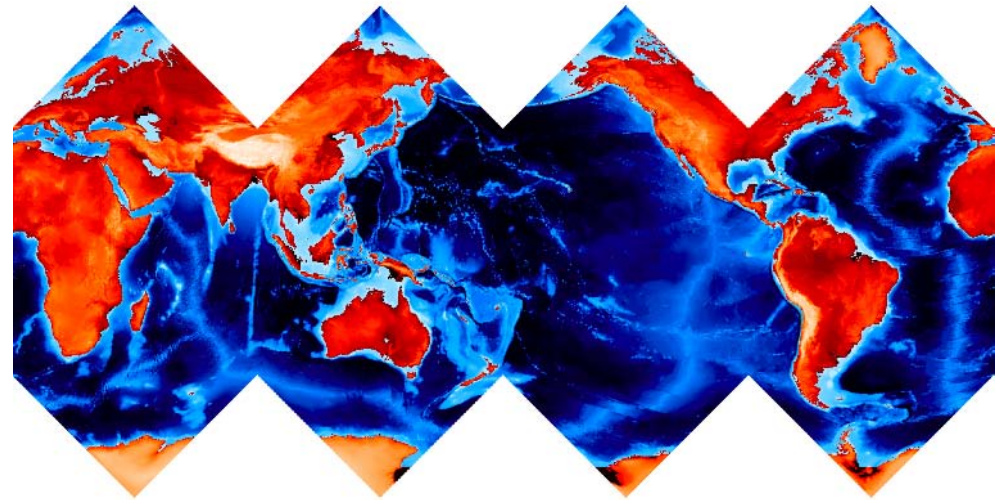
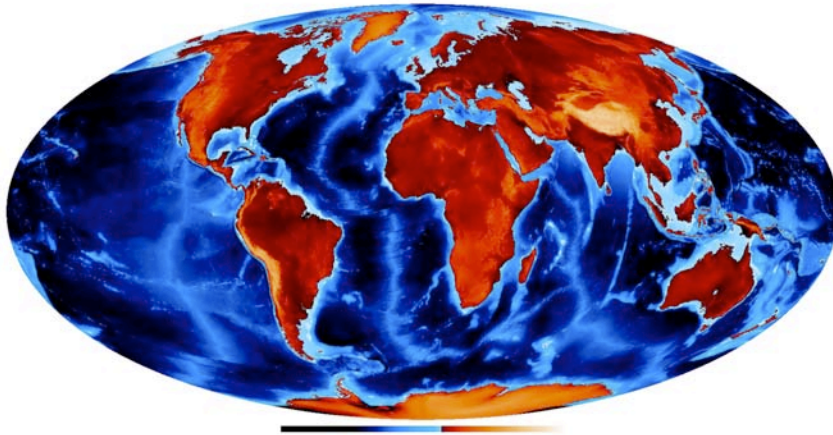
Prograde

Degrade

15 $11_1 11_2$	13 $11_1 01_2$	7 $01_1 11_2$	5 $01_1 01_2$
14 $11_1 10_2$	12 $11_1 00_2$	6 $01_1 10_2$	4 $01_1 00_2$
11 $10_1 11_2$	9 $10_1 01_2$	3 $00_1 11_2$	1 $00_1 01_2$
10 $10_1 10_2$	8 $10_1 00_2$	2 $00_1 10_2$	0 $00_1 00_2$



HEALPix Cartography

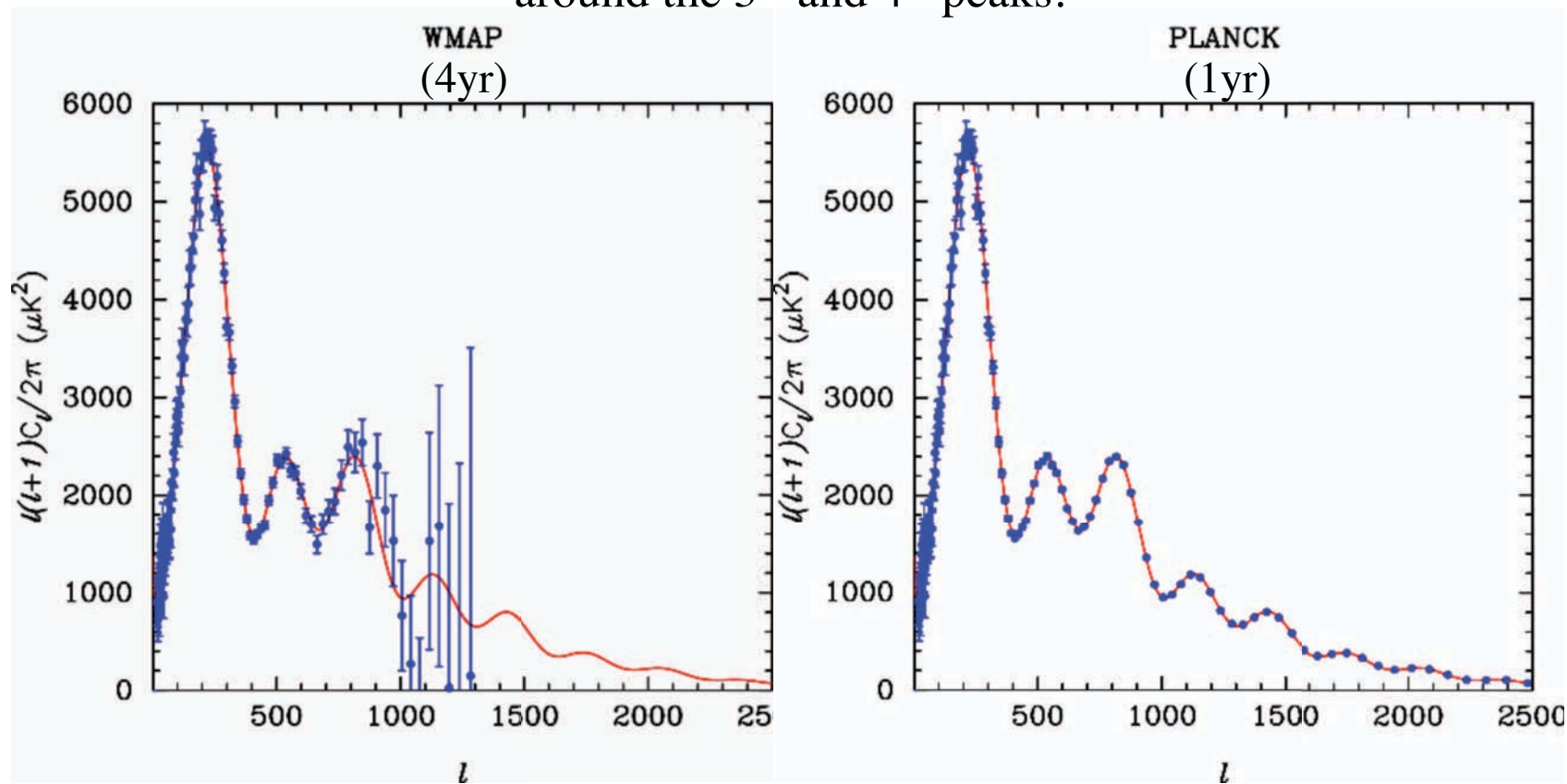


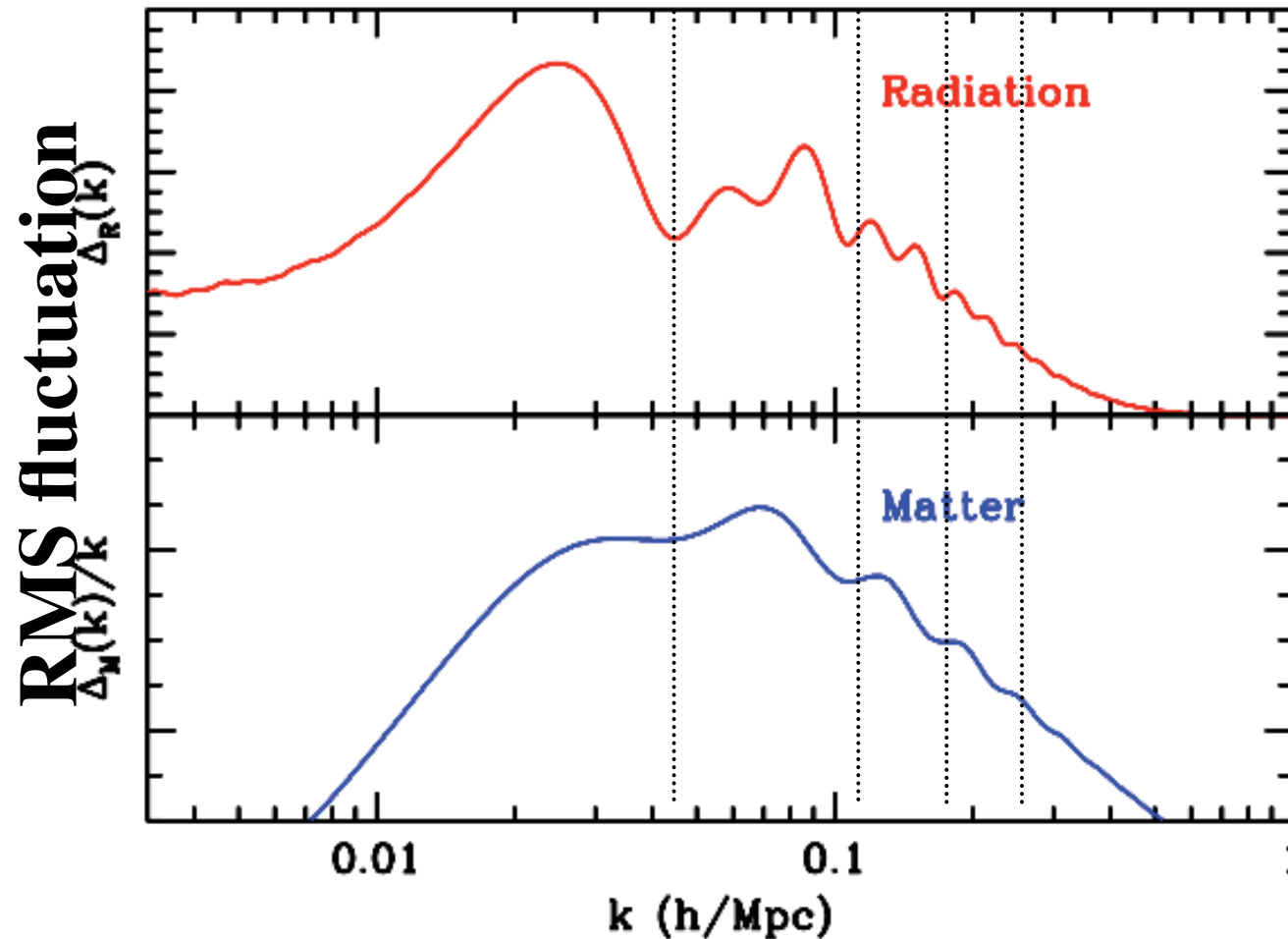
- Old subject in cartography - Flattening the Earth
- Górski, K.M., Hivon, E., Banday, A.J., Wandelt, B.D., Hansen, F.K., Reinecke, M., Bartelmann, M., 2005, Ap.J., 622, pp. 759-771, “HEALPix: A Framework for High-Resolution Discretization and Fast Analysis of Data Distributed on the Sphere”
 - Description of “HEALPix projection” from the sphere to the plane
- Calabretta, M.R., and Roukema, B.F., 2007, MNRAS, 381, pp. 865-872, “Mapping on the HEALPix grid”
 - HEALPix - a hybrid of the cylindrical equal area (equatorial region), and interrupted Collignon (polar regions) cartographic projections



Planck

In addition to wider frequency coverage and better sensitivity than WMAP, Planck has the resolution needed to see into the damping tail. It will be the first experiment to make a cosmic variance limited measurement of the scales around the 3rd and 4th peaks.



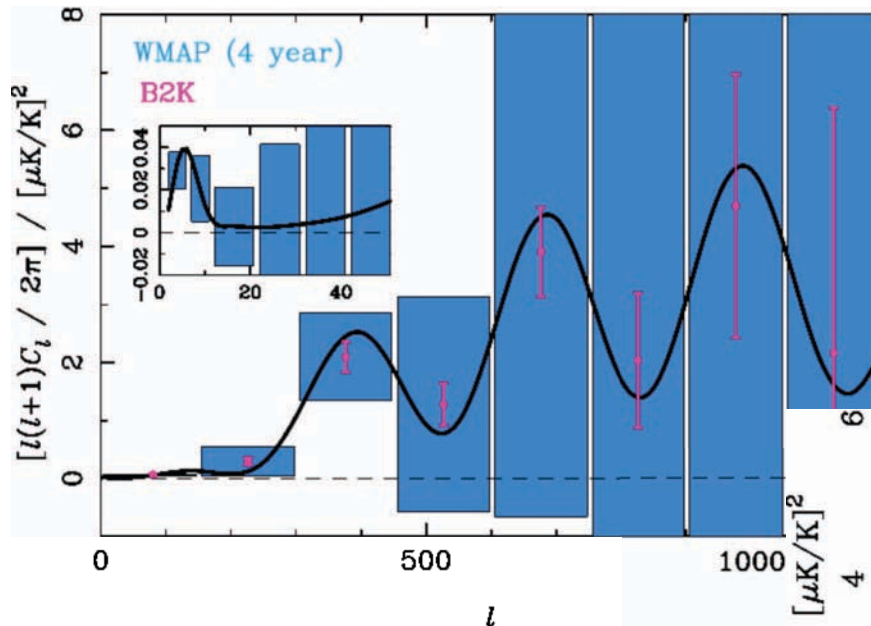


Both the large-scale “peak” in the matter power spectrum and the fine-scale “wiggles” are well calibrated by the CMB.

