

# Toulouse-Geneva Evolution Code

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## Physical Inputs

- **Equation of state** : OPAL 2001 tables, for the appropriate value of  $Z$ .
- **Opacity** : OPAL 1996 tables
- **Nuclear reactions** : NACRE tables
- **Convection treatment** : mixing-length theory  
the mixing-length parameter  $\alpha$  is a *free parameter*
- **Chemical composition** : Grevesse&Noels 93  
chemical elements are separately treated until Mg  
the initial helium composition  $Y_0$  is a *free parameter*
- **Metallicity**

## How the code works ?

- Reading of the physical inputs
- Calculation of the **initial chemical composition** with respect to inputs  $Y_0$  and  $Z$ , and of **Grevesse&Noels 93** composition
- Calculation of an initial polytropic model
- Reading of the previous model
  - calculation of the age (previous age + time step)
  - calculation of  $L$  and  $T_{\text{eff}}$  by extrapolation of previous  $L$  and  $T_{\text{eff}}$
  - Henye method** for computation of the stellar structure at each step of the evolution

## Henyey method

- Spherical symmetry in hydrostatic equilibrium
- The star is considered to be divided into **concentric shells**
  - ➔ 1D system in which radius is divided into zones by a set of mesh points
- All quantities are evaluated at the same mesh points
- At each mesh points : 4 unknown variables  $r$ ,  $P$ ,  $T$ ,  $l$   
( $r=y_1$ ,  $P=y_2$ ,  $T=y_3$ ,  $l=y_4$ )  
K mesh points ➔  $(4K-2)$  unknown variables ( $r = l = 0$  at the centre)  
which have to fulfil  $(4K-2)$  equations

- 4 equations for the innermost interval between central point  $m^K=0$  and  $m^{K-1}$

$$C_i(r^{K-1}, P^{K-1}, T^{K-1}, l^{K-1}, P^K=P_C, T^K=T_C)=0 ; i=1,4$$

- $4(K-2)$  equations for the  $K-2$  shells of the interior

$$A_i^j = \frac{y_i^j - y_i^{j+1}}{m^j - m^{j+1}} - f_i(y_1^{j+1/2}, \dots, y_4^{j+1/2}) = 0 ; i=1,4$$

- 2 equations for the outer boundary condition :  $P = \pi(R, L)$  and  $T = \theta(R, L)$

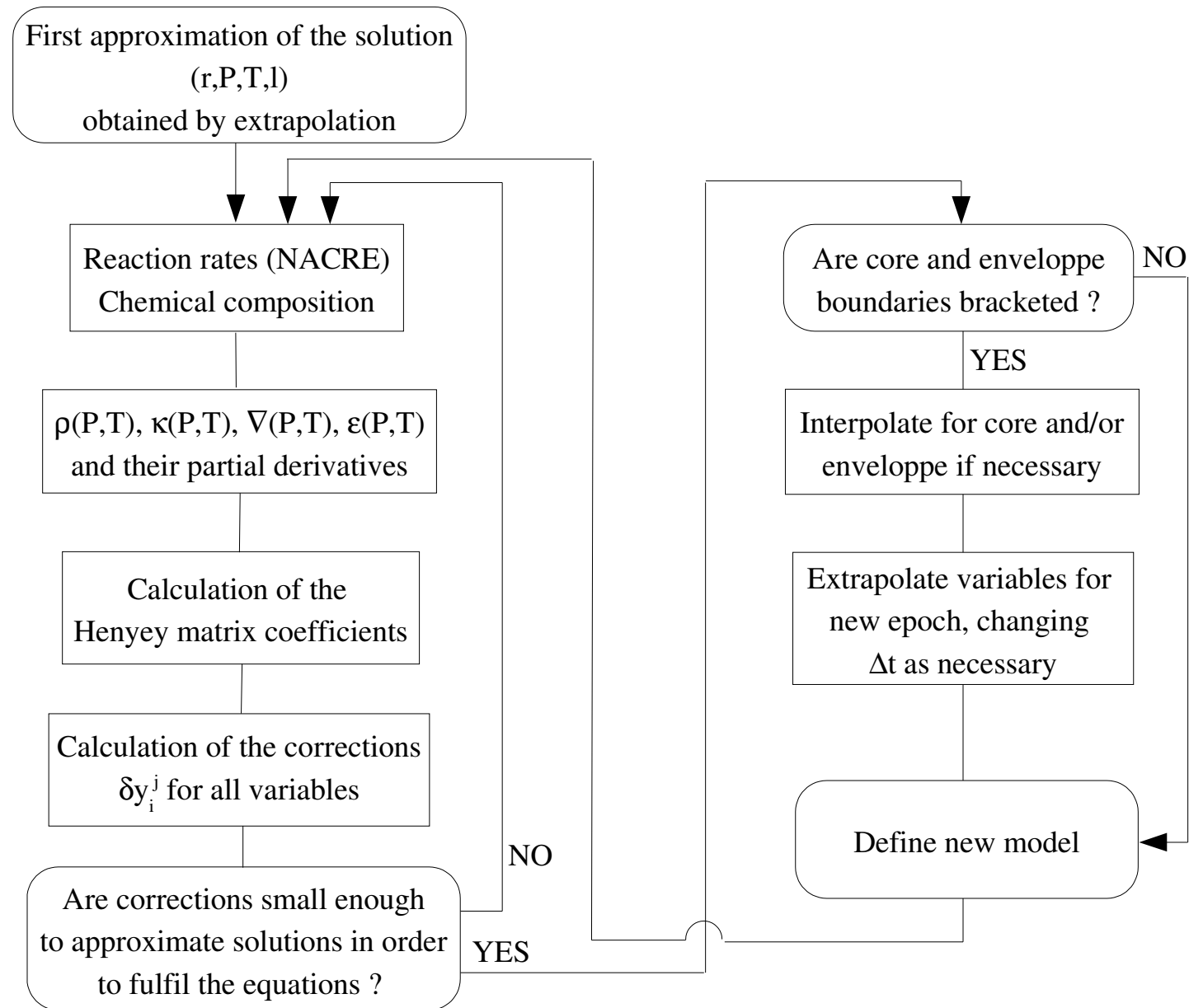
$$B_1 = y_2^1 - \pi(y_1^1, y_4^1) = 0 , \quad B_2 = y_3^1 - \theta(y_1^1, y_4^1) = 0$$

- Calculation by **iteration** :

first approximation  $(y_i^j)_1$  of the solution obtained by extrapolation of a previous solution

corrections for all variables such as :  $(y_i^j)_2 = (y_i^j)_1 + \delta y_i^j$

**Henye matrix** composed by the derivatives of the equations with respect to the  $y_i^j$



Henyey et al., 1964

## Non-standard process

- **Microscopic diffusion : gravitational settling and thermal diffusion** (Chapman & Cowling, Paquette 86)
- **Different kinds of mixing :**
  - Zahn 92 : turbulent mixing
  - Richard 96 :  $\mu$ -gradient cutoff
  - Théado 2003 : meridional circulation
- **Overshooting**
- **Radiative forces in progress**