## Report on Task 2 and further work

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- Introduction (Codes involved and procedure)
-Frequency comparison
-Large separation comparison
-Small separation comparison
-Conclusions and further work


## INTRODUCTION

## Equilibrium model

| $\mathrm{M} / \mathrm{M}_{\odot}$ | $\log \mathrm{T}_{\text {eff }}$ | $\log \mathrm{g}$ | $\log \mathrm{L} / \mathrm{L}_{\Theta}$ | $\mathrm{R} / \mathrm{R}_{\Theta}$ | $\mathrm{X}_{\mathrm{C}}$ | Age <br> $(\mathrm{My})$ | Mesh <br> points |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.2 | 3.800 | 4.399 | 0.250 | 1.146 | 0.69 | 96.7 | 902 |

## MODCONV

|  | ADIPLS | POSC | NOC | GraCo | FILOU | LOC | OSCROX |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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## Frequency comparison

## Absolute values

## $\ell=0$ and 1

## $\ell=2$ and 3

Absolute comparison $\mathrm{L}=0$ and $\mathrm{L}=1$


Absolute comparison $\mathrm{L}=2$ and $\mathrm{L}=3$


## Frequency comparison

## Absolute differences

## $\ell=1$ and 2 <br> l $=0$ and 1 <br> $$
\ell=0
$$ <br> $$
\ell=0 \text { and } 1
$$



## Frequency comparison

## Summary of differences resp. LOC

|  | $\ell=0$ |  | $\ell=1$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Absolute difference | $\%$ <br> difference | Absolute difference | $\%$ <br> difference |
| ADIPLS | 0.12 | 0.011 | 0.12 | 0.012 |
| POSC | 1.5 | 0.039 | 0.12 | 0.012 |
| NOC (no <br> Richard.) | 10.5 | 0.268 | 10.11 | 0.26 |
| GraCo | 5.81 | 0.149 | 4.28 | 0.11 |
| FILOU | 5.33 | 0.136 | 6.28 | 0.159 |
| OSCROX | 1.96 | 0.05 | 0.14 | 0.003 |

## Large separation comparison

## Absolute values

## $\ell=2$ and 3 <br> $\ell=0 \quad \ell=0$ and 1



$\mathrm{L}=0$ and $\mathrm{L}=1$


## Large separation comparison

## Absolute differences

## $\ell=1$ and 2 <br> $$
\ell=0 \text { and } 1
$$

$\ell=0$


## Large separation comparison

## Summary of differences resp. LOC

|  | $\ell=0$ |  | $\ell=1$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Absolute difference | $\%$ <br> difference | Absolut difference | $\%$ <br> difference |
| ADIPLS | 0.038 | 0.032 | 0.037 | 0.031 |
| POSC | 0.103 | 0.083 | 0.041 | 0.034 |
| NOC (no <br> Richard.) | 0.972 | 0.79 | 0.952 | 0.77 |
| GraCo | 0.411 | 0.335 | 0.316 | 0.258 |
| FILOU | 0.354 | 0.354 | 0.396 | 0.396 |
| OSCROX | 0.255 | 0.207 | 0.037 | 0.031 |

## Small separation comparison

## Absolute values

## $\ell=0-2$

$\ell=1-3$



## Small separation comparison

## Absolute differences

## $\ell=0-2$

Small separation (Resp. LOC) L=0-2

$\ell=1-3$


## Small separation comparison

## Relative differences



## Small separation comparison

## Summary of differences resp. LOC

|  | $\ell=0$ |  | $\ell=1$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Absolute difference | $\%$ <br> difference | Absolute difference | $\%$ <br> difference |
| ADIPLS | 0.023 | 0.23 | 0.0079 | 0.039 |
| POSC | 1.027 | 8.91 | 0.028 | 0.149 |
| NOC (no <br> Richard.) | 0.083 | 0.712 | 0.135 | 0.709 |
| GraCo | 1.519 | 13.4 | 0.0972 | 0.527 |
| FILOU | 0.653 | 5.77 | 0.088 | 0.485 |
| OSCROX | 1.69 | 14.95 | 0.099 | 0.545 |