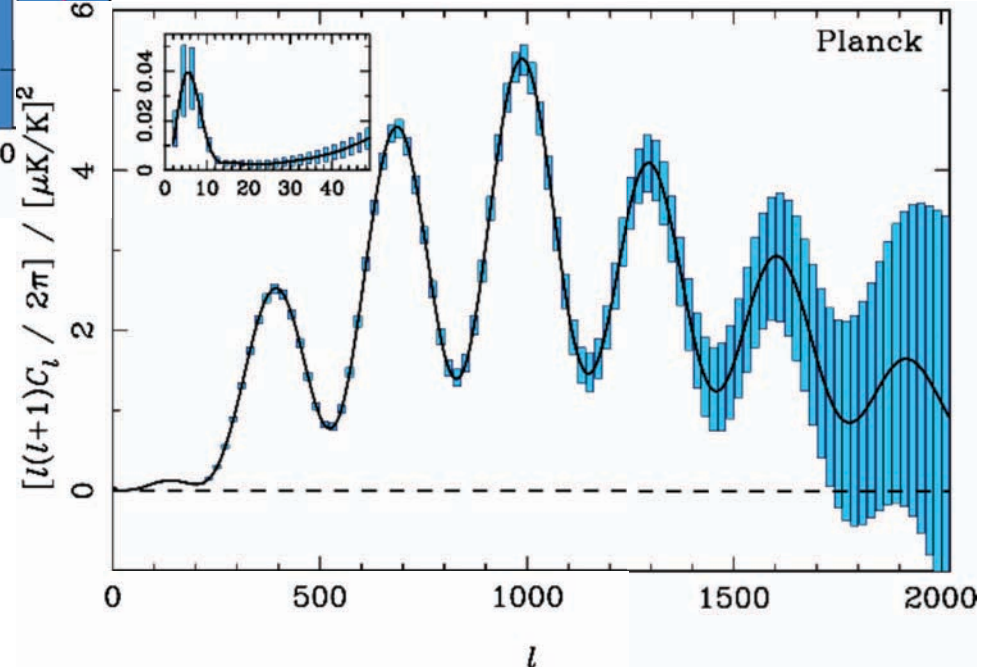
Wavenumber



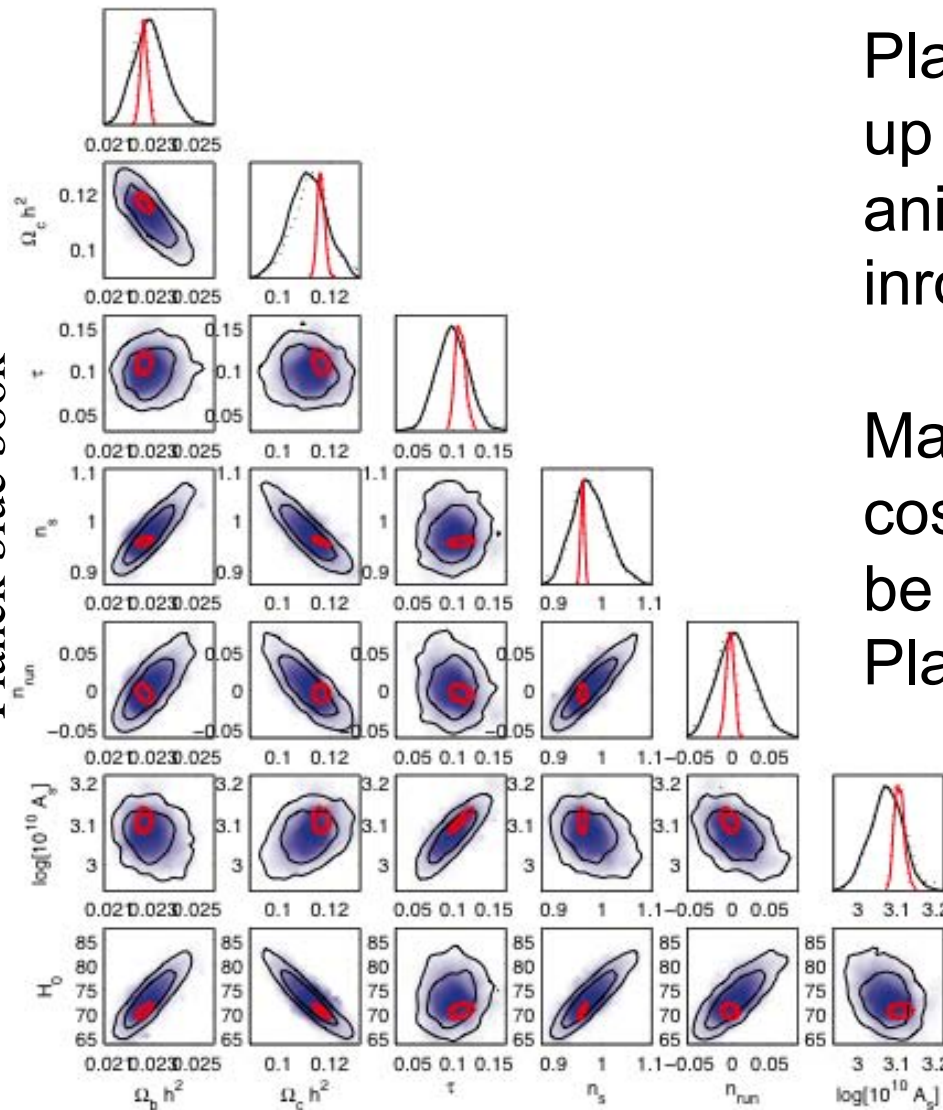
What (we hope) Planck will add



A precise measurement of the E-mode polarization power spectrum and a highly sensitive search for B-modes (from inflation?).



Planck blue book



Planck will essentially clean up the primary temperature anisotropies and make great inroads on polarization.

Many of the most important cosmological parameters will be known *much* better after Planck flies.

Projected WMAP likelihood
Projected Planck likelihood
on Hubble constant



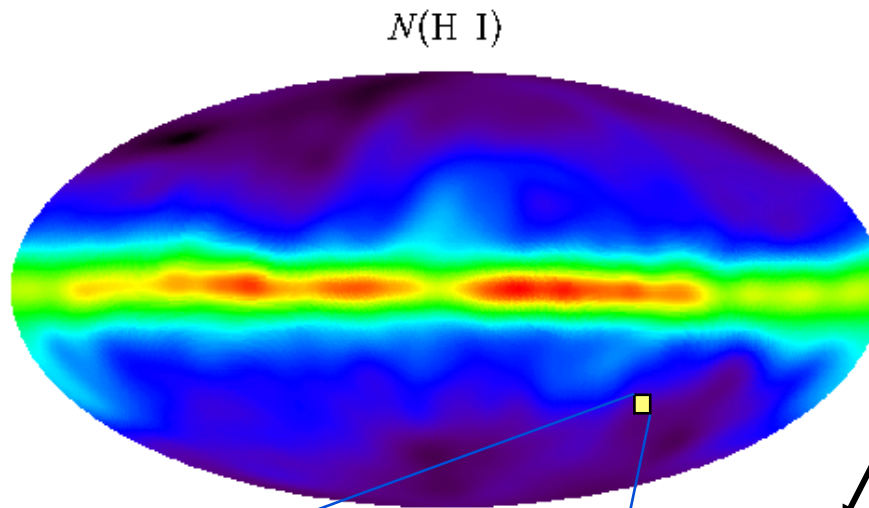
Non-CMB Science



- **Planck will measure the entire sky at 9 frequencies from 30 to 857 GHz**
- **At frequencies above 100 GHz, Planck will be the only all-sky survey since FIRAS**
- **Planck sensitivity to compact sources is $>10^4$ times better than FIRAS!**
- **Planck will see tens of thousands of discrete sources, both extragalactic and in the Milky Way, and provide extensive data for both galactic and extragalactic astrophysics.**

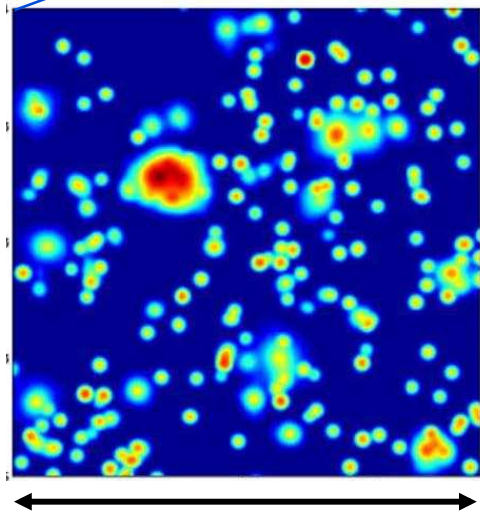


All-sky survey @ 300 μm -> 3mm



COBE FIRAS:
7 degree resolution
No discrete sources

$$[\theta_F / \theta_P]^2 > 7000$$



2 degrees

Planck:
5' @ 350, 550, 850 and 1400 μm
+ 7', 10' @ 2 and 3 mm.

~ 100,000 sources

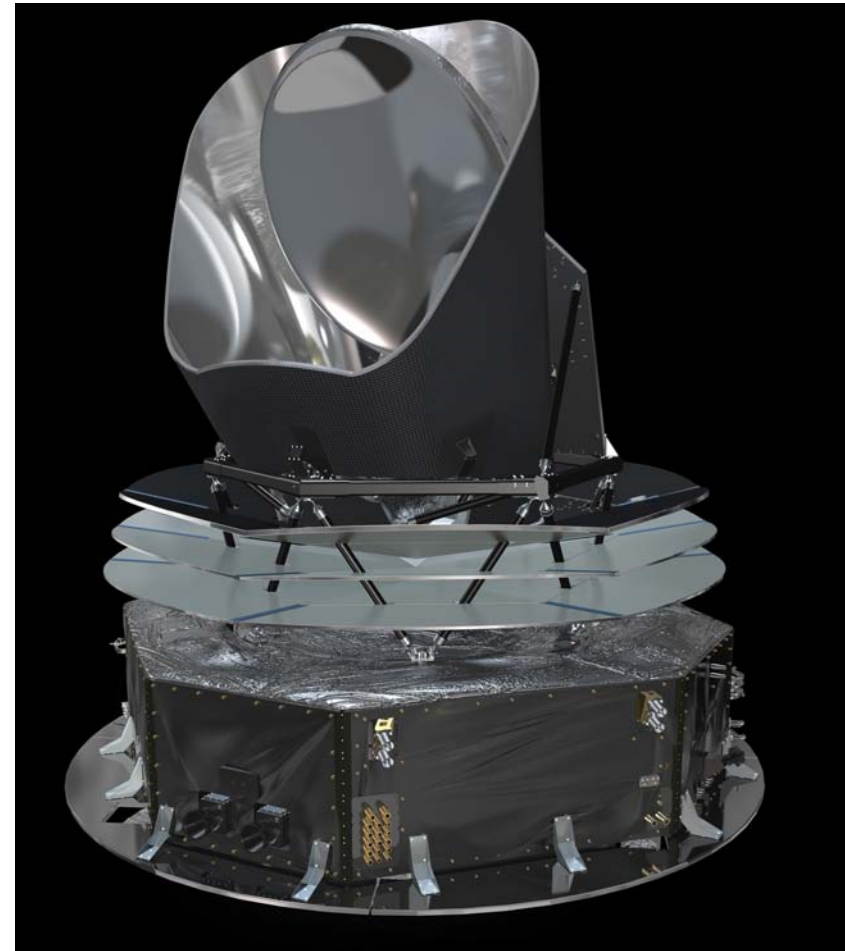
Those not seen in IRAS will include:

high Z ULIRGs

< 15K dust

SZ clusters

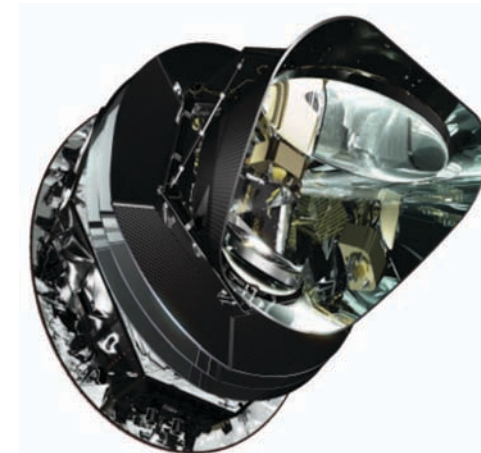
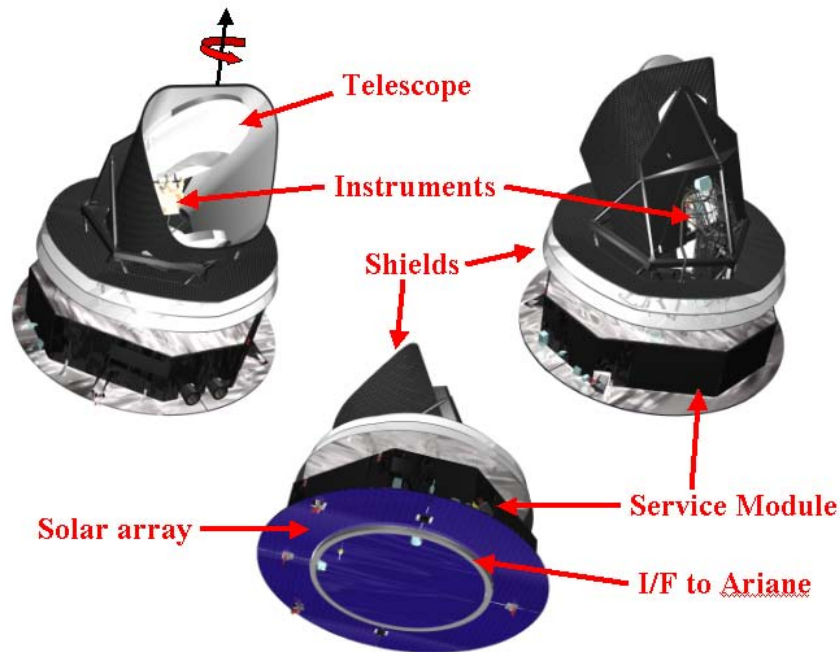
radio bright galaxies



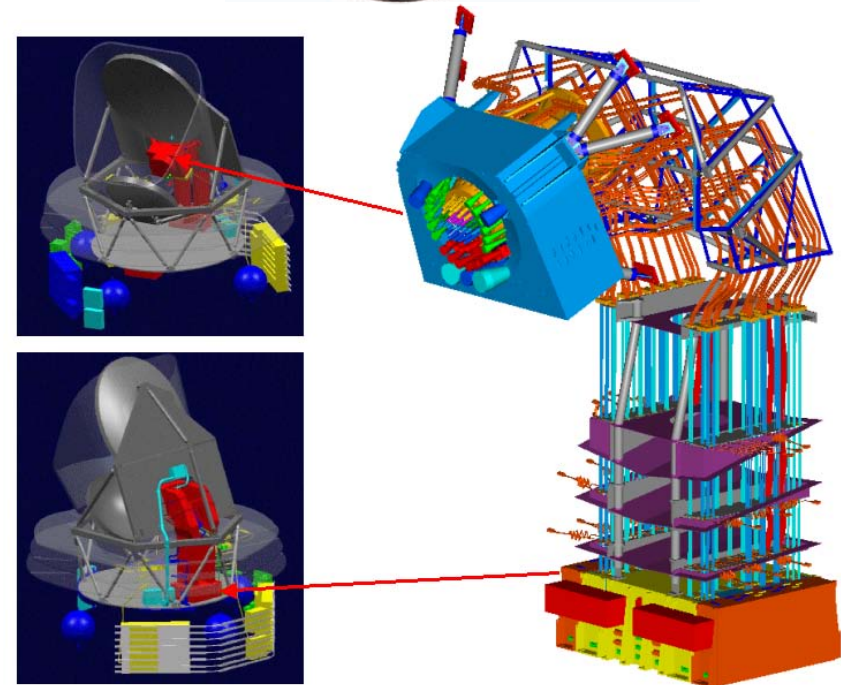
- Planck w Kourou i artystyczna wizja Plancka na orbicie

**Kourou, French Guyana, May 14, '09, 10.12am
LAUNCH!**



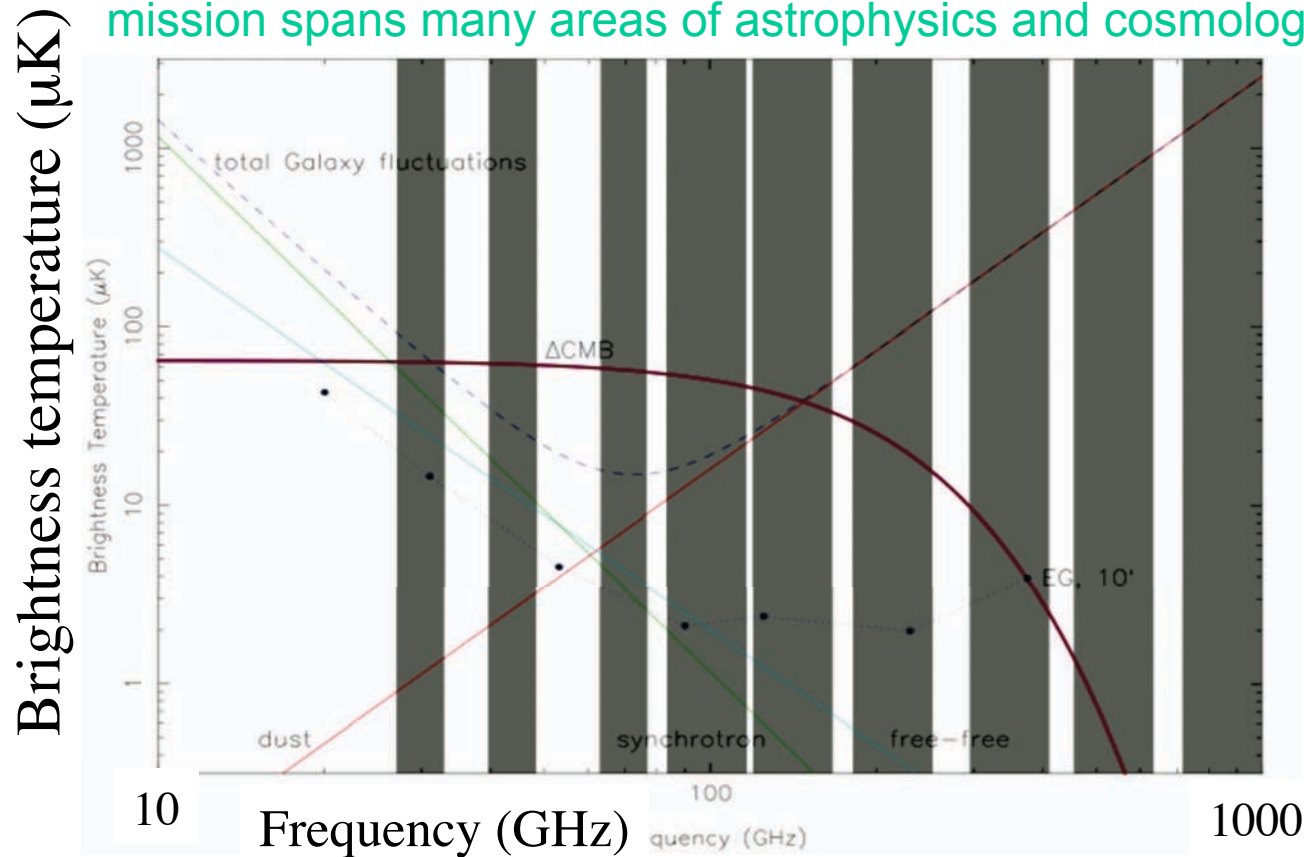


Planck has two instruments, the Low Frequency Instrument (LFI) and the High Frequency Instrument (HFI) in a shared focal plane containing 74 channels and covering an area 8 degrees-wide on the sky.



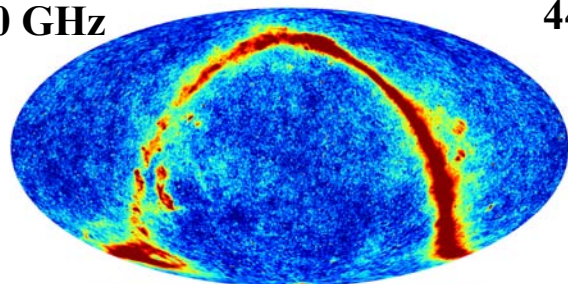
Planck is part of ESA's "Cosmic Visions" program and is currently scheduled for launch in July 2008 along with the Herschel satellite.

Planck will be the first sub-mm mission to map the entire sky with mJy sensitivity with resolution better than 10 arcminutes. The science enabled by such a mission spans many areas of astrophysics and cosmology.