## Conclusions and further work

|  | Frequency <br> comparison |  | Large <br> separation |  | Small <br> separation |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\ell=0$ | $\ell=1$ | $\ell=0$ | $\ell=1$ | $\ell=0-2$ | $\ell=1-3$ |
| Absolute <br> diff. | 10 | 10 | 1 | 1 | 1.5 | 0.14 |
| $\%$ diff. | 0.25 | 0.25 | 0.8 | 0.8 | 16 | 0.7 |

## Conclusions and further work

1. Richardson extrapolation not used by all codes
2. We must use the same value of the gravity constant $G$
3. Is there any number of mesh points minimizing the differences? (maybe around 2000)
4. We must use the same boundary condition $\delta \mathrm{P}(\mathrm{R})=0$
5. More information and contributions in:
http://www.astro.up.pt/corot/compfreqs/task2.html

## Example about Richardson extrapolation:

|  | LOC | Graco <br> no RI | GraCo <br> with RI |
| :---: | :---: | :---: | :---: |
| Frequency <br> $\ell=0, \mathrm{n}=23$ | 2922.45 | 2925.30 | 2921.25 |

HO(FILOU) $=2924.87 \mu \mathrm{~Hz}$ $\mathrm{HO}(\mathrm{NOC})=2926.8 \mu \mathrm{~Hz}$
HO(ADIPLS) $=2922.6471 \mu \mathrm{~Hz}$ $\mathrm{HO}($ POSC $)=2923.2584 \mu \mathrm{~Hz}$

## Example about constant G :

|  | Graco | Graco | GraCo |
| :---: | :---: | :---: | :---: |
|  | $\mathrm{G}=6.673 \cdot 10^{-8}$ | $\mathrm{G}=6.67232 \cdot 10^{-8}$ | $\mathrm{G}=6.671682 \cdot 10^{-8}$ |
| Frequency | 254.0617 | 254.0482 | 254.0356 |
| HO | $\mu \mathrm{Hz}$ | $\mu \mathrm{Hz}$ | $\mu \mathrm{Hz}$ |

$\mathrm{HO}(\mathrm{LOC})=254.0304 \mu \mathrm{~Hz}$
$\mathrm{HO}(\mathrm{NOC})=254.05 \mu \mathrm{~Hz}$
$\mathrm{HO}($ ADIPLS $)=254.0438 \mu \mathrm{~Hz}$
$\mathrm{HO}(\mathrm{POSC})=254.051 \mu \mathrm{~Hz}$

|  | Groups with similar behaviors |  |  |
| :---: | :---: | :---: | :---: |
| Frequencies | LOC-ADIPLSOSCROX (linear) | POSCOSCROX (cubic) | FILOU-GraCo |
| Large separation L=0 | LOC-ADIPLSOSCROX (linear) | POSCOSCROX (cubic) | FILOU-GraCo |
| Large separation L=1 | LOC-ADIPLSOSCROX (lin)-POSCOSCROX (cubic) | FILOU-GraCo |  |
| Small separation $\mathrm{L}=0-2$ | $\begin{aligned} & \text { LOC-ADIPLS- } \\ & \text { OSCROX (lin)- } \\ & \text { NOC } \end{aligned}$ | GraCo-POSCOSCROX (cubic) |  |
| Small separation L=1-3 | $\begin{aligned} & \text { LOC-ADIPLS- } \\ & \text { OSCROX (lin)- } \\ & \text { POSC } \end{aligned}$ | GraCo-FILOUNOC |  |

We need a better knowledge about how we treat boundaries and the constants used.

Optimize number and distribution of mesh points.

## Frequency comparison

## Relative differences

$$
\ell=0
$$

## $\ell=0$ and 1




## Large separation comparison

## Relative differences



Relative Large Differences (resp. LOC) $\mathrm{L}=0$ and $\mathrm{L}=1$