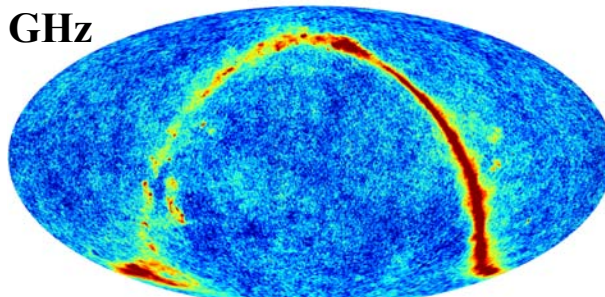


Simulated 9-frequency Planck Data Set for Temperature

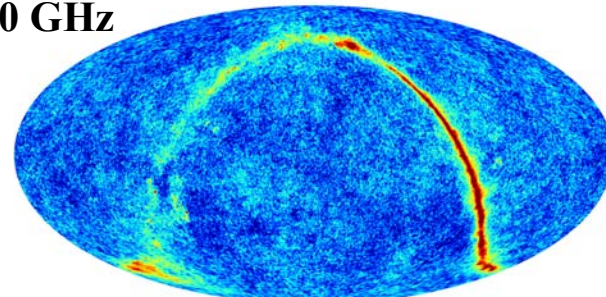
30 GHz



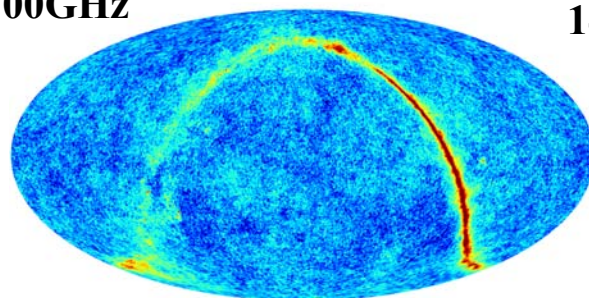
44 GHz



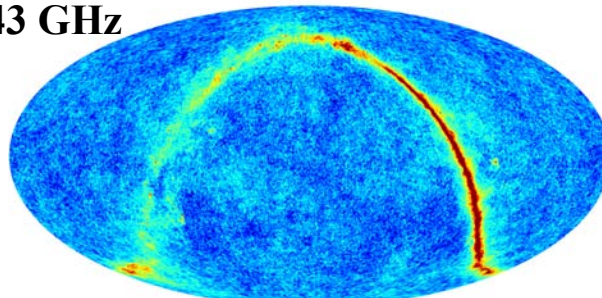
70 GHz



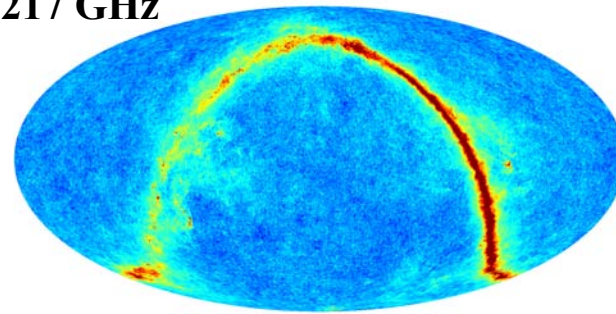
100GHz



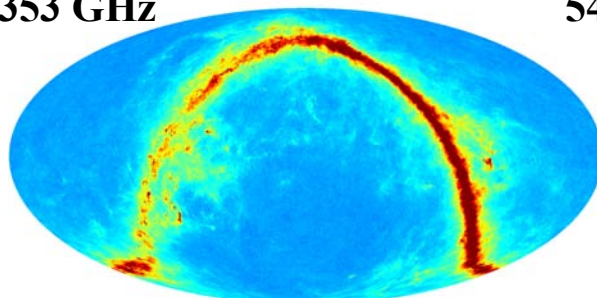
143 GHz



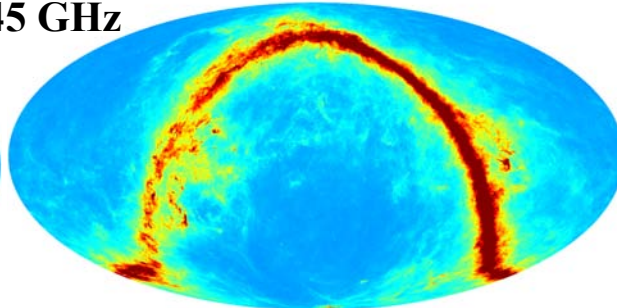
217 GHz



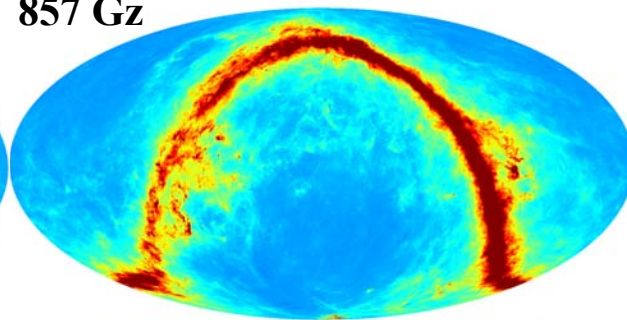
353 GHz

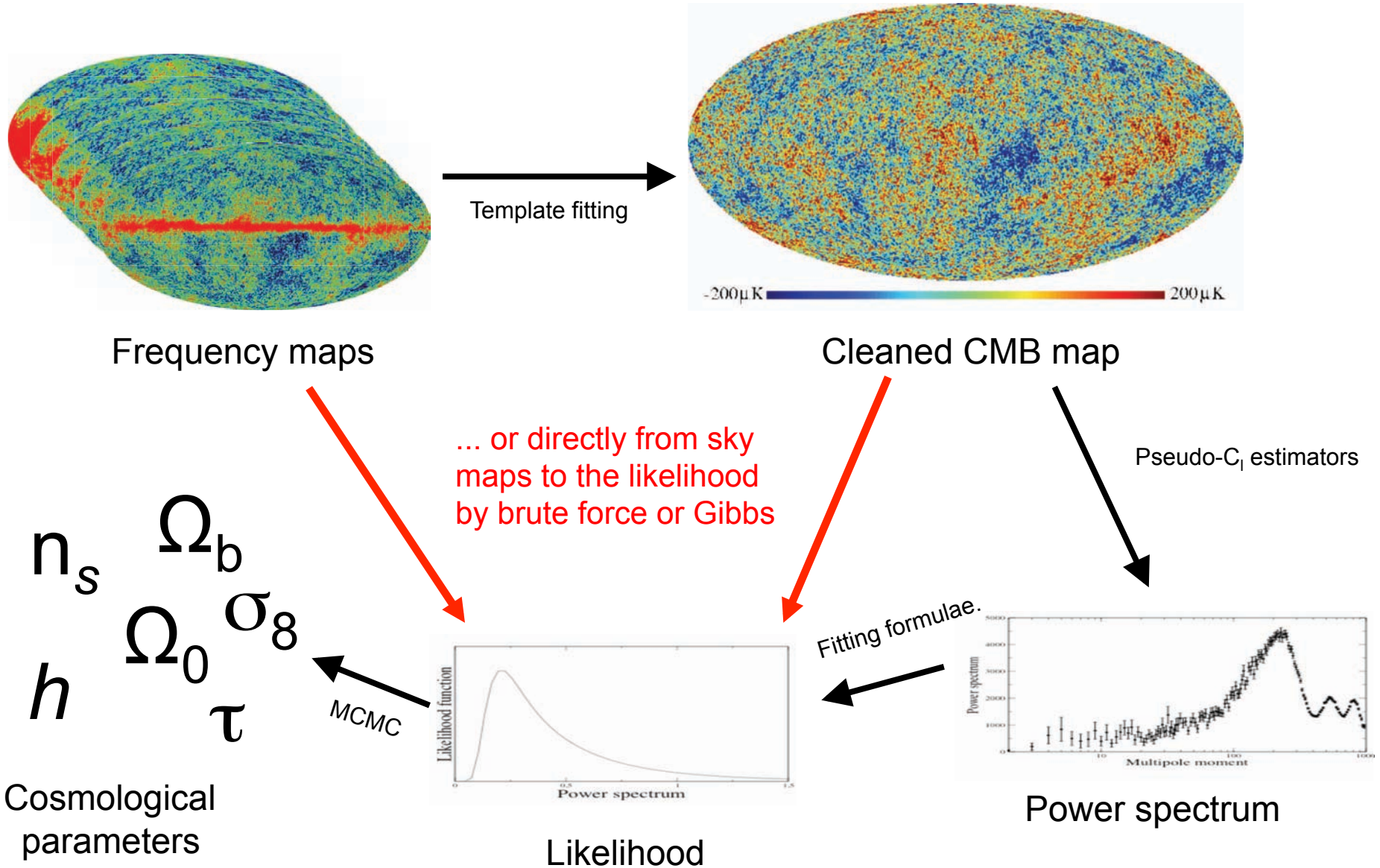


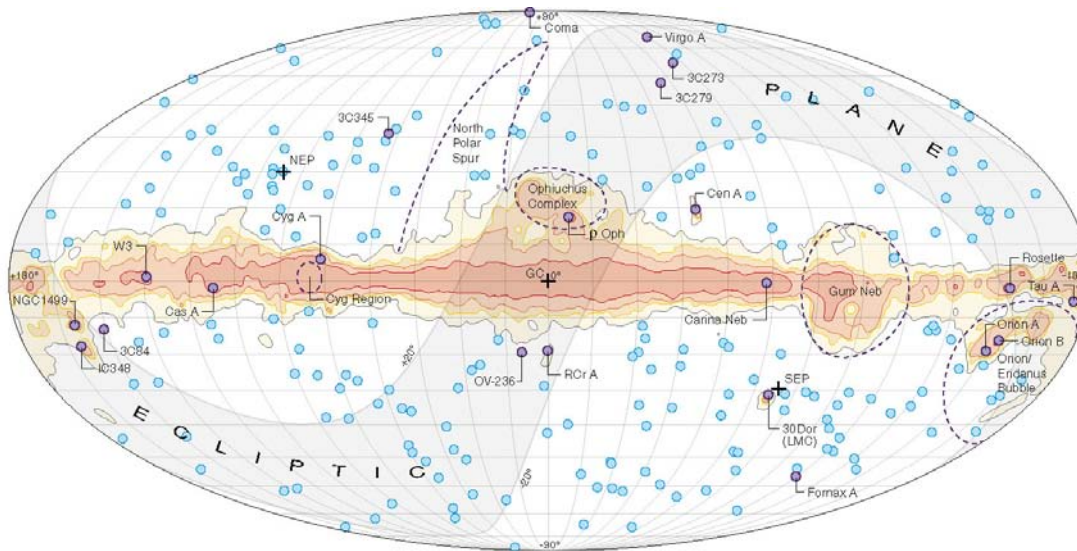
545 GHz



857 Gz





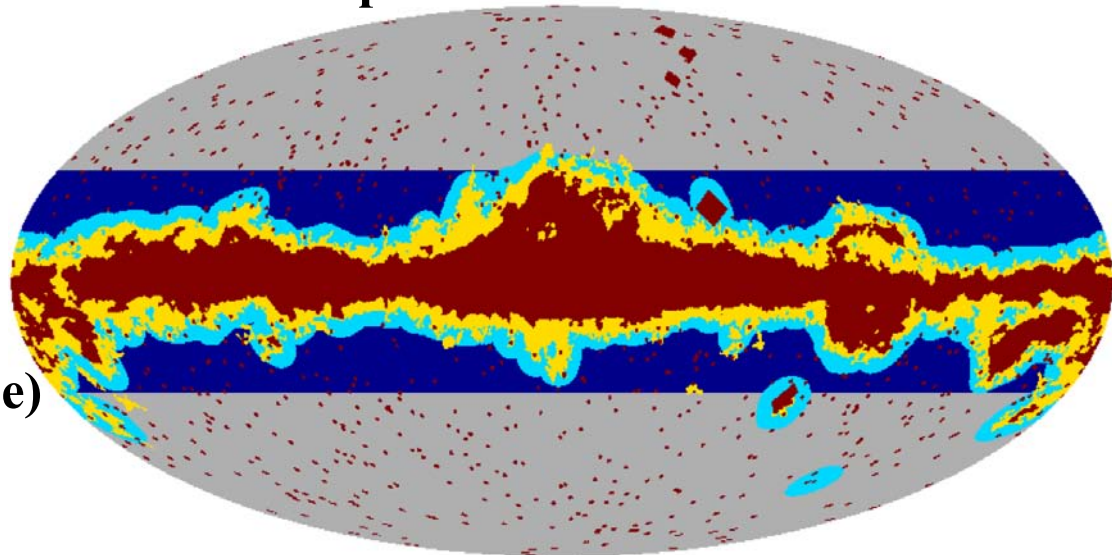


Courtesy of the WMAP Science Team

Representative masks

KQ85 (red)
KQ75 (yellow)
KQ75 ext (light blue)
 $|b| < 30$ degrees (dark blue)

Point sources (red)





Foreground Separation



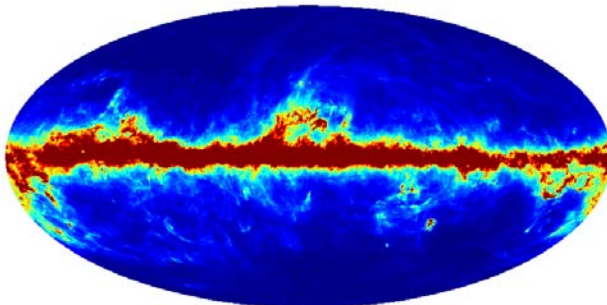
From Eriksen, Jewell, Dickinson, Banday, Górski, & Lawrence; → ApJ 2007

$$d(\mathbf{p}, \nu) = s + \underbrace{\left(\sum_j a_j(\nu) t_j(\mathbf{p}) \right)}_{\text{Monopole, Dipole, Dust: Fit for amplitude at each frequency}} + \underbrace{\left(\sum_k b_k \left(\frac{\nu}{\nu_{0,k}} \right)^{\beta_k} f_k(\mathbf{p}) \right)}_{\text{Free-Free: Fit for amplitude}} + \underbrace{\left(c(\mathbf{p}) \left(\frac{\nu}{\nu_{ref}} \right)^{\alpha(\mathbf{p})} \right)}_{\text{Synchrotron: Fit pixel independent amplitudes, and spatially varying spectral index}} + n(\mathbf{p}, \nu)$$

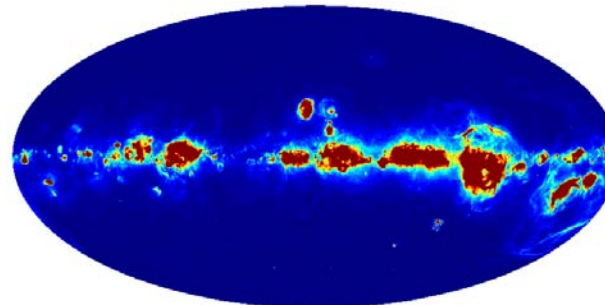
**Monopole, Dipole,
Dust:**
Fit for amplitude
at each frequency

Free-Free:
Fit for amplitude

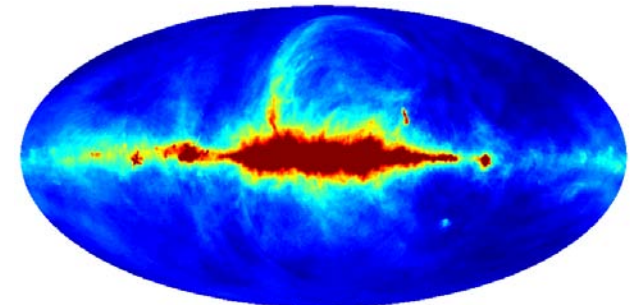
Synchrotron:
Fit pixel independent
amplitudes, and
spatially varying
spectral index



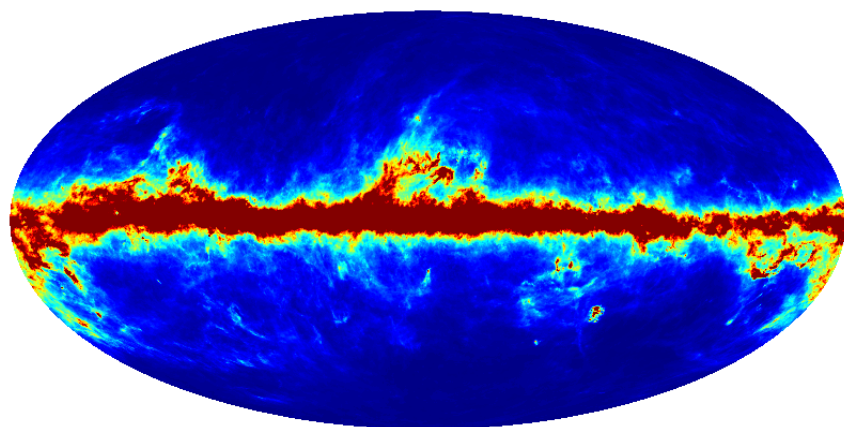
FDS



H-alpha



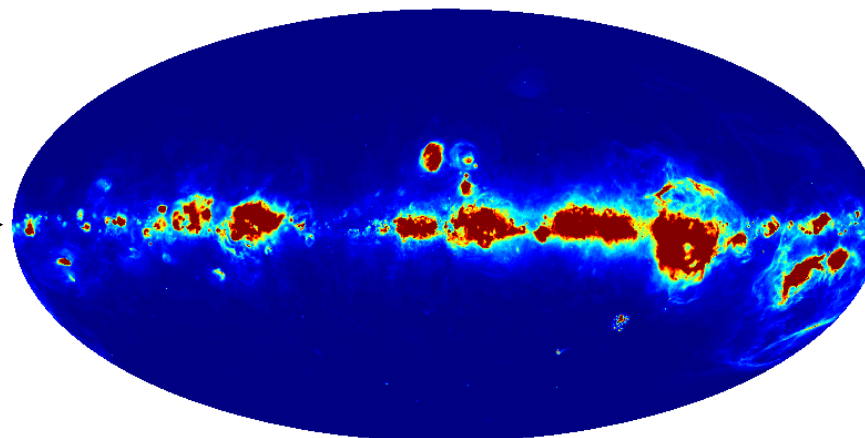
Haslam



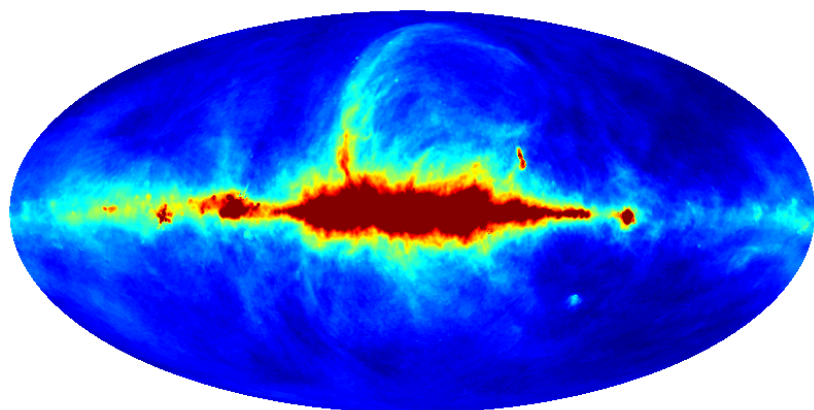
+0.448  +100.

Dust emission according to the Finkbeiner Davis & Schlegel map derived from IRAS and DIRBE observations

Free-free Emission traced by H-alpha



+9.884E-02  +100.



+11.5  +100.

Synchrotron Emission traced by Haslam radio survey



Foreground Separation - Commander vs. WMAP3

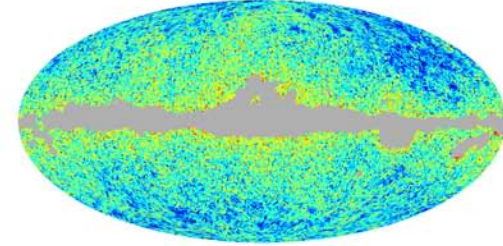
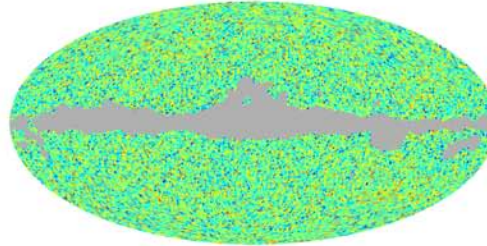
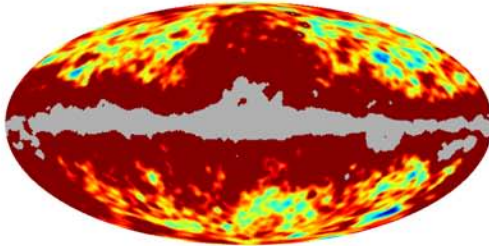


Commander model

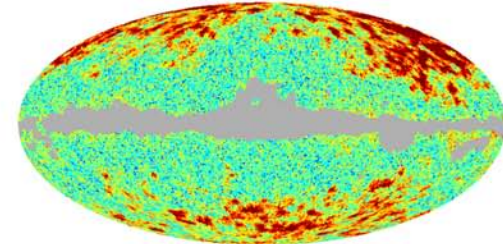
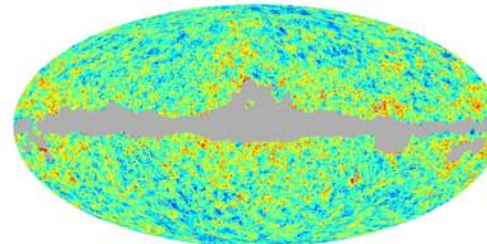
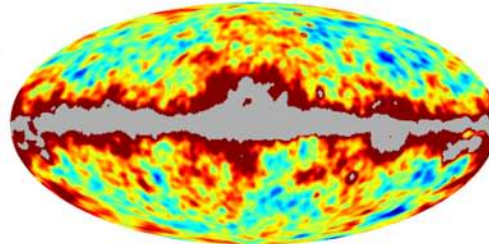
Data - Commander model

Data - WMAP model

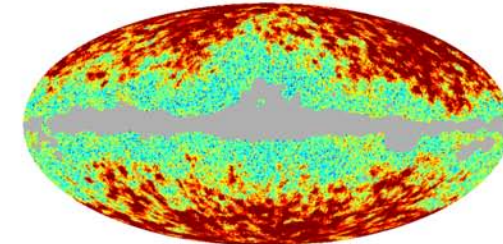
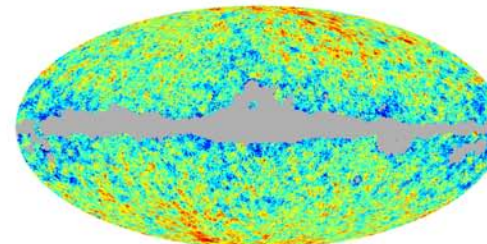
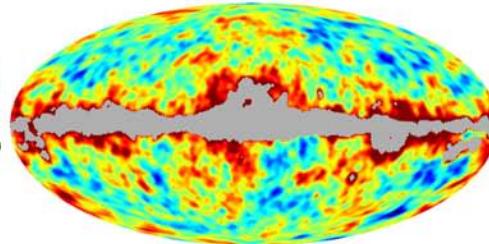
K-band



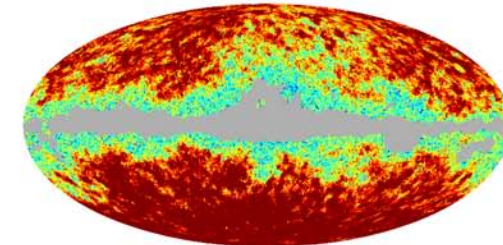
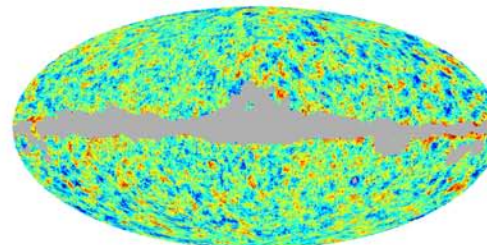
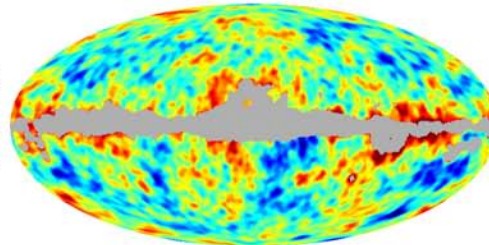
Ka-band



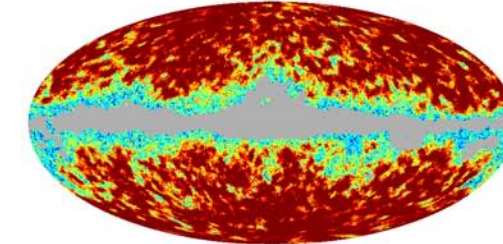
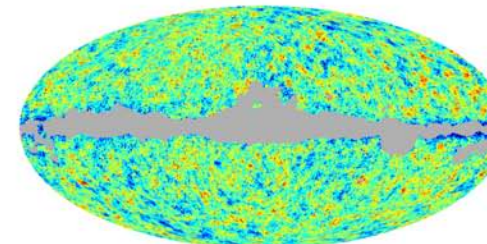
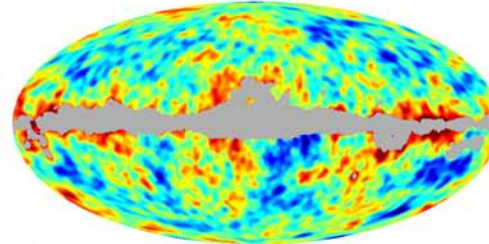
Q-band



V-band



W-band



-150 μ K 150 μ K

-10 μ K 10 μ K

-10 μ K 10 μ K

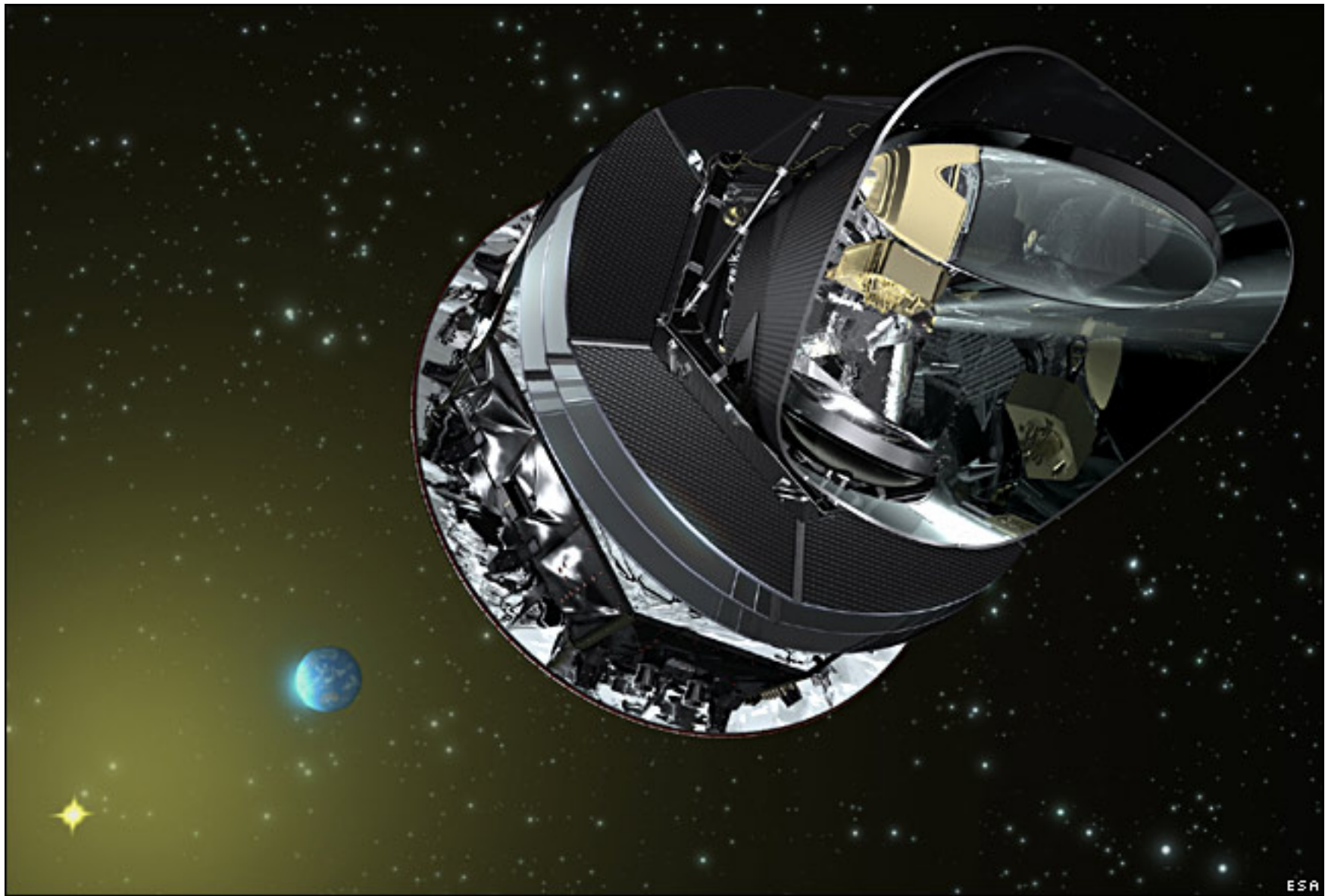
NAIL IN THE COFFIN

leroisimo,
ept. 2011

- Planck data volume drives (almost) everything
 - LFI :
 - 22 detectors with 32.5, 45 & 76.8 Hz sampling
 - 4×10^{10} samples per year
 - **0.2 TB time-ordered data + 1.0 TB full detector pointing data**
 - HFI :
 - 52 detectors with 200 Hz sampling
 - 3×10^{11} samples per year
 - **1.3 TB time-ordered data + 0.2 TB full boresight pointing data**
 - LevelS (simulation example) :
 - 4 LFI detectors with 32.5 Hz sampling
 - 4×10^9 samples per year
 - 2 scans x 2 beams x 2 samplings x 7 components + 2 noises
 - **1.0 TB time-ordered data + 0.2 TB full detector pointing data**



Enter Planck ...

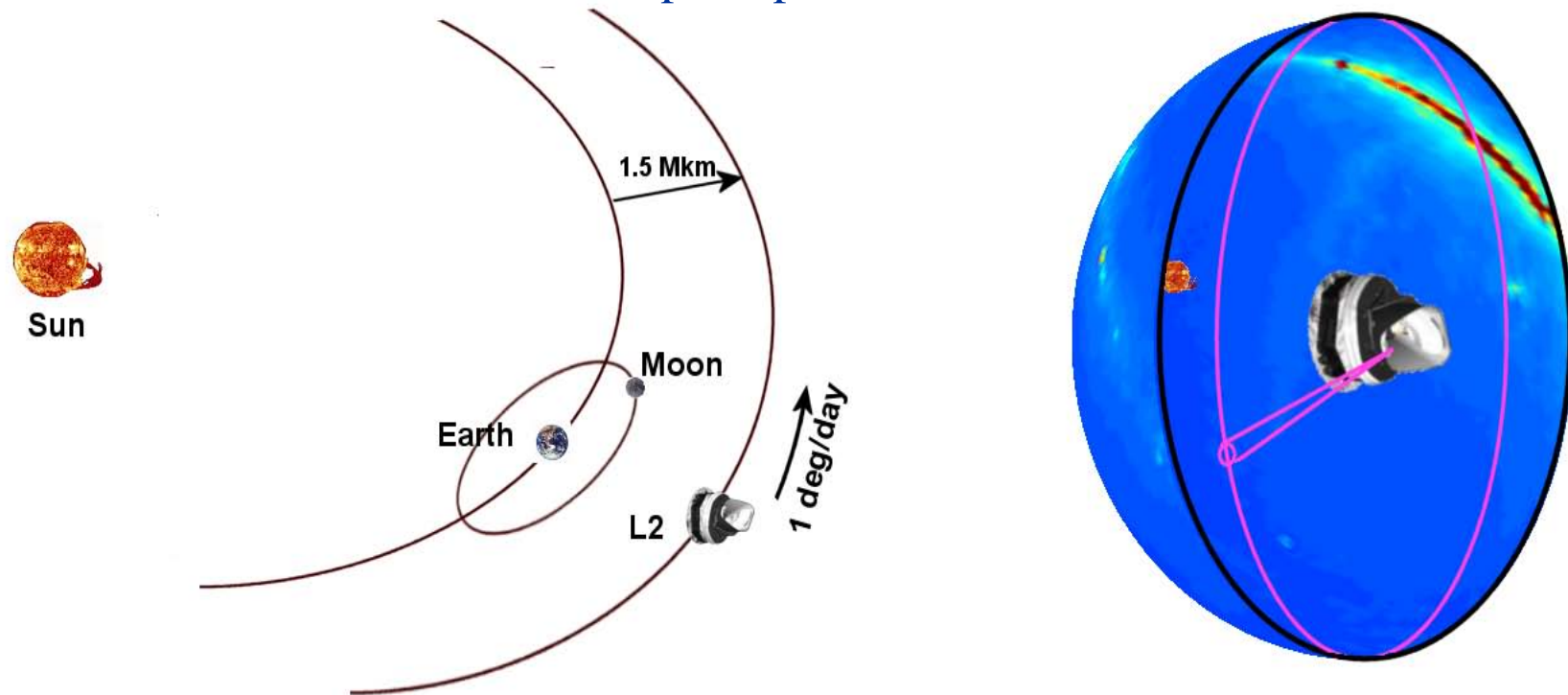


ESA

Planck will make its measurements from the Earth-Sun L_2 point.

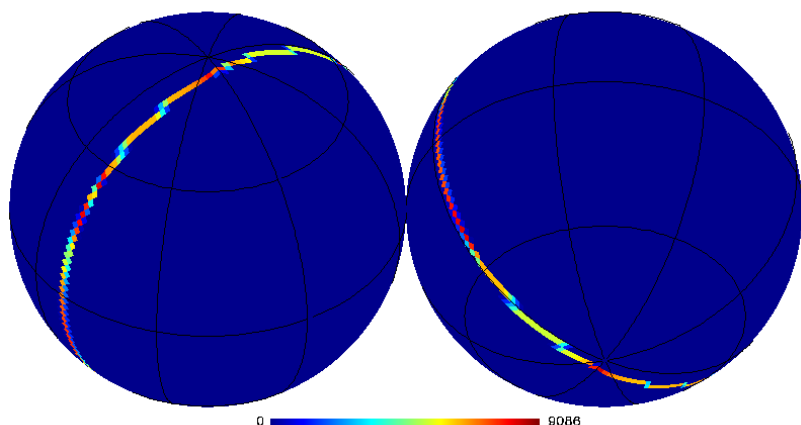
It will make a map of the full sky every 6 months.

Currently, it is planned to run for 14 months, but should be extended to \sim twice that for HFI, perhaps more for LFI.

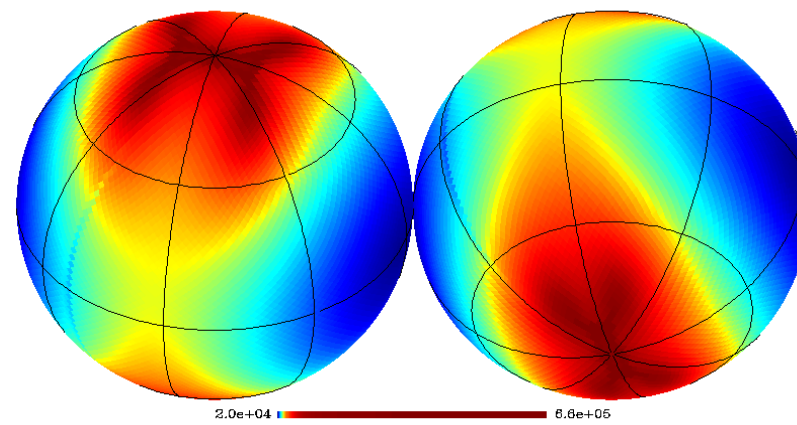


Planck Scanning Strategy – Slow (6-months) Precession Case

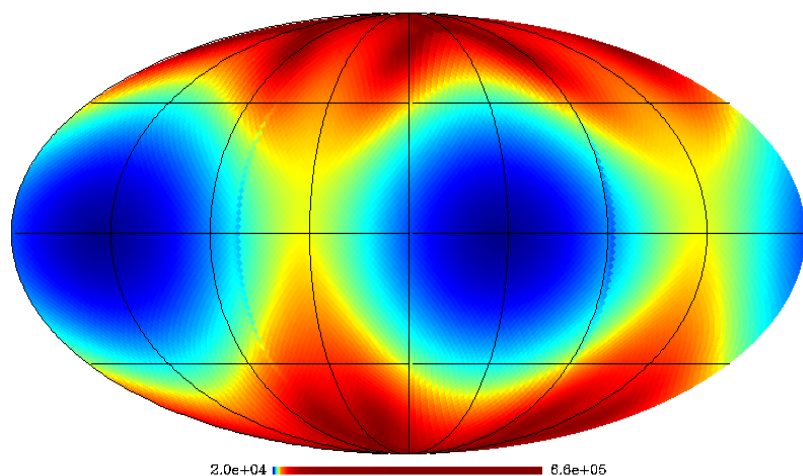
Planck 1day



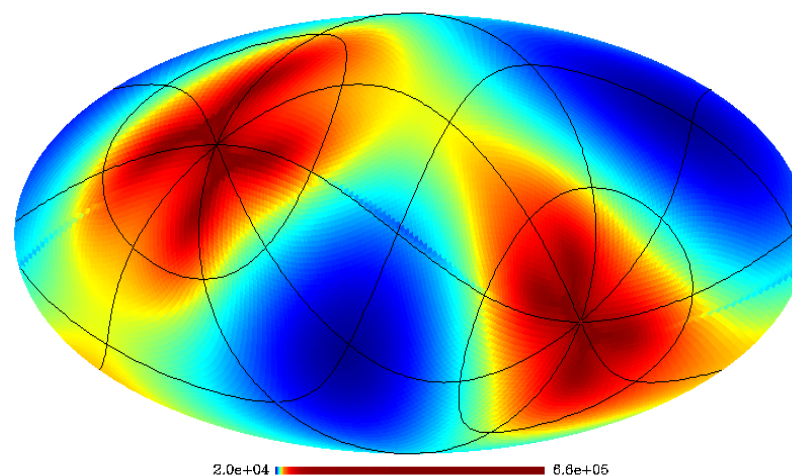
Planck 1yr



Planck 1yr



Planck 1yr

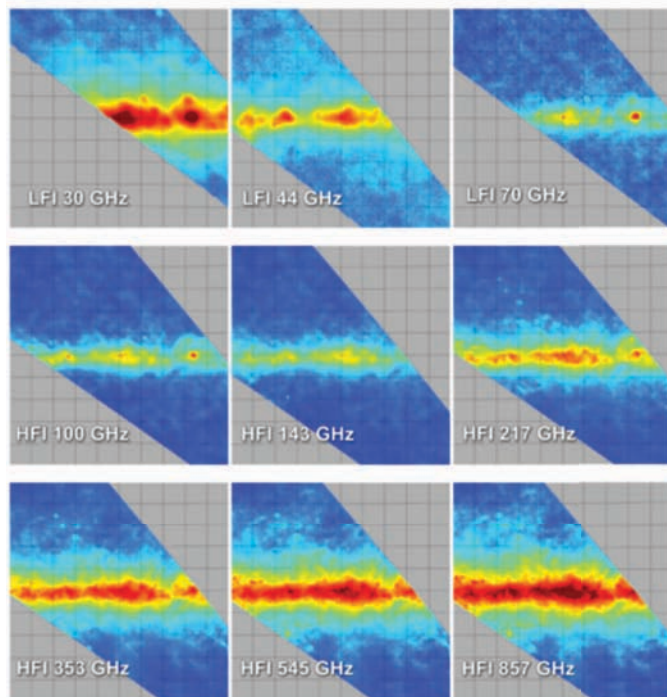




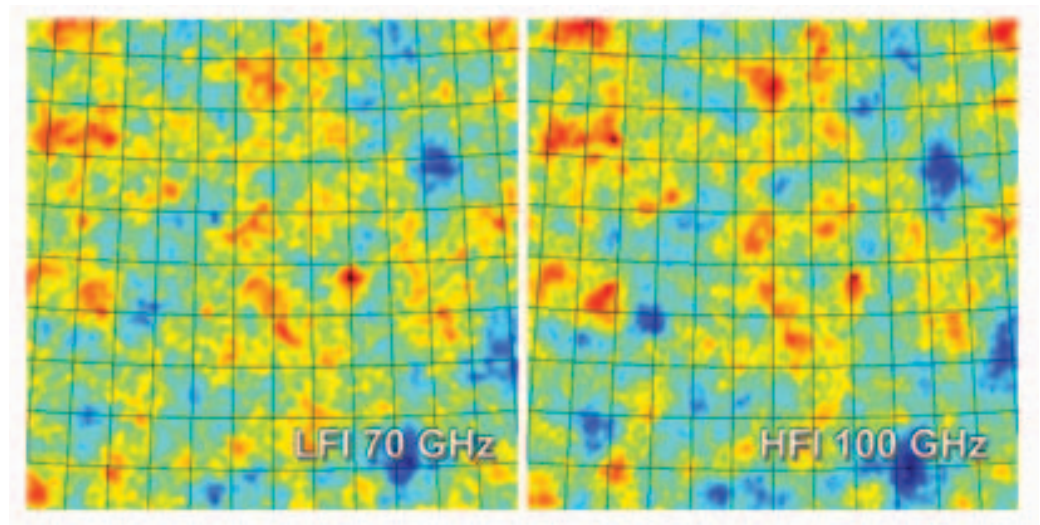
First PR snapshots from Planck



The Planck First Light Survey



Mosaic of maps at 9 different frequencies, showing part of the Milky Way



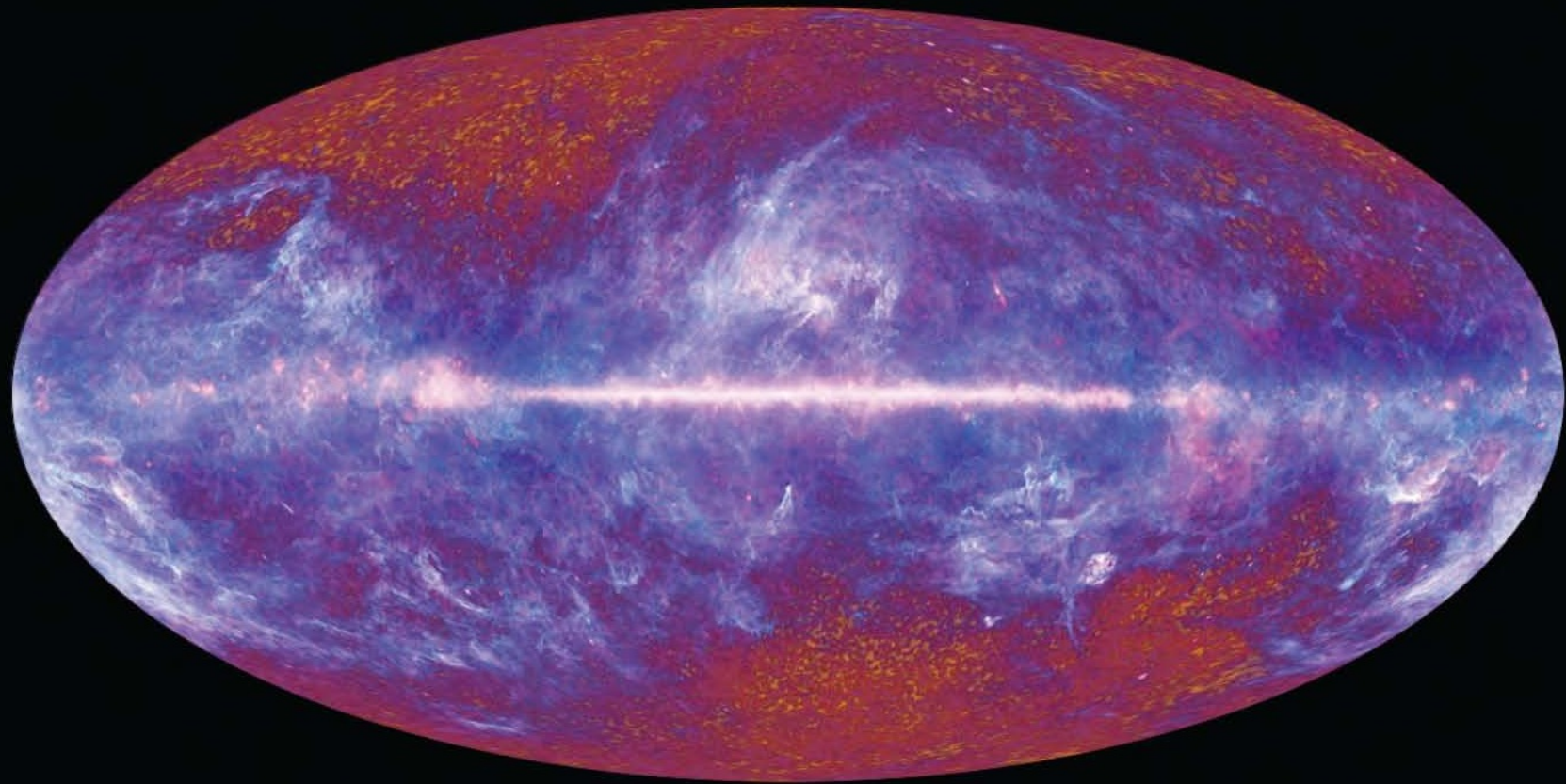
Maps of the high-galactic-latitude sky at 70 and 100 GHz

Copyright: ESA, HFI & LFI Consortia (Planck)





Planck's Universe



The Planck one-year all-sky survey



[c] ESA, HFI and LFI consortia, July 2010



Plank Data Processing and Analysis Scope



- 50 x the data volume of WMAP
- 3 x the angular resolution \Rightarrow 10 x as many pixels in maps
- 10 x lower noise \Rightarrow deal with 10 x lower systematics
- 2 x as many frequencies
- Data analysis is a much bigger and harder job than for WMAP!
 - Approximately 10 x

● Motivation (in a nutshell):

- Find out if residuals of the $1/f^2$ detector noise remaining in the sky maps made from the TODs with correlated noise compromise Planck's ability to measure the low- l reionization features in the TQU power spectra

● Input Data:

- Generated by Level S Simulation Pipeline
- Involved: G. Rocha, G. Prezeau, I. O'Dwyer, K. Huppenberger, C. Cantalupo
- TOD Volume: about ~1.5 TB at all channels

● Map Making:

- G. Rocha run DPC compliant version of Springtide to generate 3 TQU maps
- M. Ashdown helped with running Springtide to generate the internally coadded single TQU map

● Power Spectrum Evaluation

- Simple galactic cut developed by C. Cantalupo (based on thresholded, smoothed SFD Galaxy dust emission map; ~60% of the sky retained)
- KMG: HEALPix (MPI) anafast runs on full and cut-sky maps – Sun/Linux 64bit, 4CPU, 32GB RAM machine at JPL; single anafast run on $N_{\text{side}}=2048$, $l_{\text{max}}=3000$ TQU map (~600 MB size) takes ~4 mins CPU

4

C. Rosset et al.: Beam mismatch in

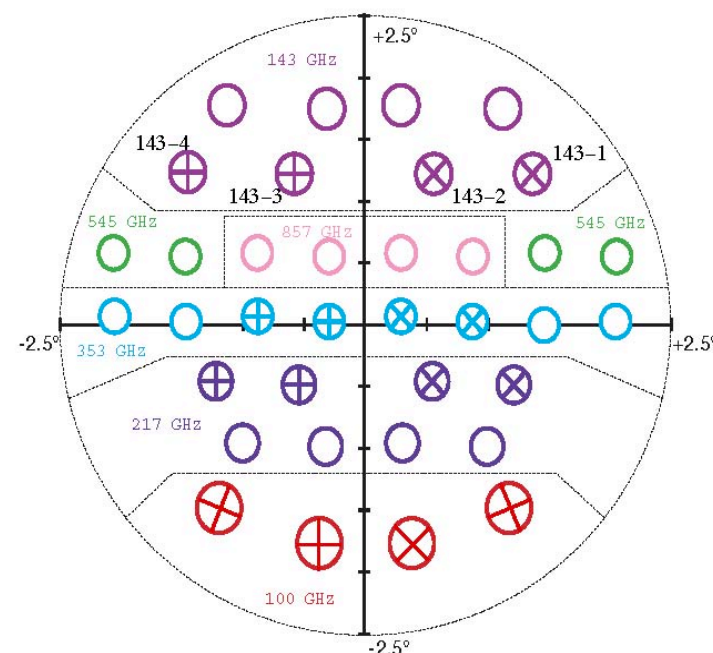
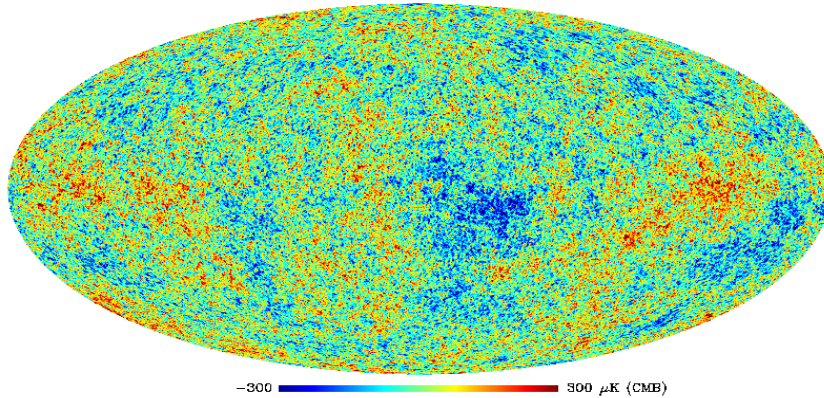


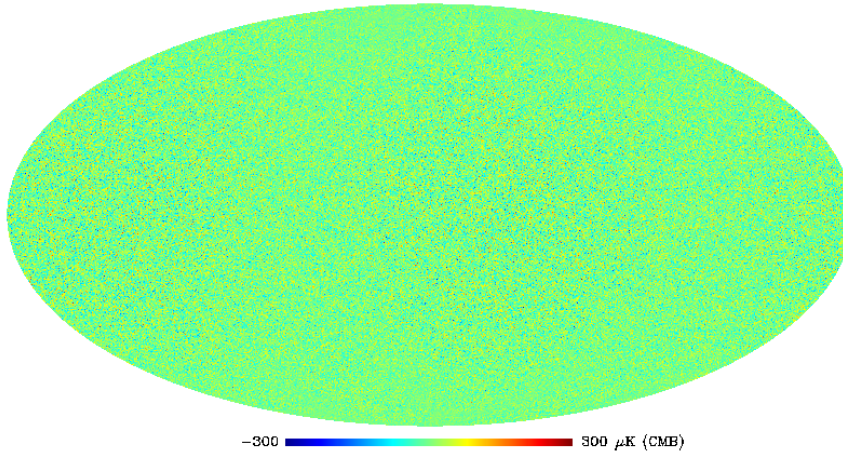
Fig. 2. Planck focal plane with polarization sensitive bolometers as seen from the sky. Complementary pairs of PSB detectors are arranged in two horns following each other while scanning the sky so that four detectors are in an optimized configuration for polarization measurement.

on line processing :
Nside=2048, T

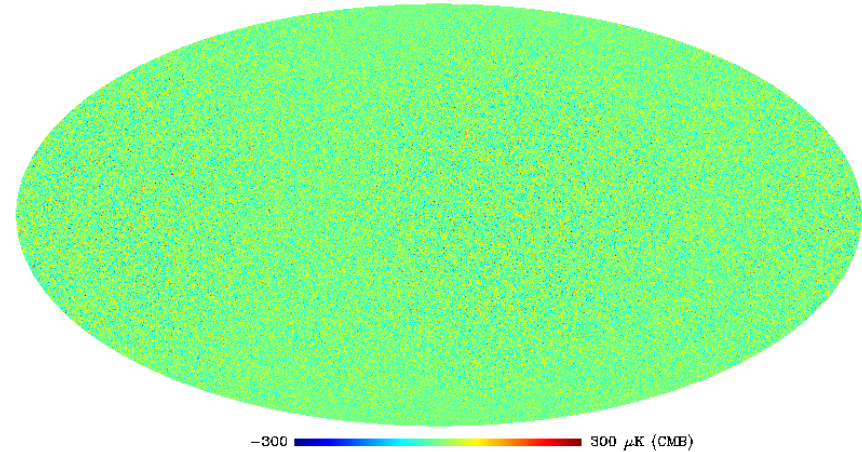


The input CMB signals for these simulations were generated by matching spherical harmonics up to $l = 3000$ to the WMAP data.

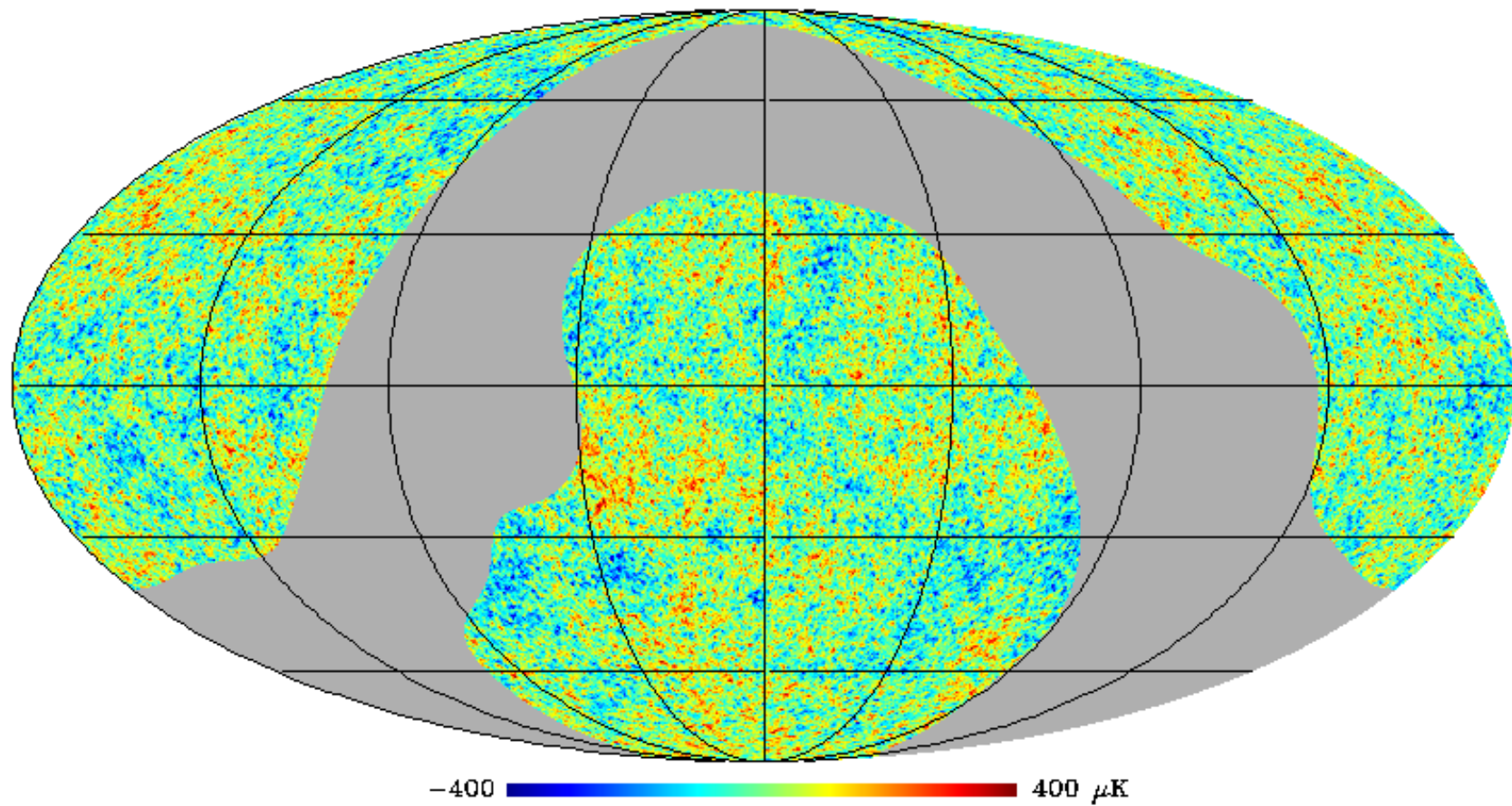
on line processing :
Nside=2048, Q



on line processing :
Nside=2048, U



HFI 143GHz Temperature





Simulation Parameters and Computational Resources



Parameters:

Detectors	8 @ 100 GHz (8 polarized) 12 @ 143 GHz (8 polarized, 4 unpolarized) 12 @ 217 GHz (8 polarized, 4 unpolarized)
Observations (ONLY CMB TQU signals are measured)	366 days @ 200 Hz = 6,324,480,000 samples per detector (× 32) Total number of samples $\sim 2.024 \times 10^{11}$
Noise Properties	White + $1/f^2$, knee=30 mHz, 6-day piecewise stationary
Scanning Strategy/Pointing	Cycloidal – slow (6 month) precession; Satellite pointing with jitter
Resolution of the Sky Maps	HEALPix $N_{\text{side}} = 2048$ — 50,331,648 × 1.7' pixels per Stokes parameter

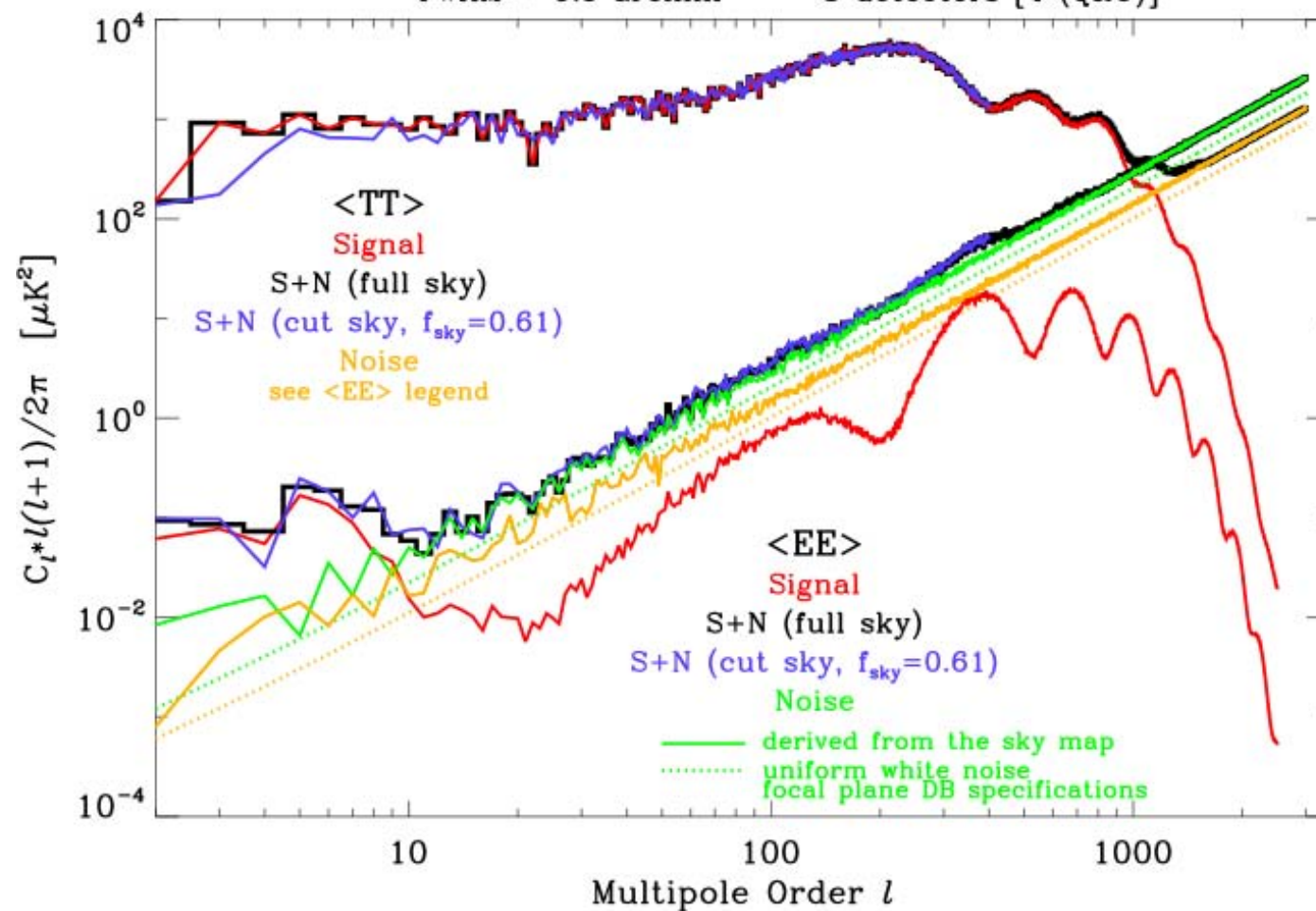
Computing:

Machines	Seaborg and Bassi at NERSC
Processors	6000 x 375 MHz; 976 x 1.9GHz
Run-time	<3 hr wallclock given CPUs deployed
Memory	Dominated by map size
Disk	~ 1.5 Tbytes (aggregate TODs)

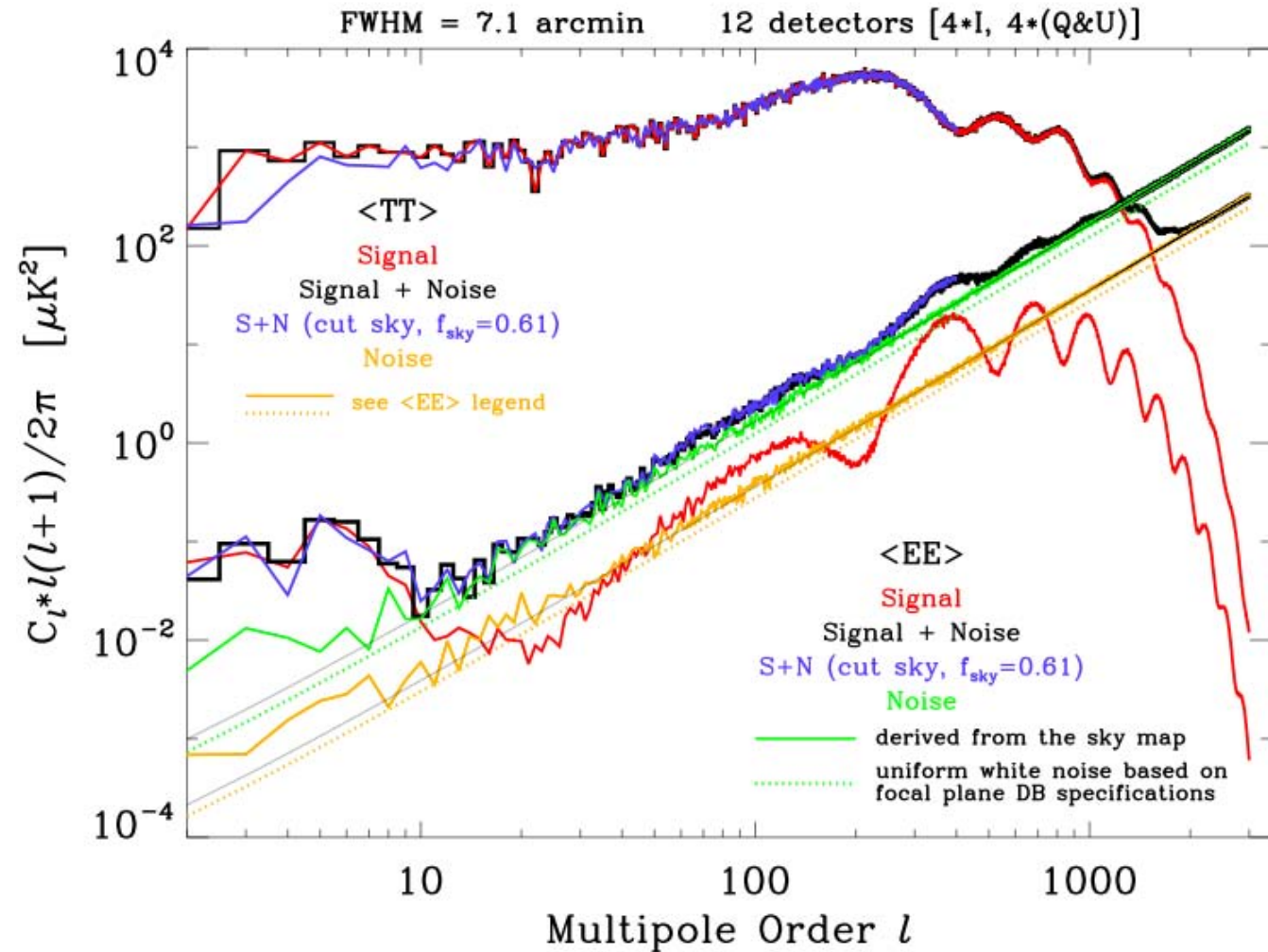
Planck-HFI 100GHz T & E Sensitivity

FWHM = 9.5 arcmin

8 detectors [4*(Q&U)]

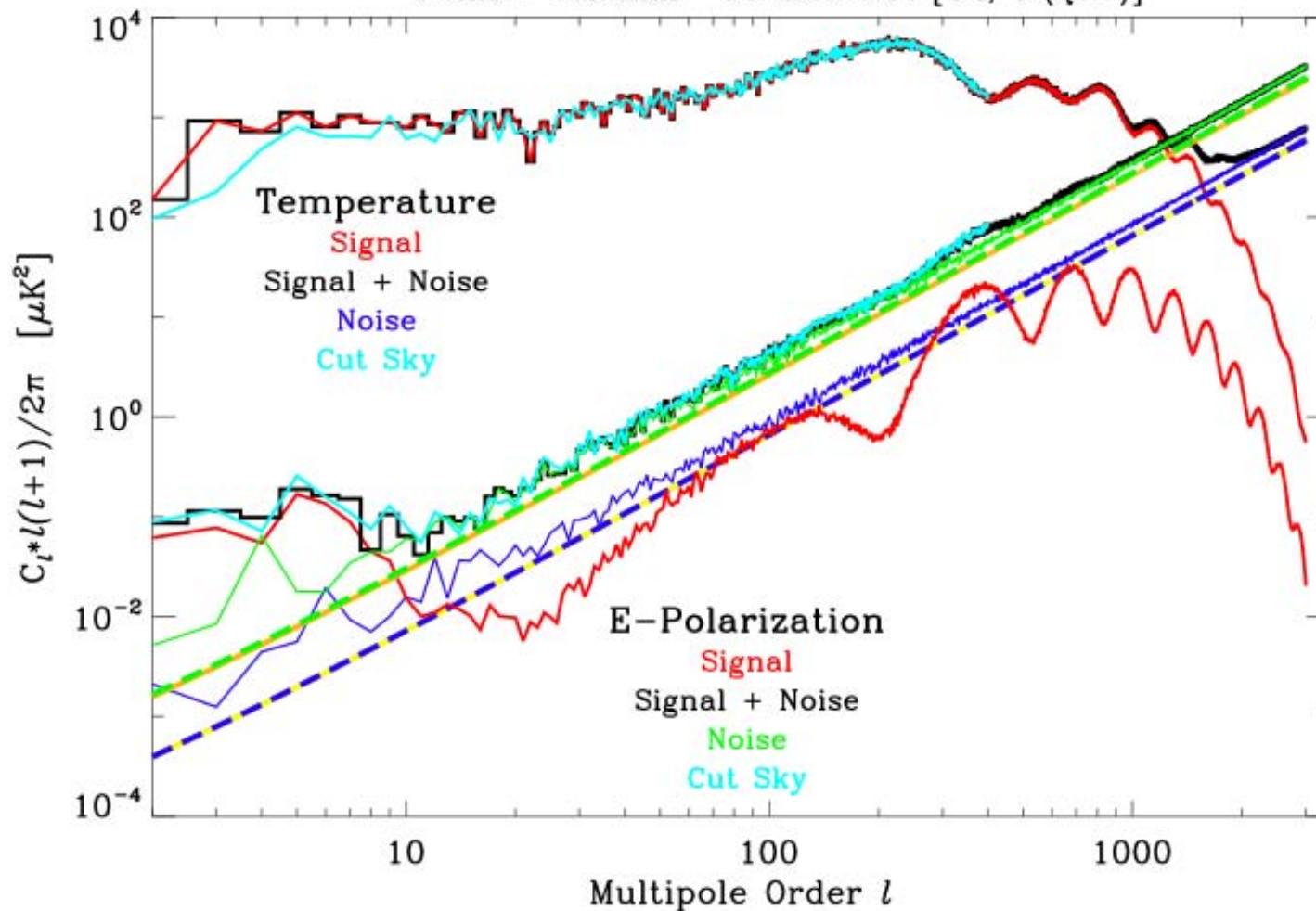


Planck-HFI 143GHz T & E Sensitivity



Planck-HFI 217GHz T & E Sensitivity

FWHM = 5 arcmin 12 detectors [4*I, 4*(Q&U)]



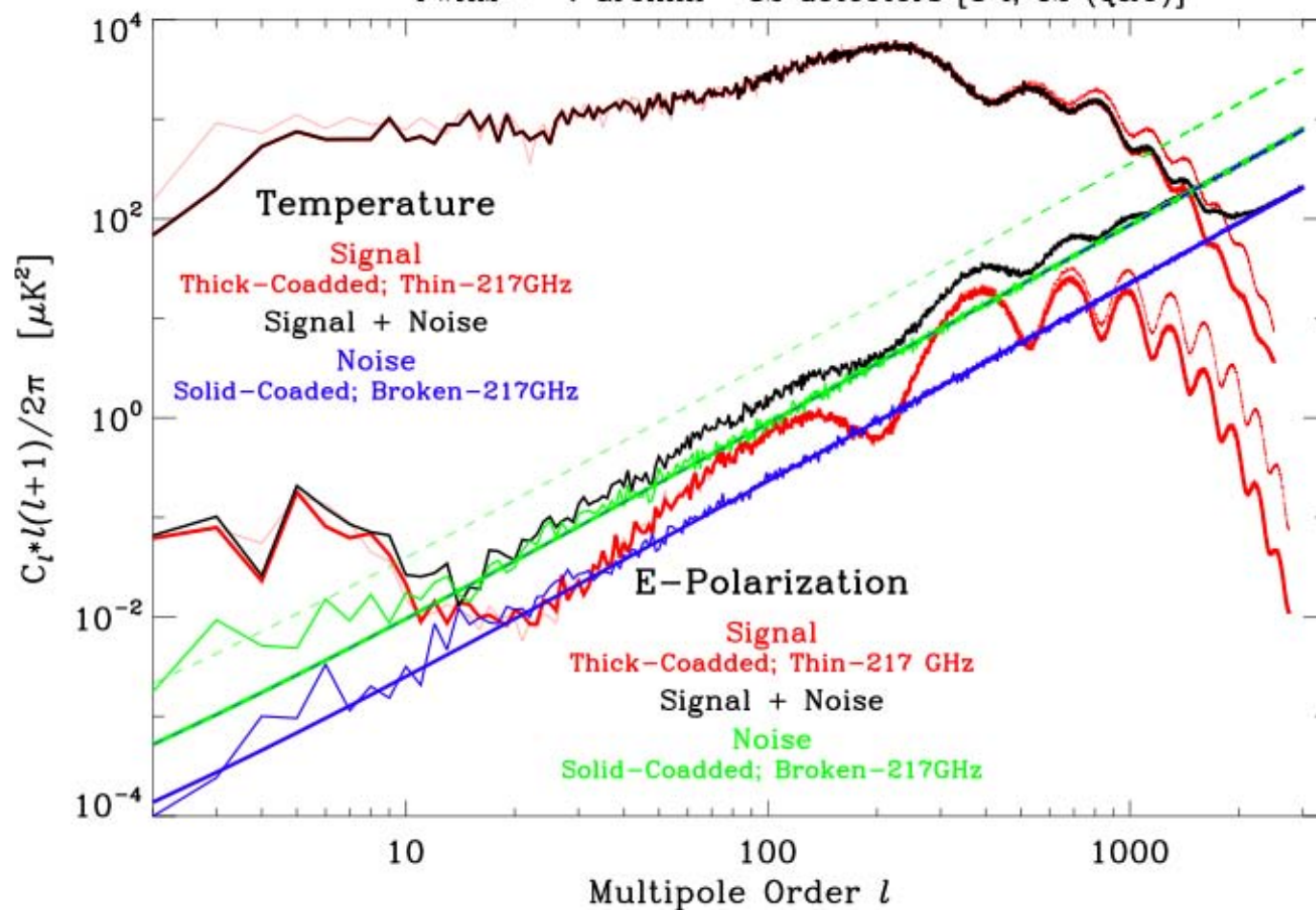


Coadded 100/143/217 GHz Channels



Planck-HFI 100+143+217 GHz T & E Sensitivity

FWHM = ? arcmin 32 detectors [8*I, 12*(Q&U)]



- After Planck, we will have very precise knowledge of the universe at $z \sim 1000$.
- We will have tightly constrained the physical densities of matter and baryons, the amplitude of the fluctuations in the linear phase over 3 decades in length scale and the shape of the primordial power spectrum.
- Our knowledge of physical conditions and large-scale structure at $z \sim 10^3$ will be better than our knowledge of such quantities at $z \sim 0$!
- If dark energy is a recent phenomenon, then we can translate this knowledge reliably to intermediate redshifts which are currently at the observational frontier.
- This CMB “prior” is assumed by all Beyond Einstein concepts, etc. (e.g., all JDEM concepts, Cosmic Inflation Probe, CMBPol)



After launch, before lunch ...
with Planck PIs - Reno Mandolesi and Jean Loup Puget



Krzysztof M. Górski

Azores School on Observational Cosmology, Angra do Heroísmo,
Sept. 2011



Joint Core Teams of Planck



Krzysztof M. Górski

Azores School on Observational Cosmology, Angra do Heroismo,
Sept. 2011



END